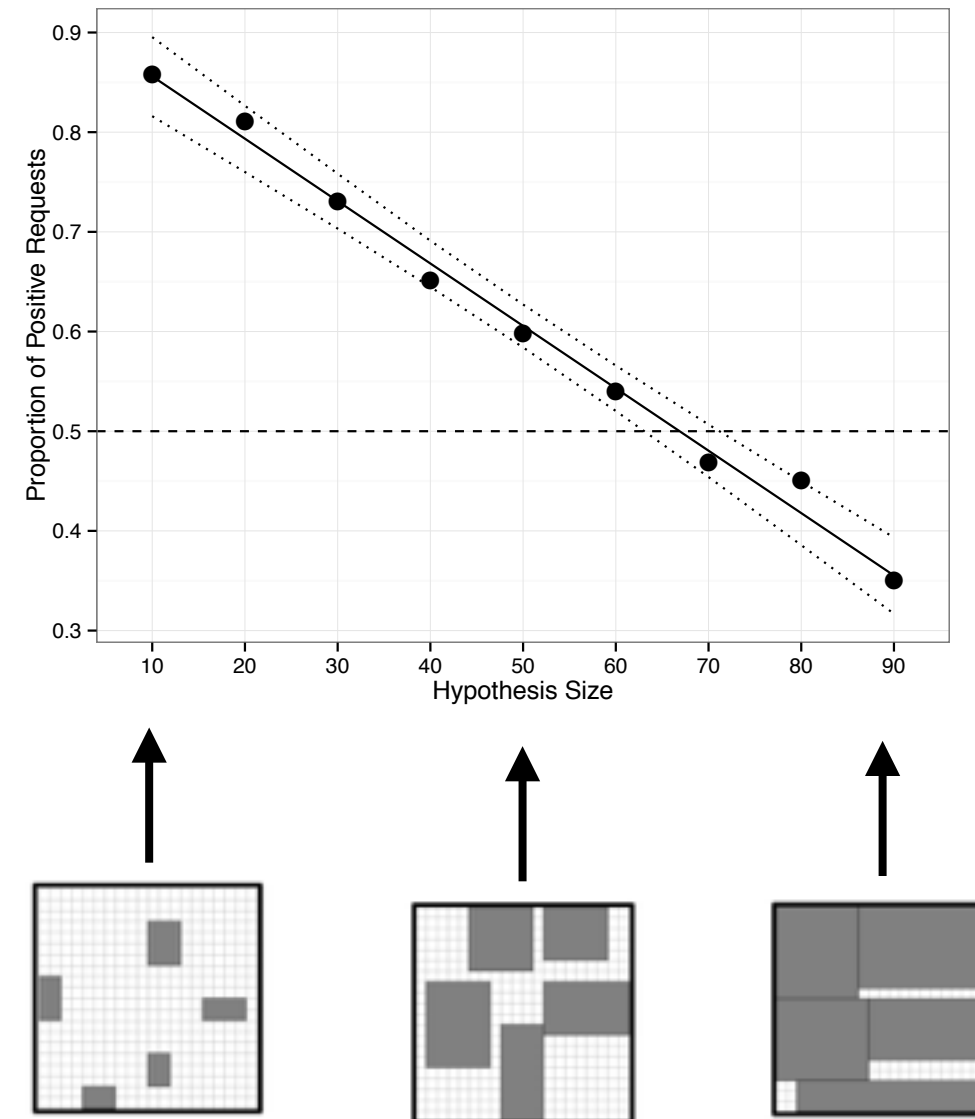


# On the origins of data

Dan Navarro  
University of Adelaide

The lab has been busy lately, and I really  
wanted to talk about all their good  
work...

# Drew has cool stuff looking at the kind of evidence people prefer to learn from...

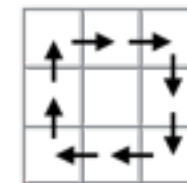


Hendrickson, Navarro & Perfors (under revision). Sensitivity to hypothesis size during information search. *Decision*

# Steve has cool stuff looking at how people learn (and use) “admissable” stimulus transformations



Movement transformation

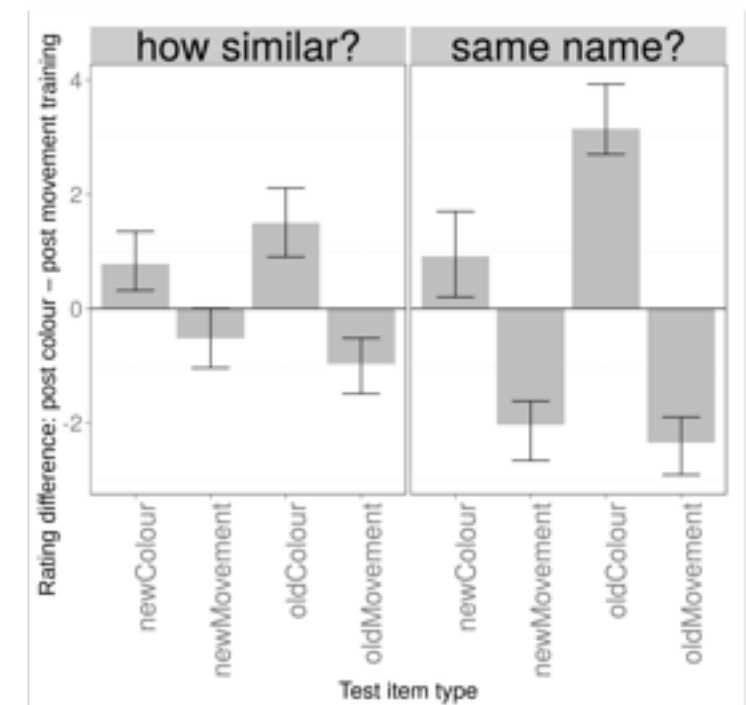
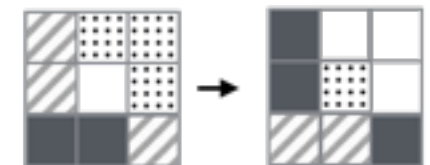
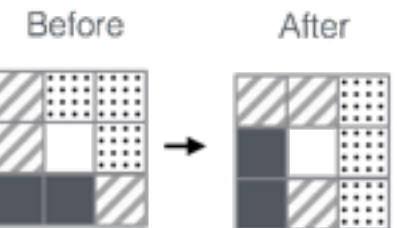


Color transformation

red  $\longleftrightarrow$  green  
yellow  $\longleftrightarrow$  blue

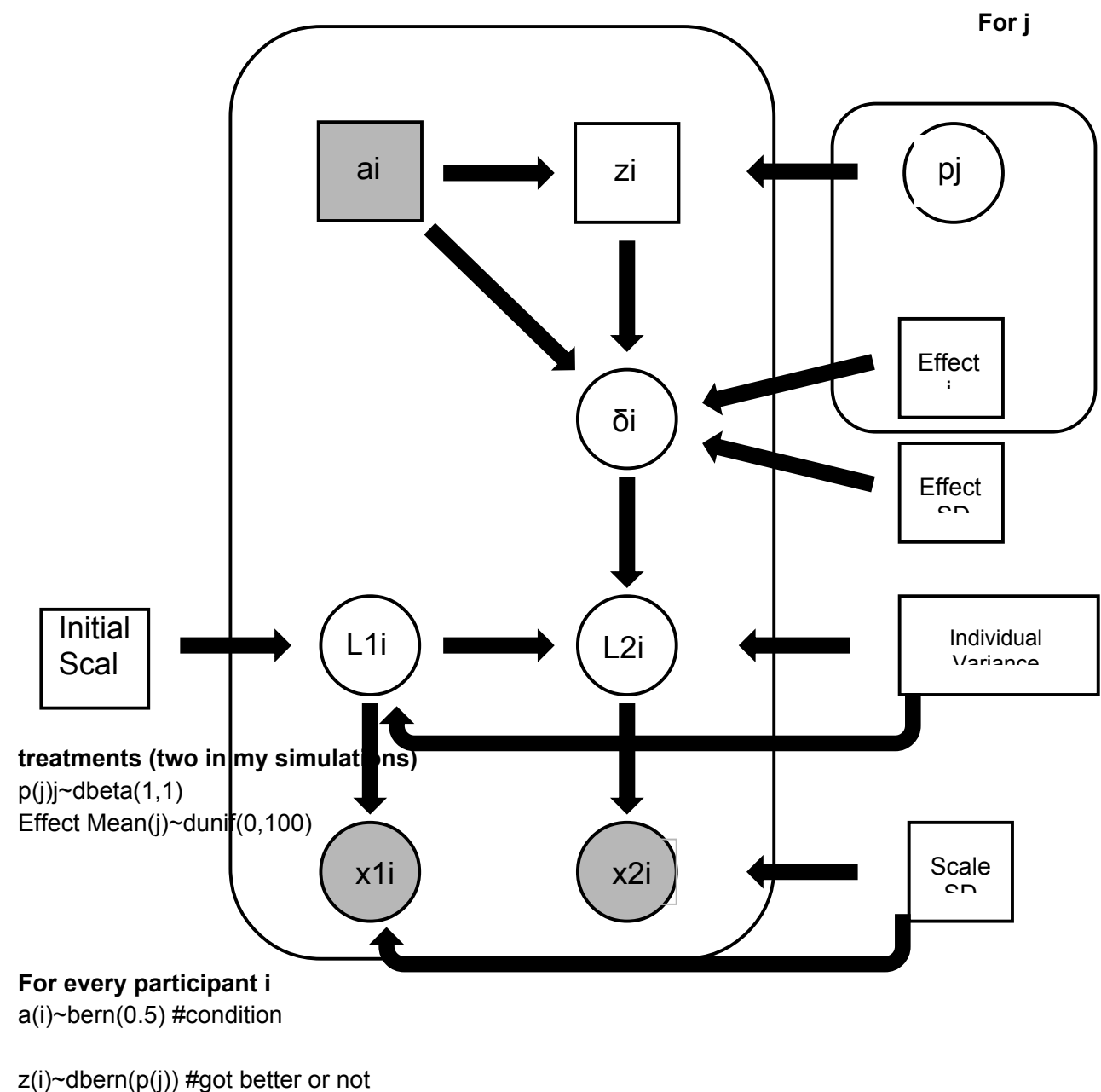
Definition

Example

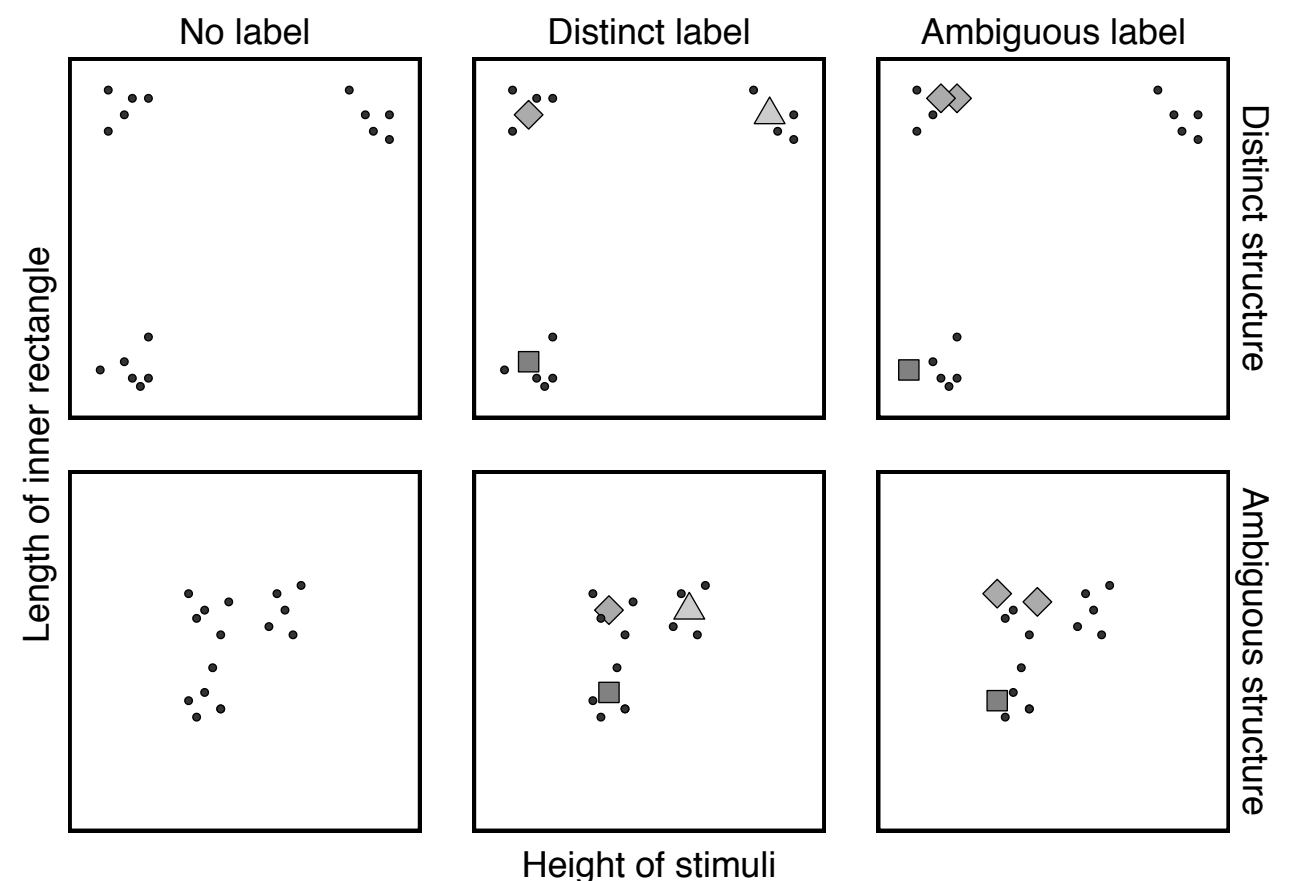


Langsford, Navarro, Perfors & Hendrickson (under review).  
Transformation learning and its effect on similarity. *JEP:LMC*

Lauren has some scarily effective ideas about how the analysis of clinical trials could be done better...



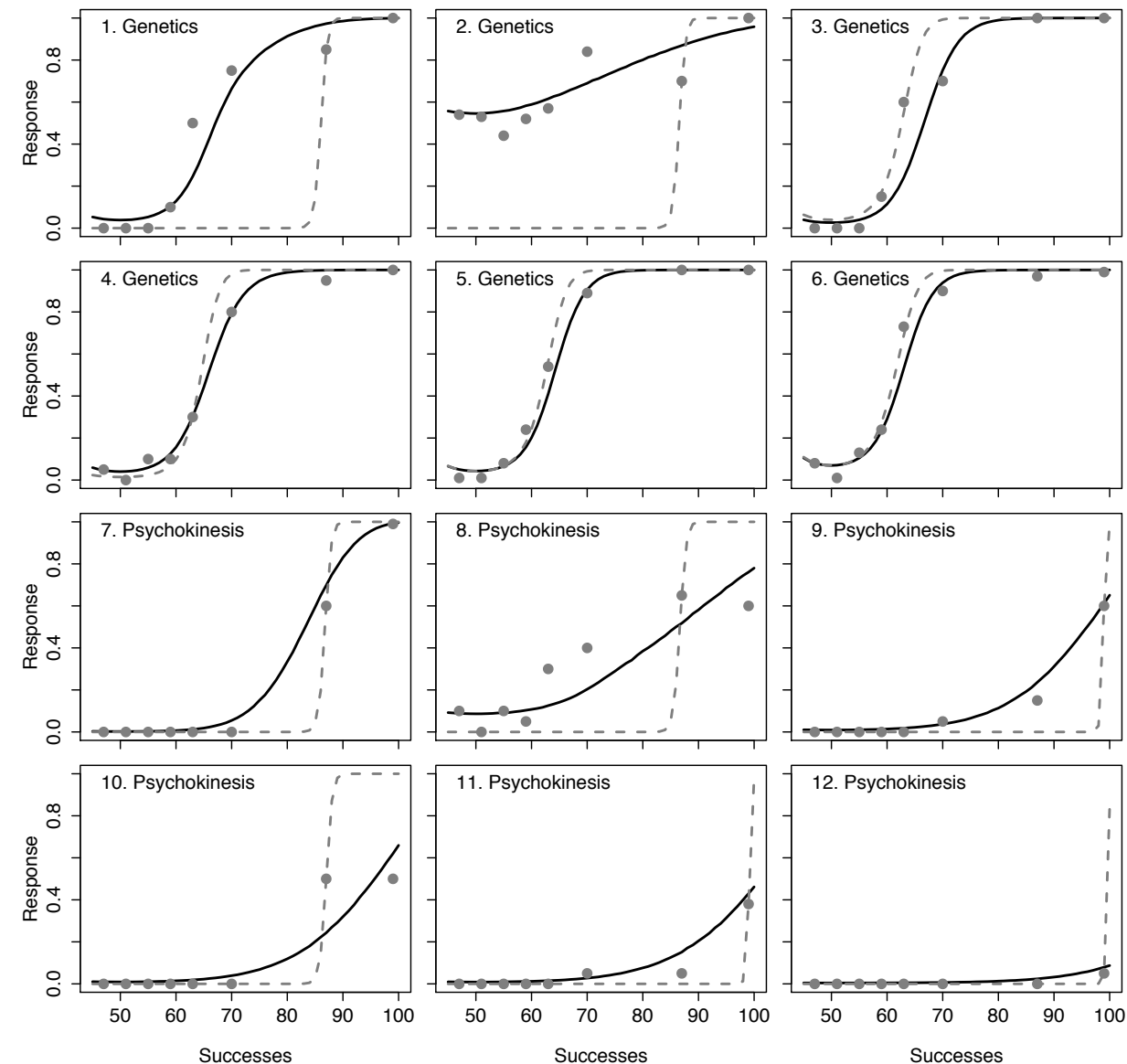
# Wai Keen thinks much of the semi-supervised learning literature is missing the point...



Vong, Perfors & Navarro (in press). The helpfulness of category labels in semi-supervised learning depends on category structure. *Psychonomic Bulletin and Review*

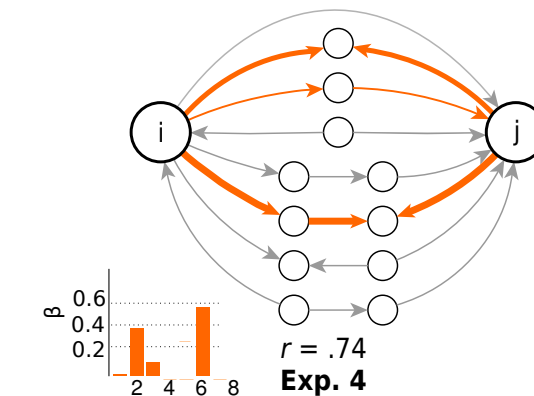
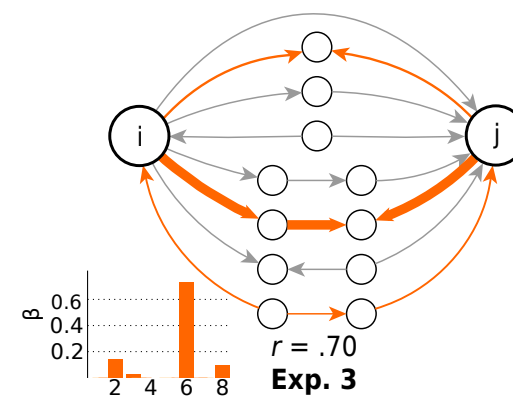
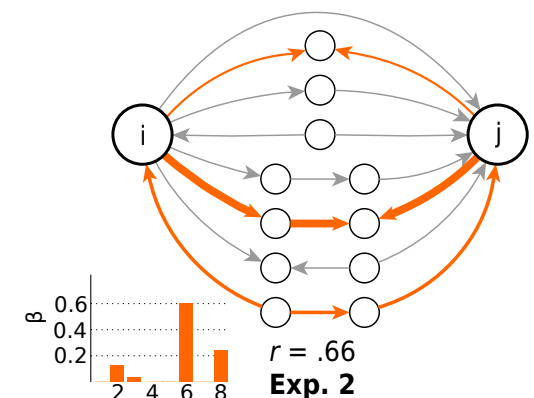
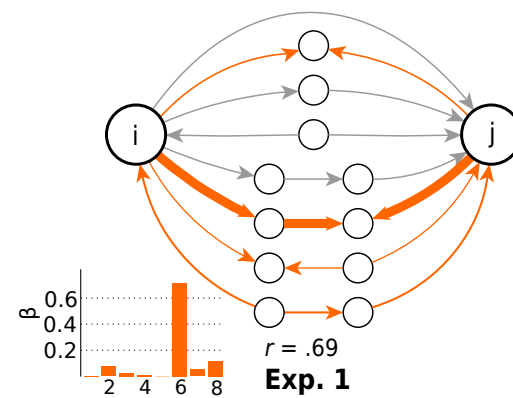
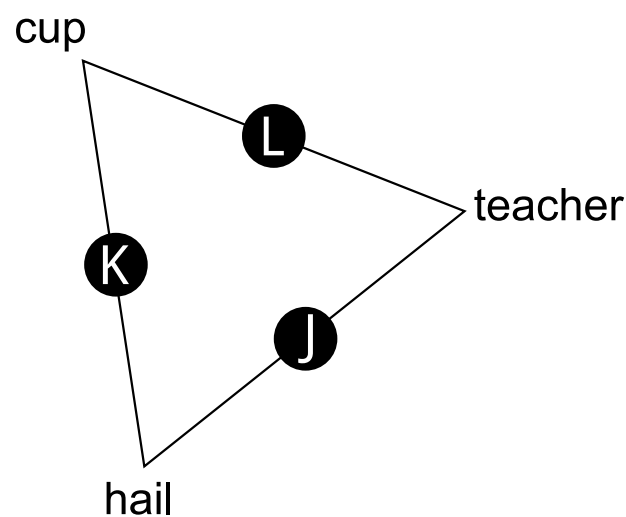


# Sean has an awesome rant about how Bayesian cognitive modeling ought to work



Tauber, Navarro, Perfors & Steyvers (in preparation). Bayesian models of cognition revisited: Letting go of optimality and letting data drive psychological theory. *Psych Review*?

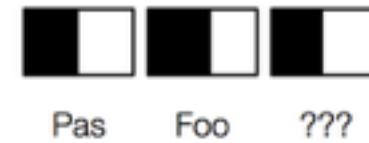
# Simon has a semantic network model for predicting similarities between very unrelated words



De Deyne, Navarro, Perfors, Storms (submitted?). Structure at every scale: A semantic network account of the similarities between very unrelated concepts. *JEP:G*

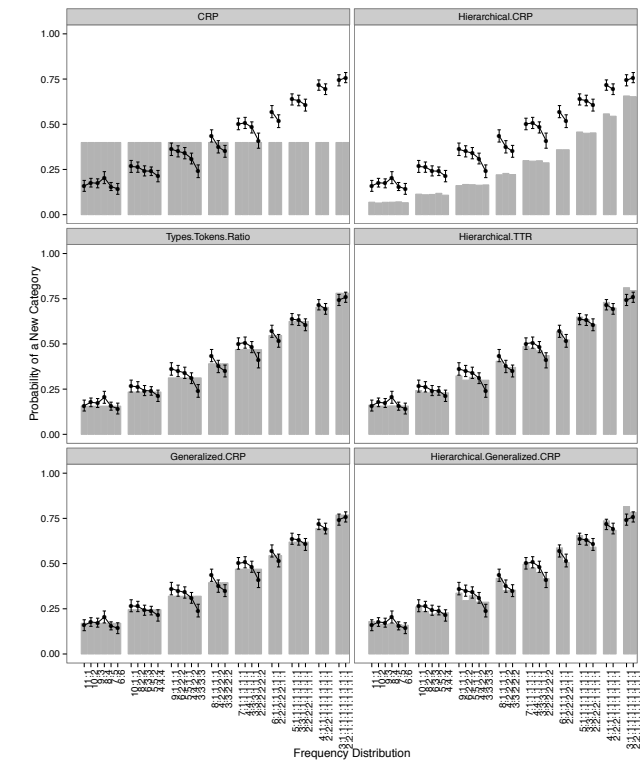
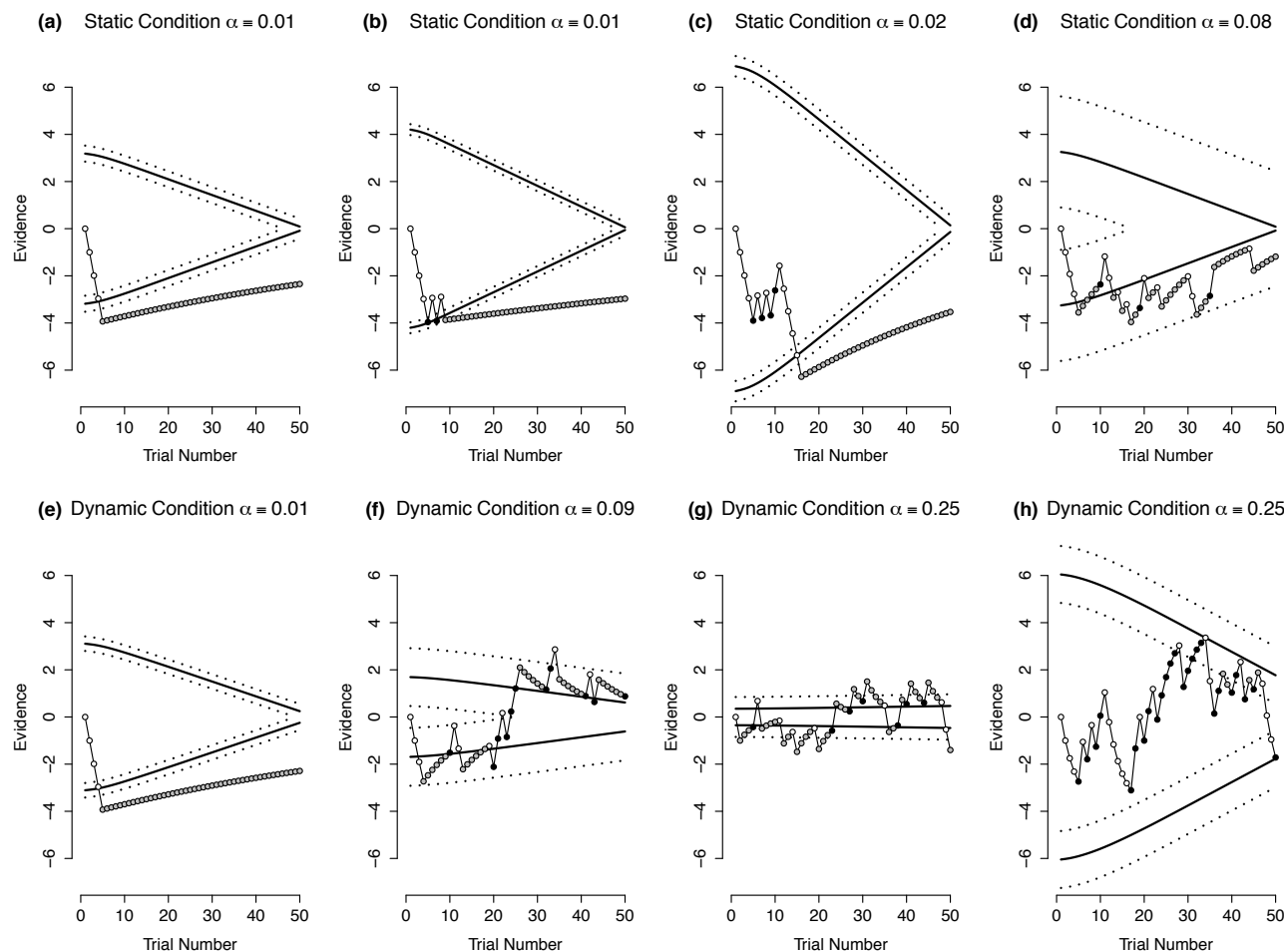


# (Even I've been doing research)



Which category does this belong to?

Pas      Foo      New



Navarro, Newell & Schulze (under revision). Learning and choosing in an uncertain world: An investigation of the explore-exploit dilemma in static and dynamic environments. *Cognitive Psychology*

Navarro & Kemp (in preparation). None of the above: A Bayesian account of the selection of novel categories. *Psych Review*?

In the end, I had to ignore most people  
and concentrate on one line of work...

:-)



Navarro, Dry & Lee (2012). Sampling assumptions in inductive generalization. *Cognitive Science*



**Hendrickson**, Perfors & Navarro (in preparation). One cat, two cats: Sampling models in different category learning tasks produce qualitatively different inductive generalisations



**Ransom**, Perfors & Navarro (in press). Leaping to conclusions: Why premise relevance affects argument strength. *Cognitive Science*



**Voorspoels**, Navarro, Perfors, Ransom & Storms (under revision). How do people learn from negative evidence? Non-monotonic generalizations and sampling assumptions in inductive reasoning. *Cognitive Psychology*



Perfors, Navarro & Shafto (in preparation). Stronger evidence isn't always better: The role of social inference in evidence selection and interpretation.



Navarro, Dry & Lee (2012). Sampling assumptions in inductive generalization. *Cognitive Science*



**Drew Hendrickson**, Perfors & Navarro (in preparation). One cat, two cats: Sampling models in different category learning tasks produce qualitatively different inductive generalisations



**Keith Ransom**, Perfors & Navarro (in press). Leaping to conclusions: Why premise relevance affects argument strength. *Cognitive Science*

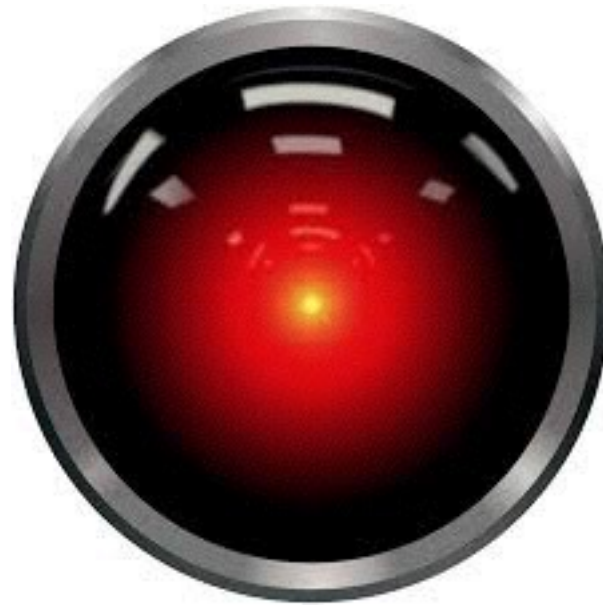


**Wouter Voorspoels**, Navarro, Perfors, Ransom & Storms (under revision). How do people learn from negative evidence? Non-monotonic generalizations and sampling assumptions in inductive reasoning. *Cognitive Psychology*

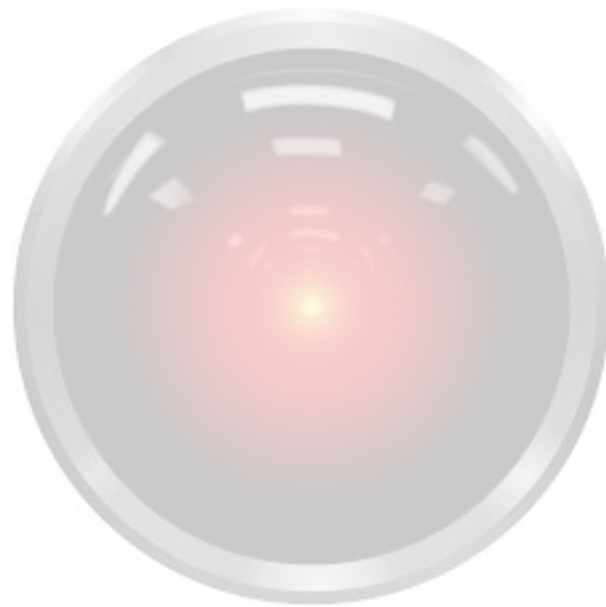


Perfors, Navarro & Shafto (in preparation). Stronger evidence isn't always better: The role of social inference in evidence selection and interpretation.

So... I want to build a smart machine, and I want it to do human-like inductive reasoning



So... I want to build a smart machine, and I want it to do human-like inductive reasoning



**I want it to have common sense**



So I have to ask...

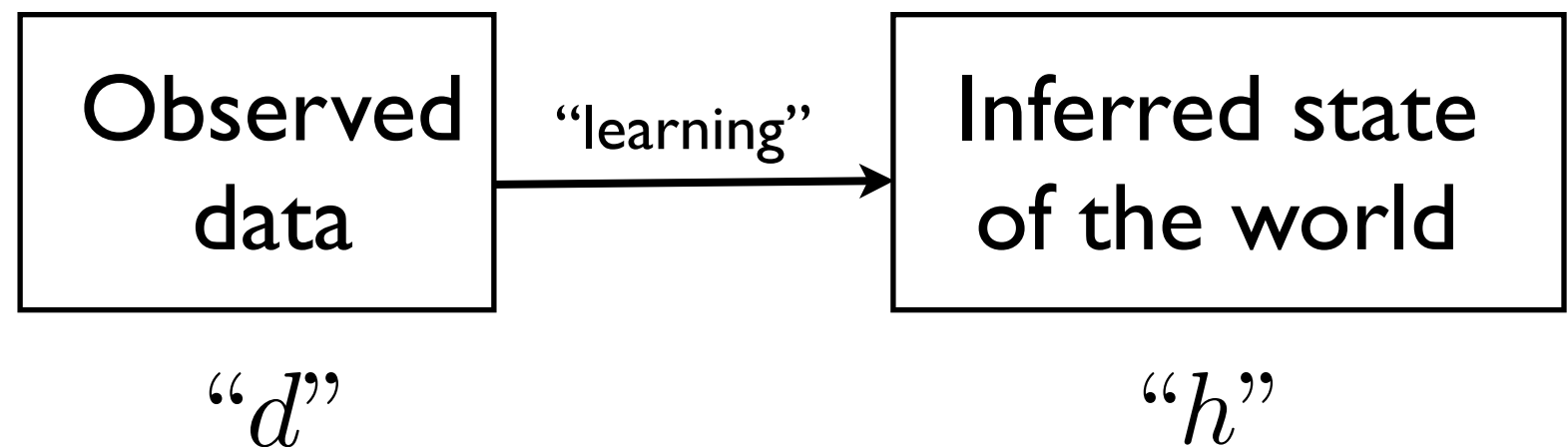
Why isn't inductive inference simple?

# Why isn't inductive inference simple?



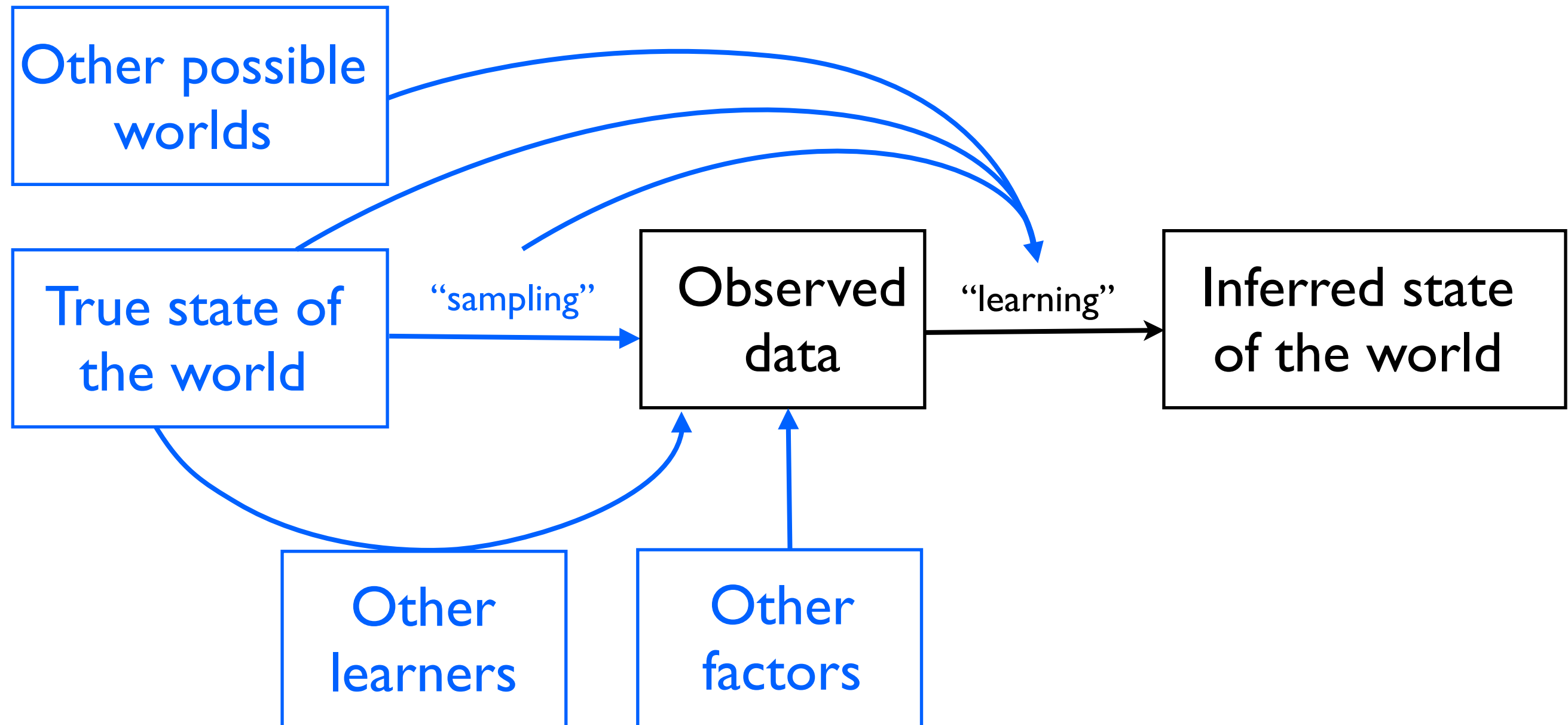
$$P(h|d) = \frac{P(d|h)P(h)}{P(d)}$$

# A simple learning rule...



$$P(h|d) = \frac{P(d|h)P(h)}{P(d)}$$

... hides a lot of complexity



And what this means is that even  
“simple” problems become  
surprisingly tricky...



$$P(h|d) = \frac{P(d|h)P(h)}{P(d)}$$

# Sampling assumptions in simple generalisation problems





Navarro, Dry & Lee (2012). Sampling assumptions in inductive generalization. *Cognitive Science*



Hendrickson, Perfors & Navarro (in preparation). One cat, two cats: Sampling models in different category learning tasks produce qualitatively different inductive generalisations



Ransom, Perfors & Navarro (in press). Leaping to conclusions: Why premise relevance affects argument strength. *Cognitive Science*



Voorspoels, Navarro, Perfors, Ransom & Storms (under revision). How do people learn from negative evidence? Non-monotonic generalizations and sampling assumptions in inductive reasoning. *Cognitive Psychology*



Perfors, Navarro & Shafto (in preparation). Stronger evidence isn't always better: The role of social inference in evidence selection and interpretation. Previously rejected from *JEP:G*



“tufa”



“tufa”



“tufa”

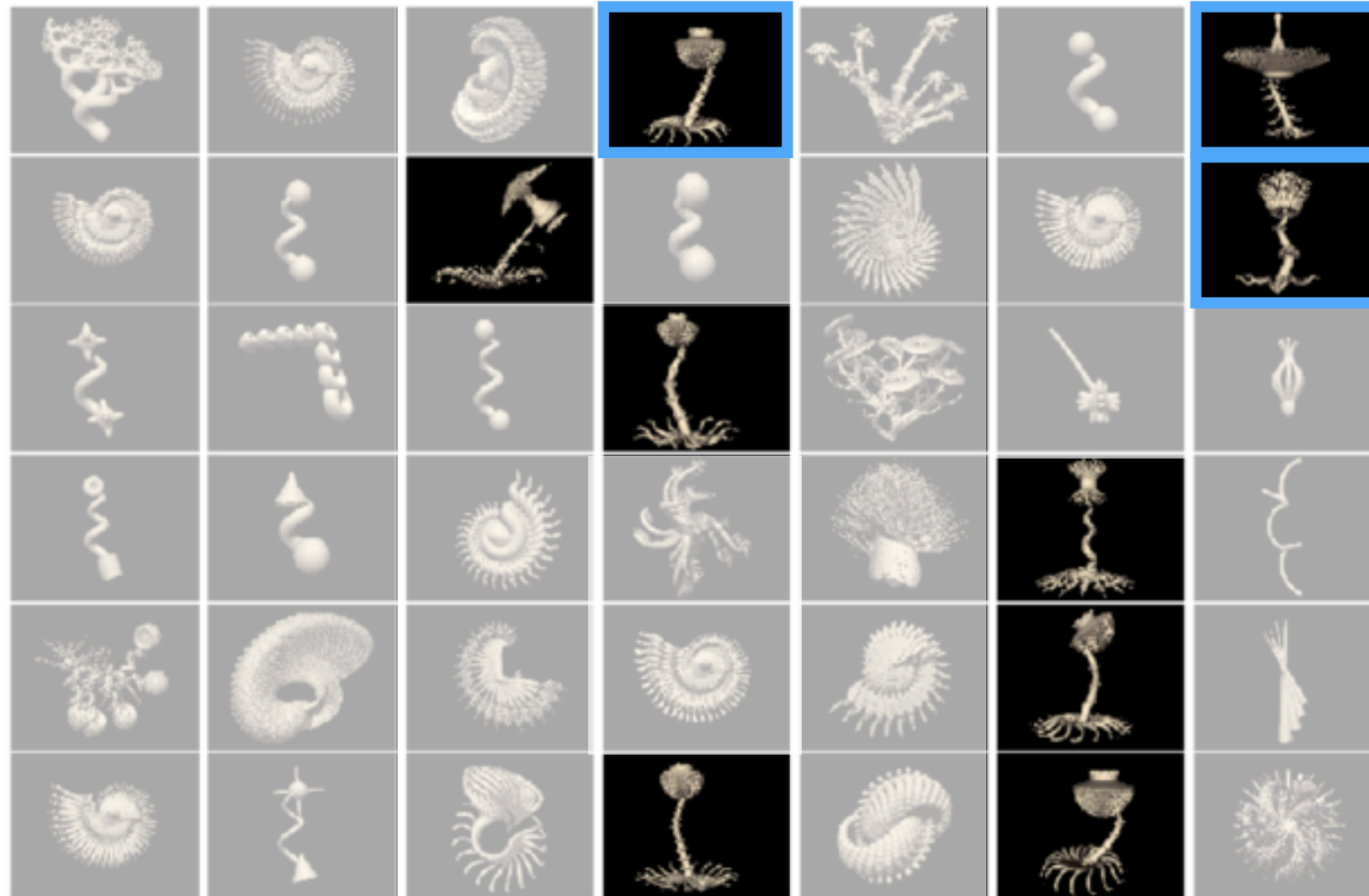


“tufa”

“tufa”



“tufa”



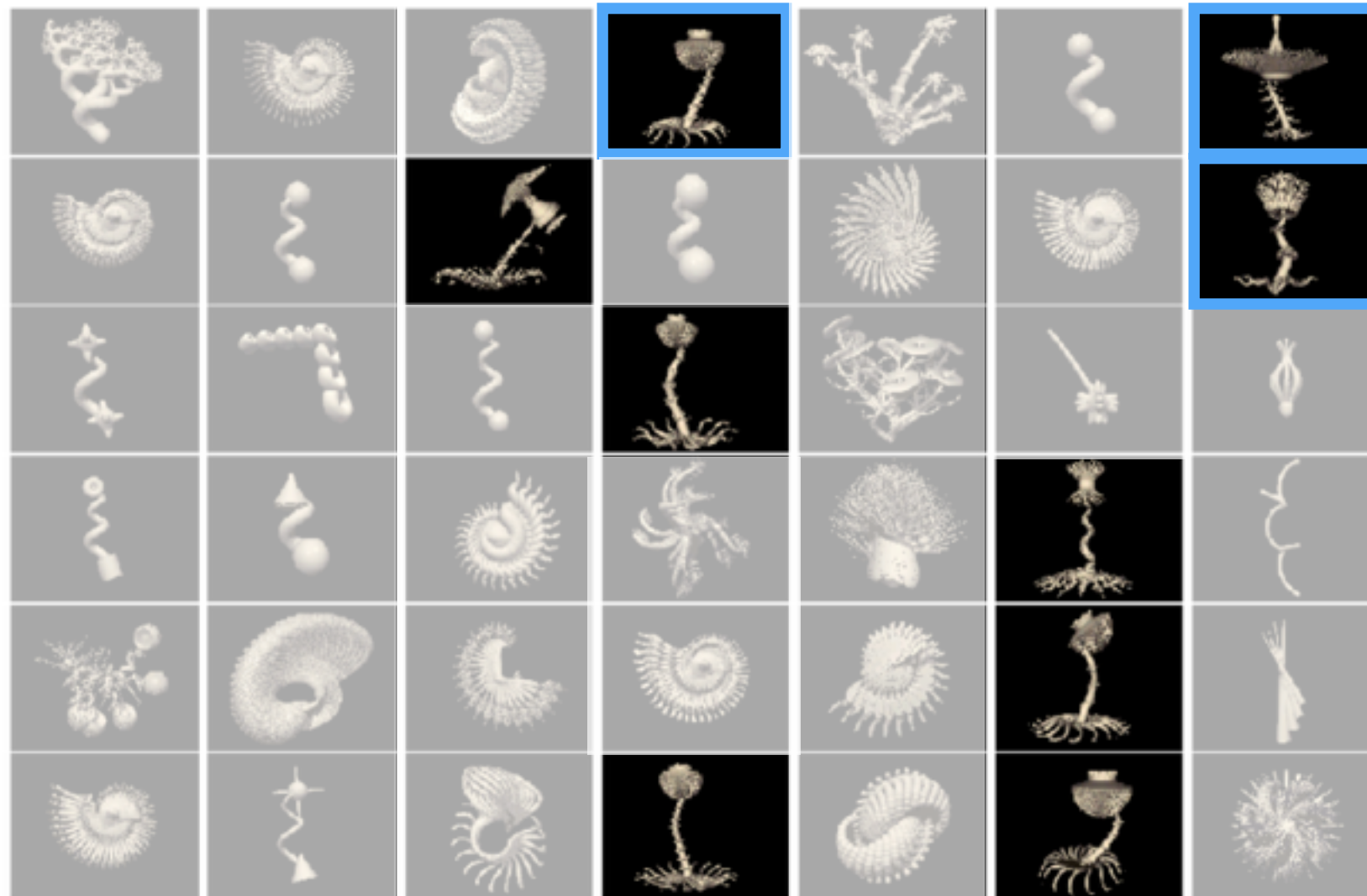
“tufa”

“tufa”



# Why should generalizations become narrower with more positive examples?

“tufa”



“tufa”

“tufa”

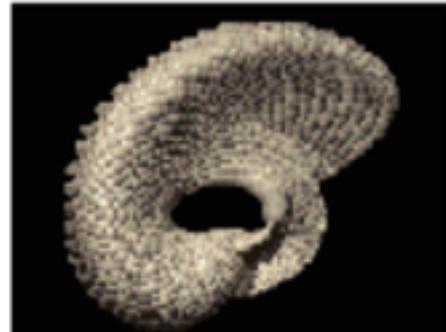
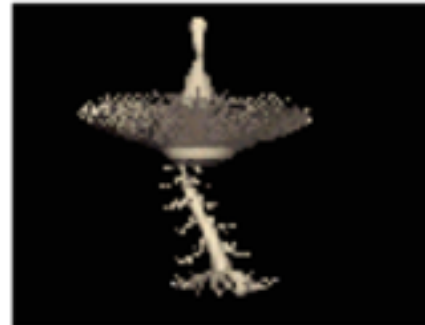
There is a puzzle here...



"The null hypothesis is never proved or established, but is possibly disproved, in the course of experimentation. Every experiment may be said to exist only to give the facts a chance of disproving the null hypothesis."

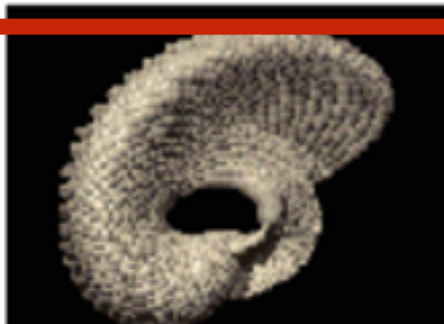
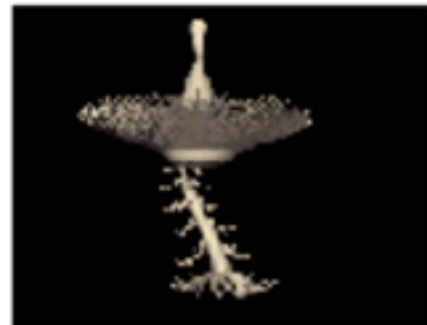
- R.A. Fisher

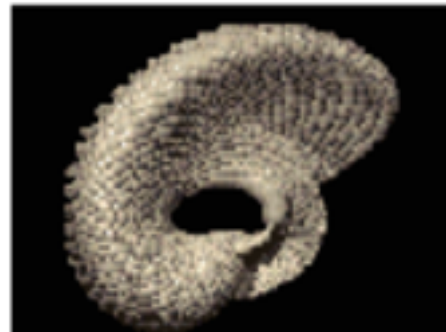
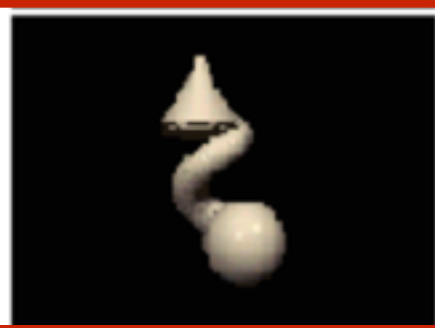
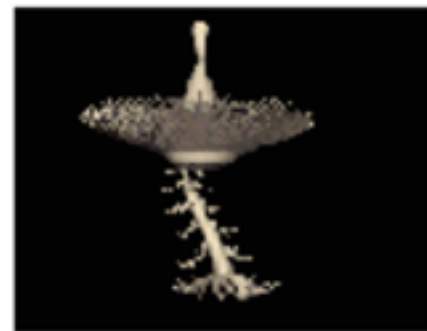
Okay let's reason like a falsificationist...



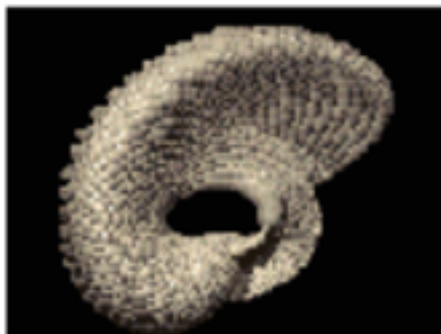
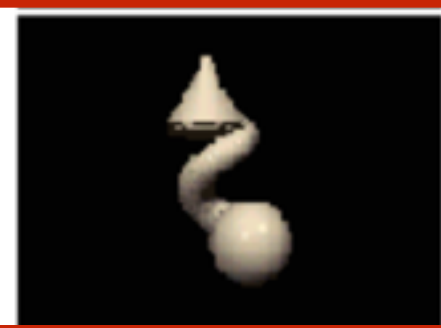
Here are some  
objects

And seem  
plausible a priori  
hypotheses for  
the extension of  
a novel category



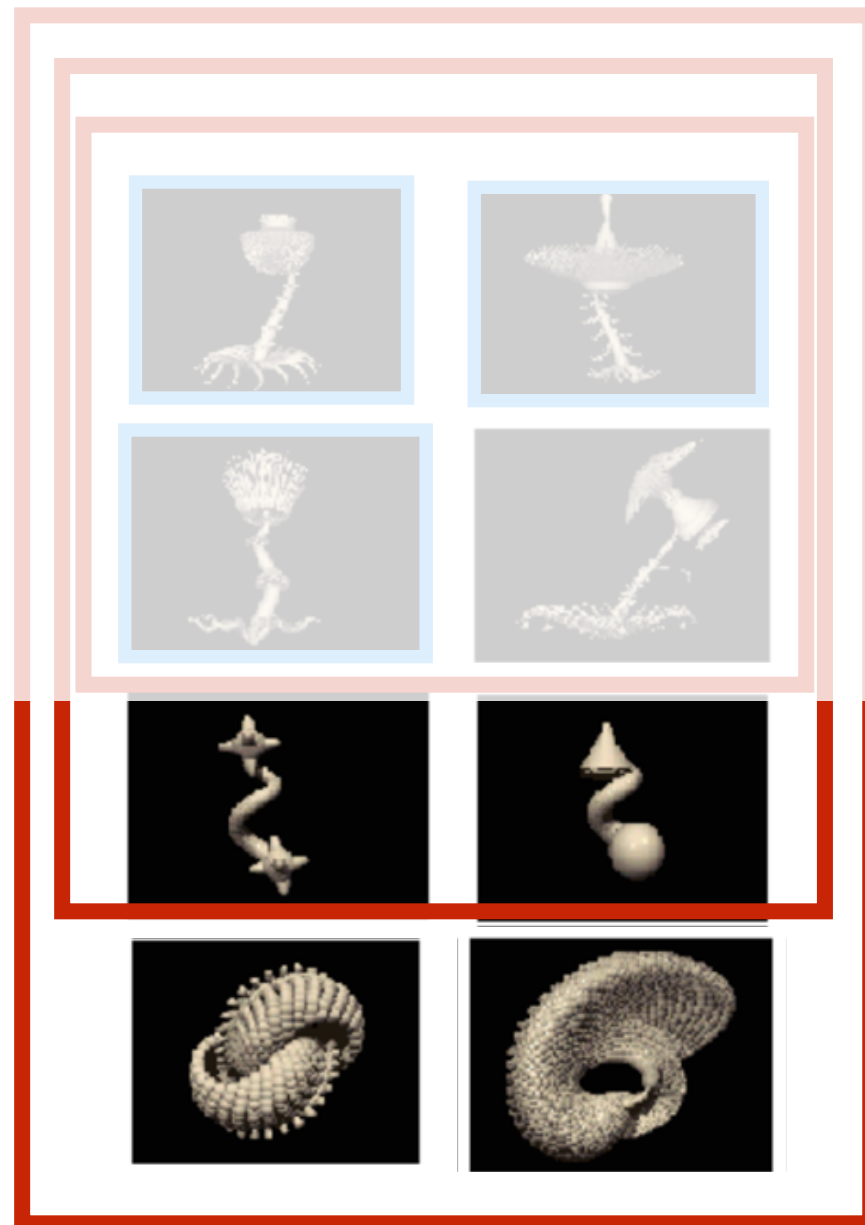
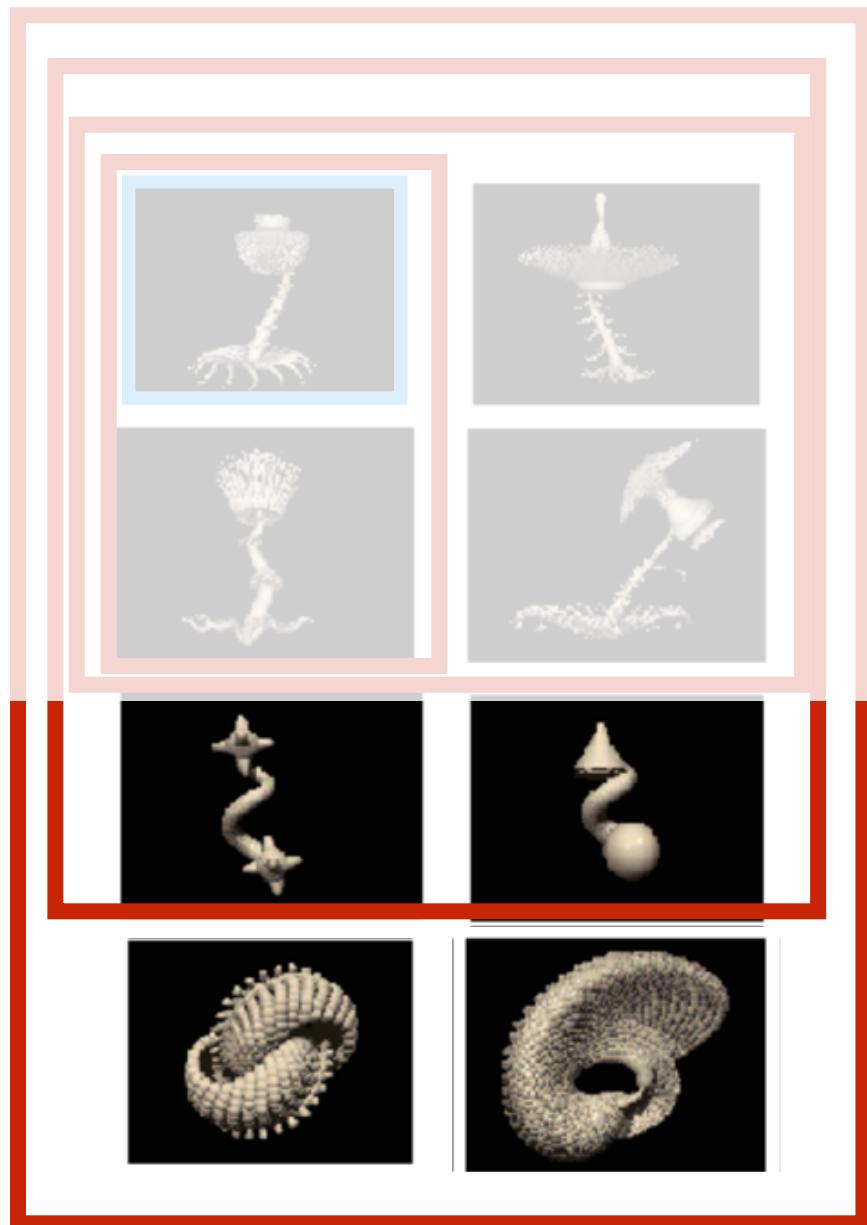


The first labelled  
object eliminates  
some hypotheses

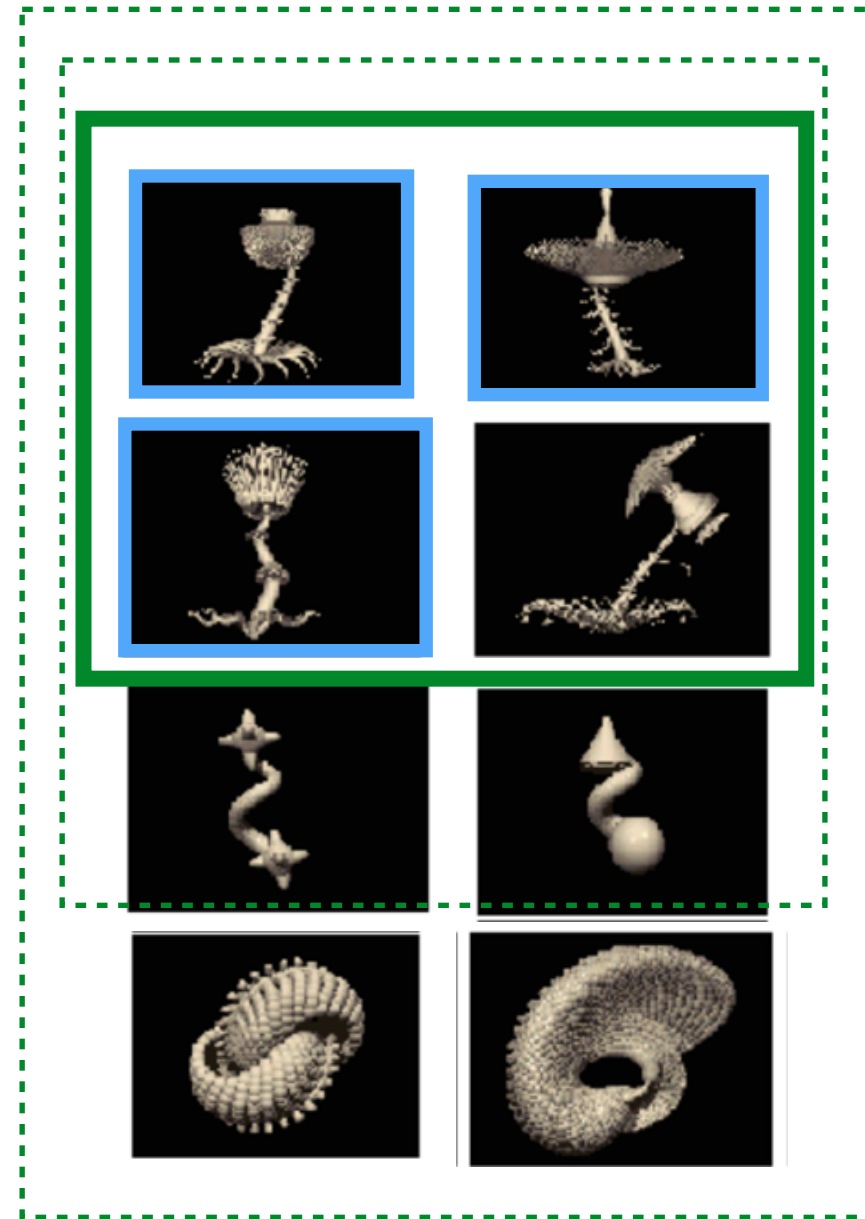


... and two more

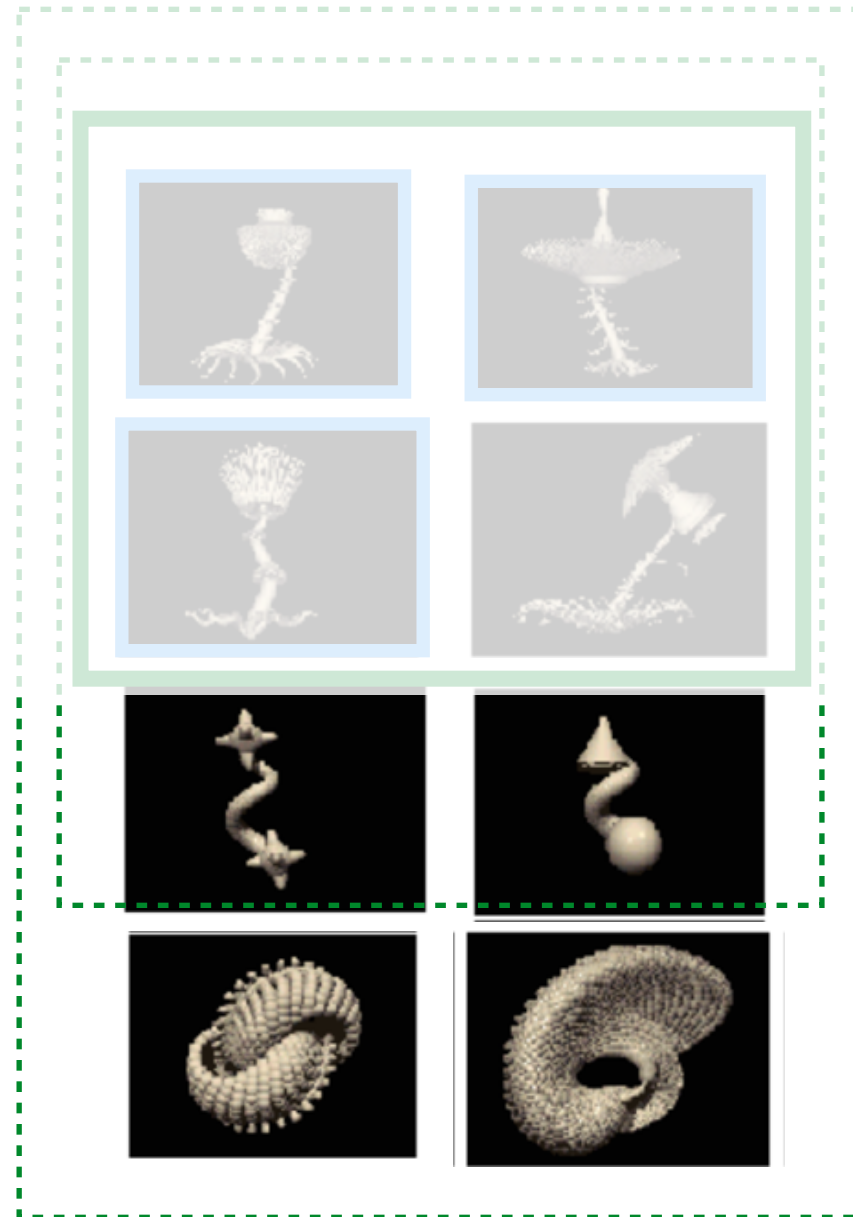
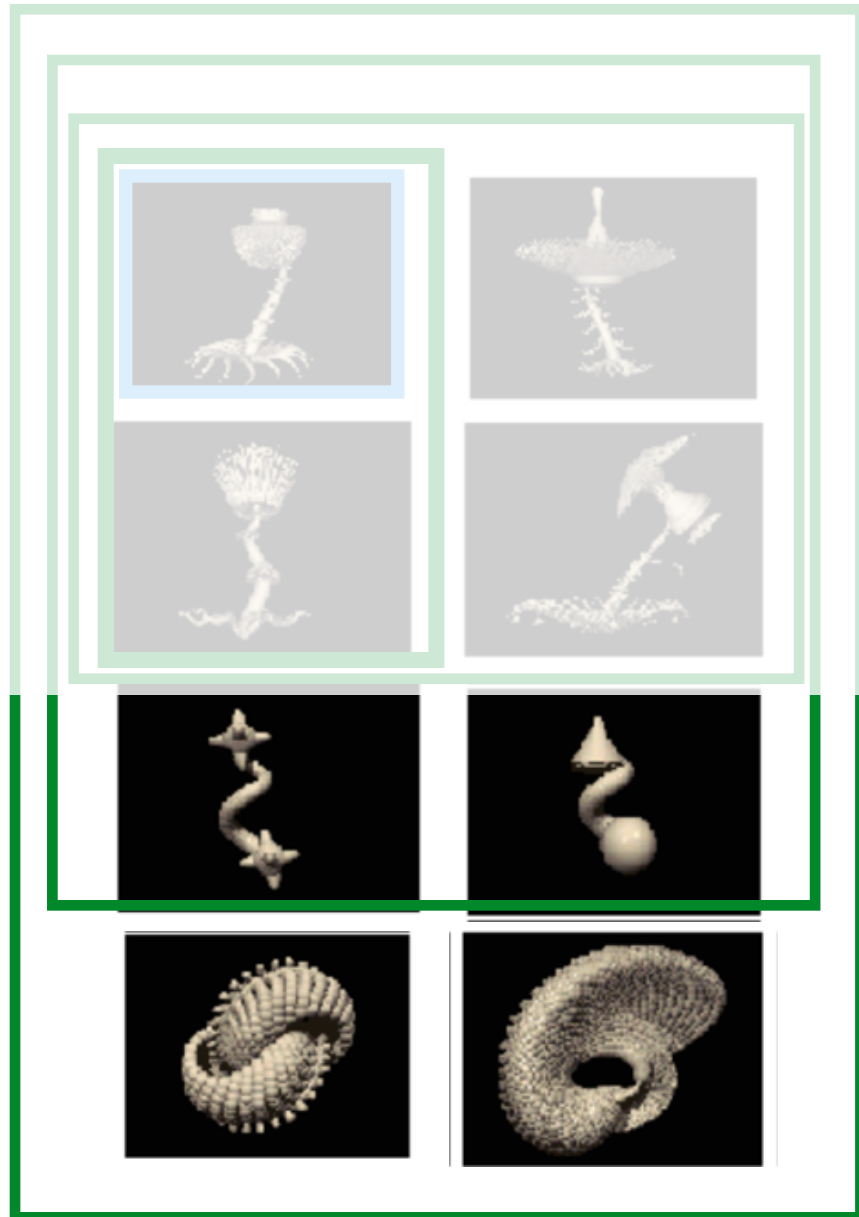




Generalization to these items should be the same in both cases. It is not



Ockham's razor: the smaller hypothesis provides a simpler explanation for why all the observed tufas look so damn similar



Generalizations should tighten around the positive exemplars as the sample size increases

# A tale of two Bayesians



$$P(h|d) = \frac{P(d|h)P(h)}{P(d)}$$

$$P(h|d) = \frac{P(d|h)P(h)}{P(d)}$$

Bayes' rule:

$$P(h|x) \propto P(x|h)P(h)$$



Posterior  
degree of belief



Prior degree  
of belief

A Bayesian “scores” hypotheses by asking  
how likely they think it is that we data  $x$   
would be if hypothesis  $h$  were true?



$$P(h|x) \propto P(x|h)P(h)$$

The likelihood is the learner's theory about the problem they're solving



$$P(h|x) \propto P(x|h)P(h)$$

# Different theories, different learning



$$P(h|d) = \frac{P(d|h)P(h)}{P(d)}$$

$$P(h|d) = \frac{P(d|h)P(h)}{P(d)}$$



# Two very simple theories...

Weak sampling:

“select an item at random and then provide the category label”



# Two very simple theories...

Weak sampling:

“select an item at random and then provide the category label”



Strong sampling:

“make sure you pick an item that actually belongs to the target category”



... produce two different learning rules

Weak sampling:

$$P(x|h) \propto \begin{cases} 1 & \text{if } x \in h \\ 0 & \text{otherwise} \end{cases}$$



Strong sampling:

$$P(x|h) = \begin{cases} \frac{1}{|h|} & \text{if } x \in h \\ 0 & \text{otherwise} \end{cases}$$



# And qualitatively different behaviour

Weak sampling:

Act like a falsificationist



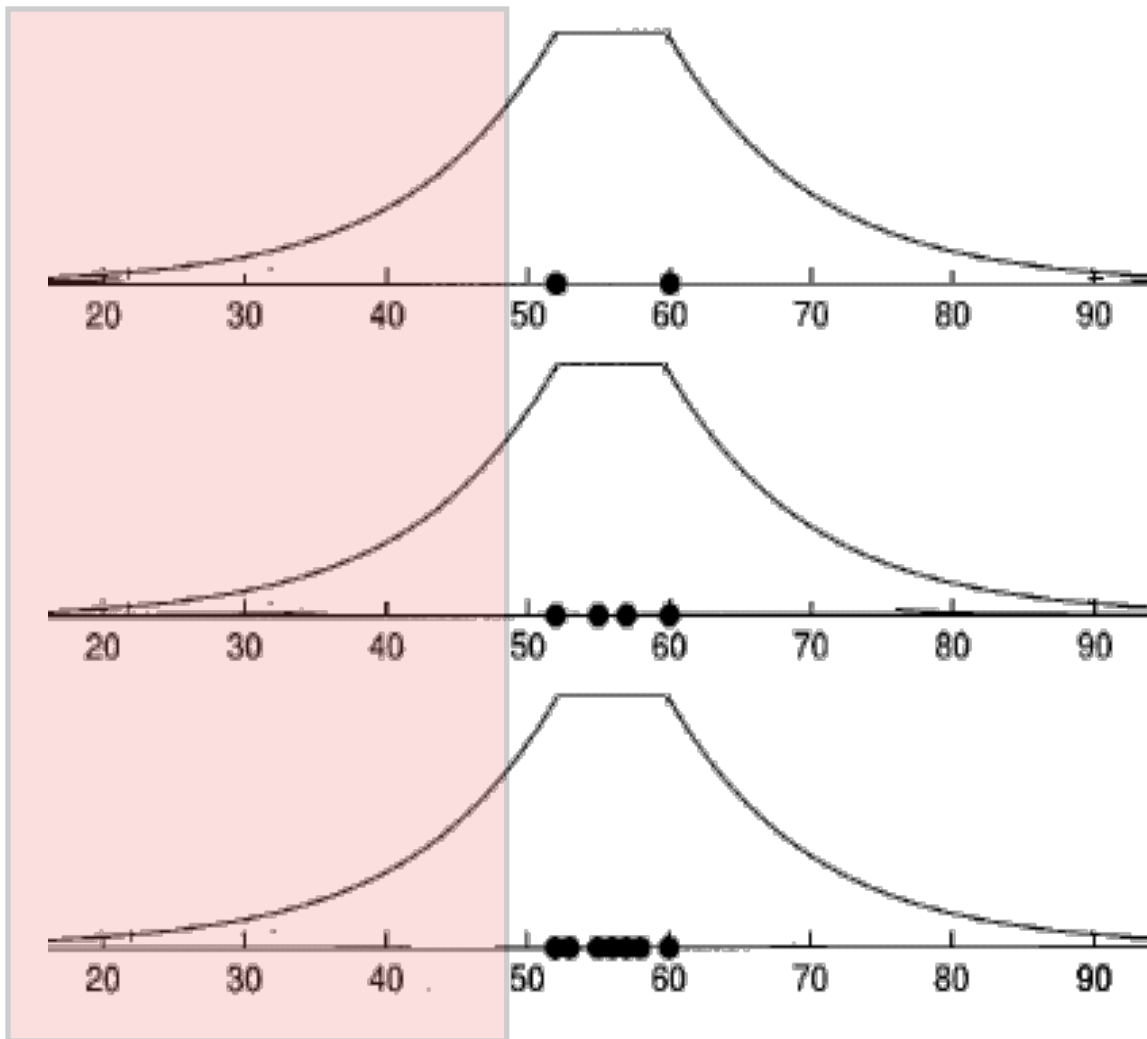
Strong sampling:

Apply Ockham's razor: prefer  
small/simple hypotheses

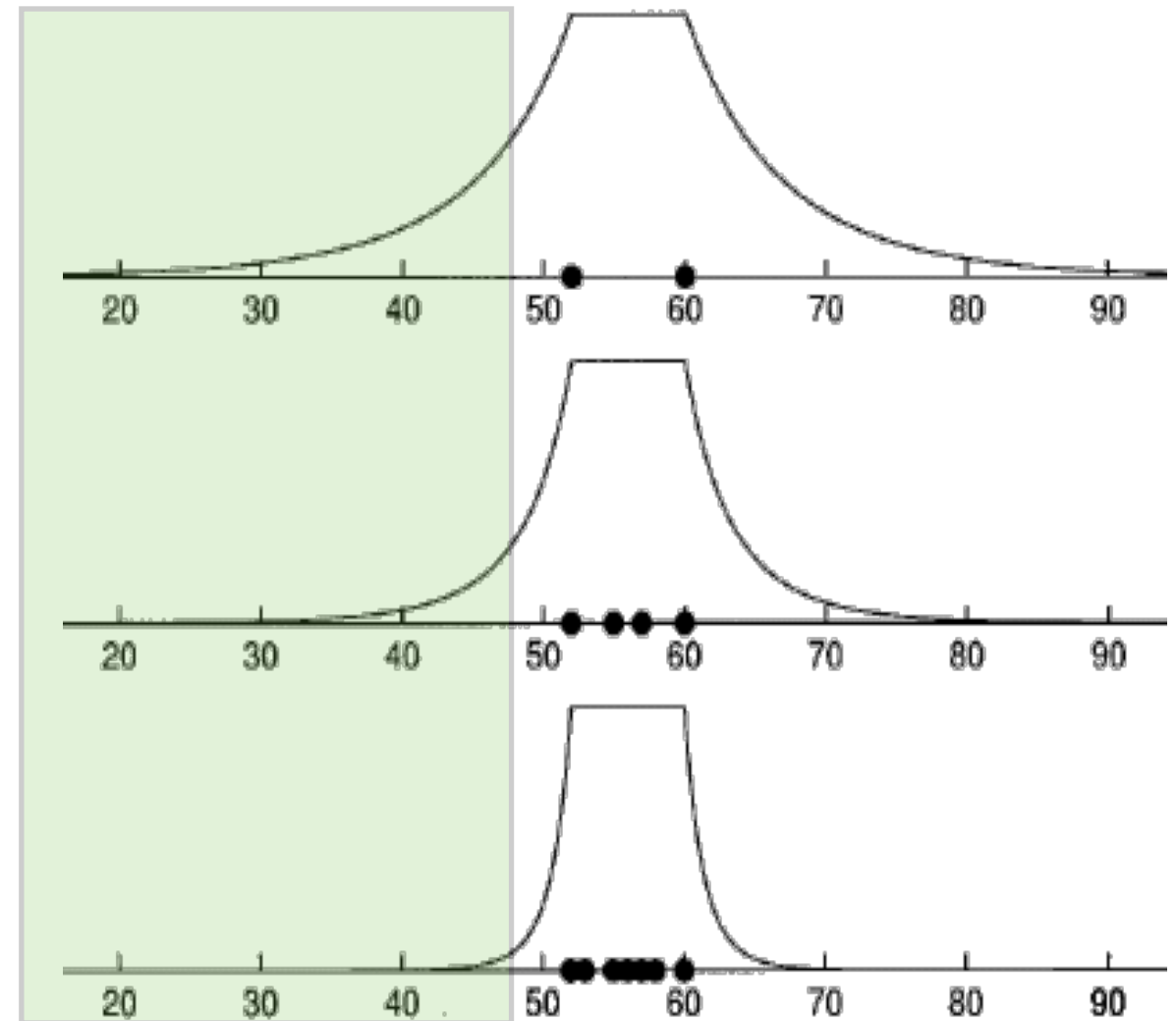


# Here's the testable prediction about generalisation gradients...

weak sampling



strong sampling



# And a series of experimental tests...

- Navarro, Dry & Lee (2012):
  - Two experiments, stimuli varied on one dimension
  - N=22 & N=20 undergraduates
  - Non traditional stimulus presentation
  - Response measure: Probability judgments

# And a series of experimental tests...

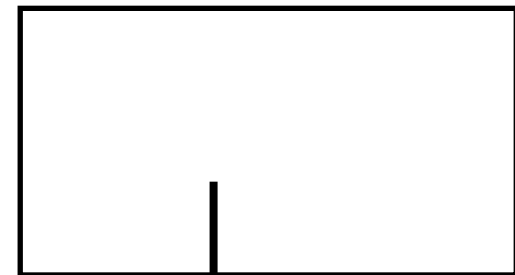
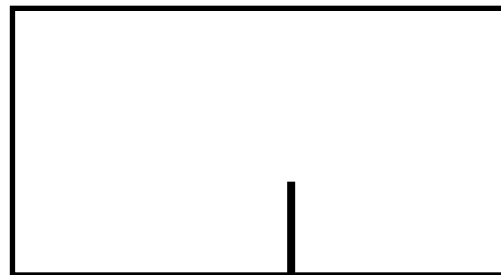
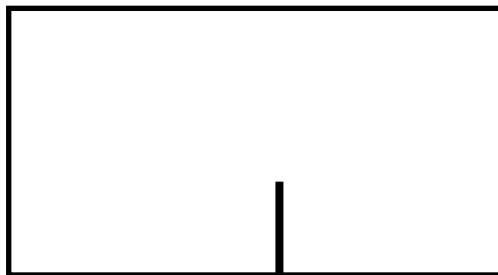
- Navarro, Dry & Lee (2012):
  - Two experiments, stimuli varied on one dimension
  - N=22 & N=20 undergraduates
  - Non traditional stimulus presentation
  - Response measure: Probability judgments
- Vong, Hendrickson, Perfors & Navarro (2013)
  - As above, but with N=318 workers on AMT



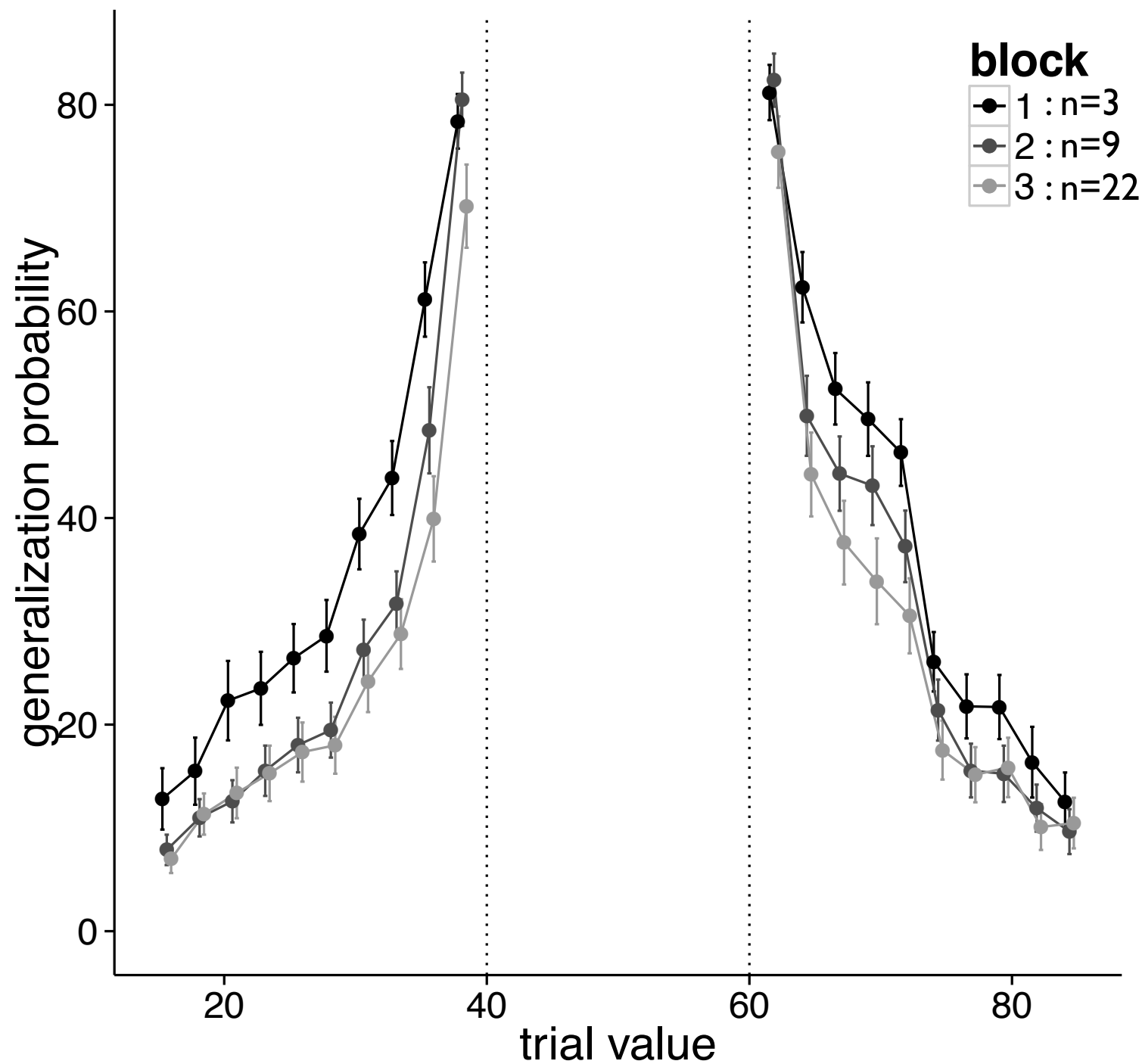
# And a series of experimental tests...

- Navarro, Dry & Lee (2012):
  - Two experiments, stimuli varied on one dimension
  - N=22 & N=20 undergraduates
  - Non traditional stimulus presentation
  - Response measure: Probability judgments
- Vong, Hendrickson, Perfors & Navarro (2013)
  - As above, but with N=318 workers on AMT
- Hendrickson, Perfors & Navarro (in preparation)
  - One experiment (N=470) on AMT
  - Participants shown traditional categorisation stimuli (below)
  - Response measures: probability judgment & categorisation decisions

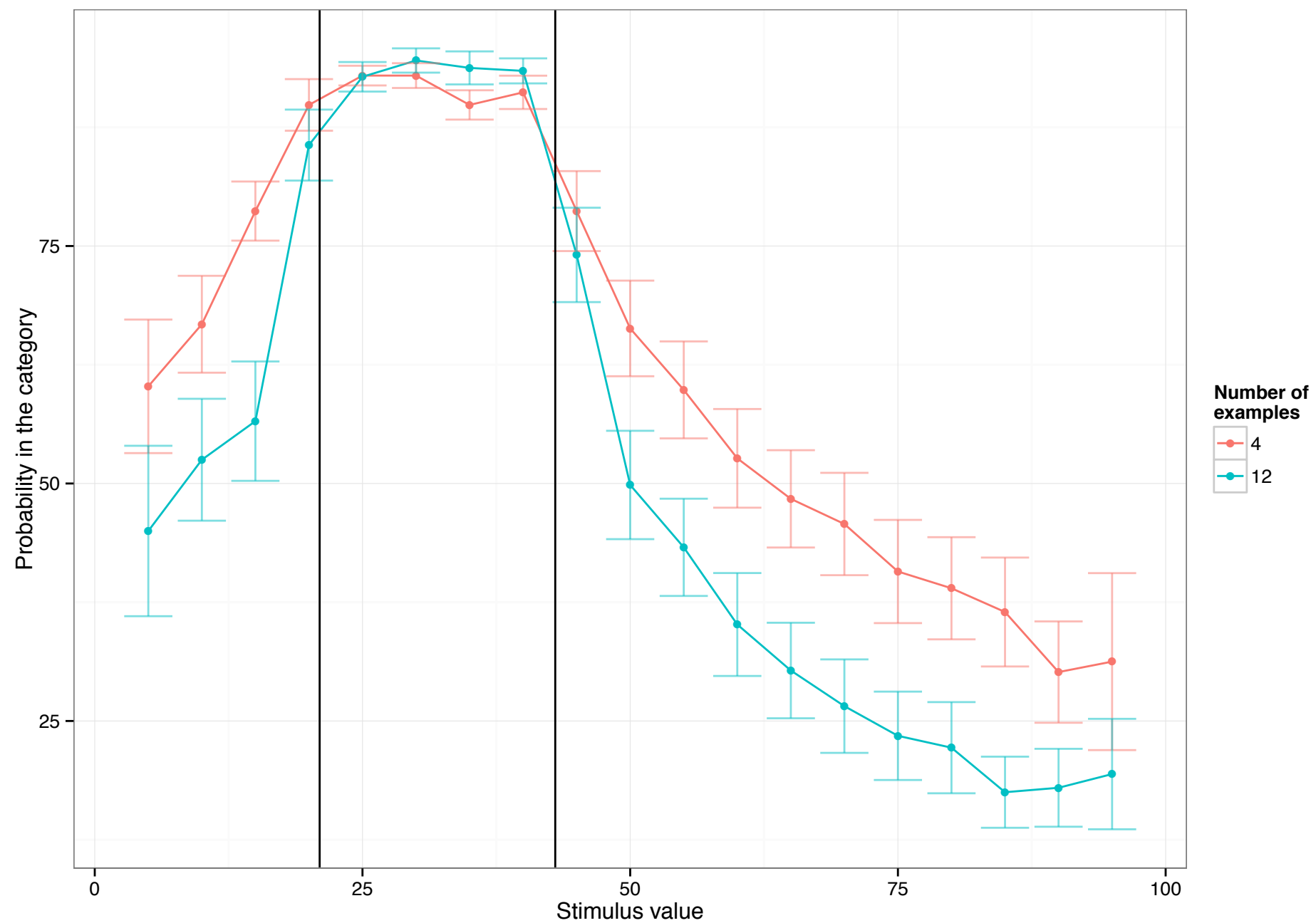
stimuli:



# Looks like strong sampling...

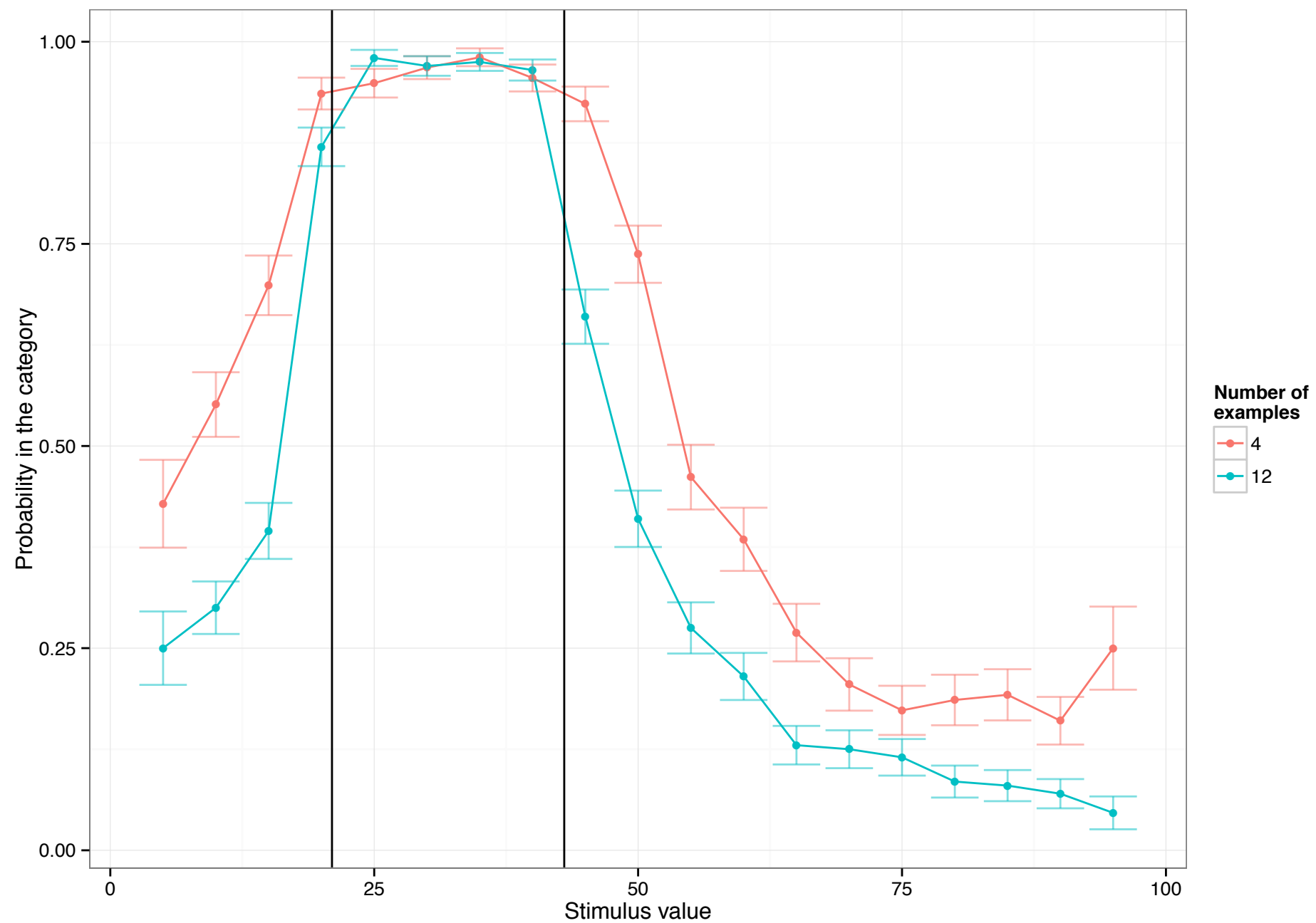


# Looks like strong sampling...



Hendrickson, et al (in prep) - probability judgments

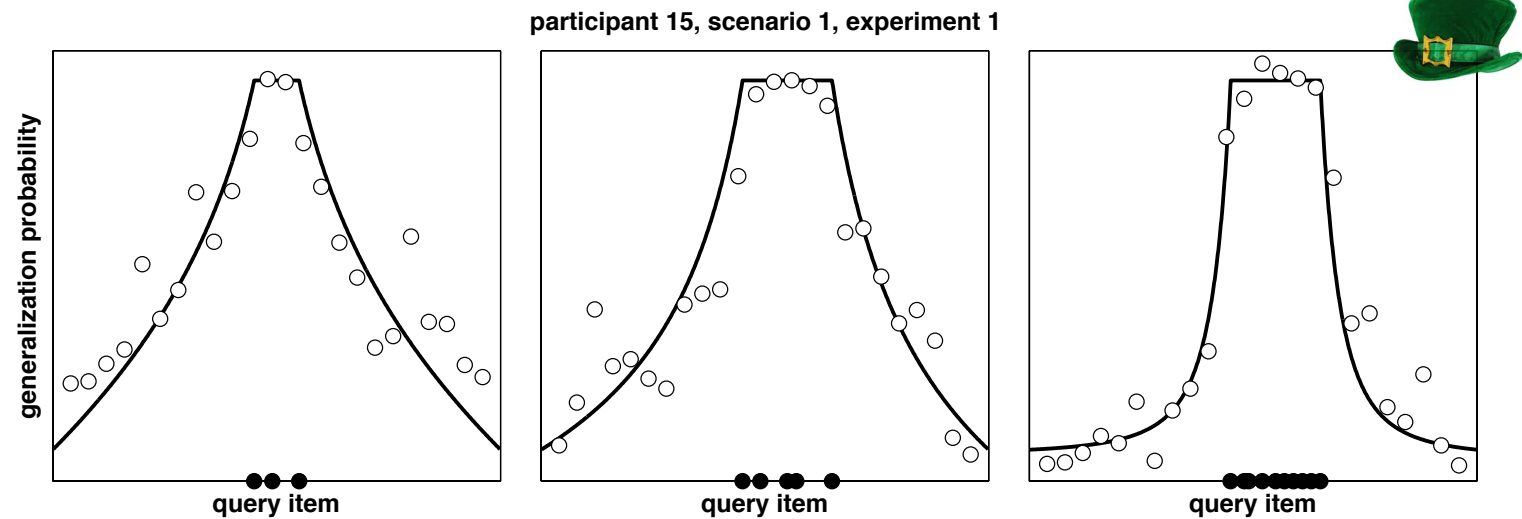
# Looks like strong sampling...



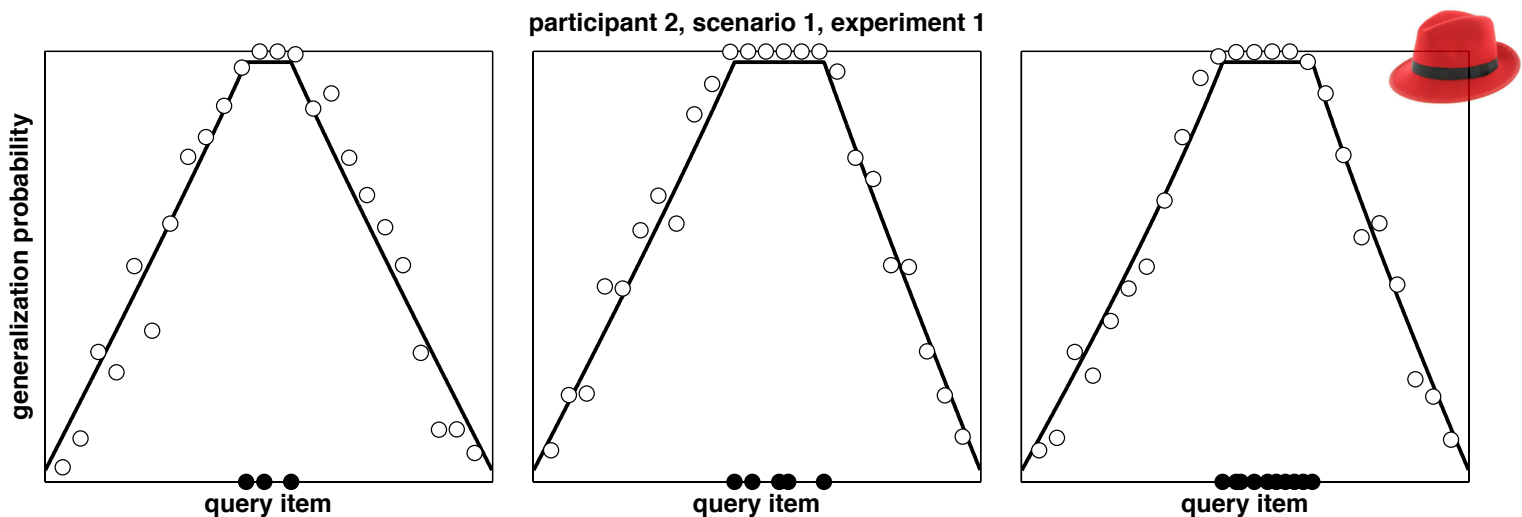
Hendrickson, et al (in prep) - categorisation data

# But there are individual differences:

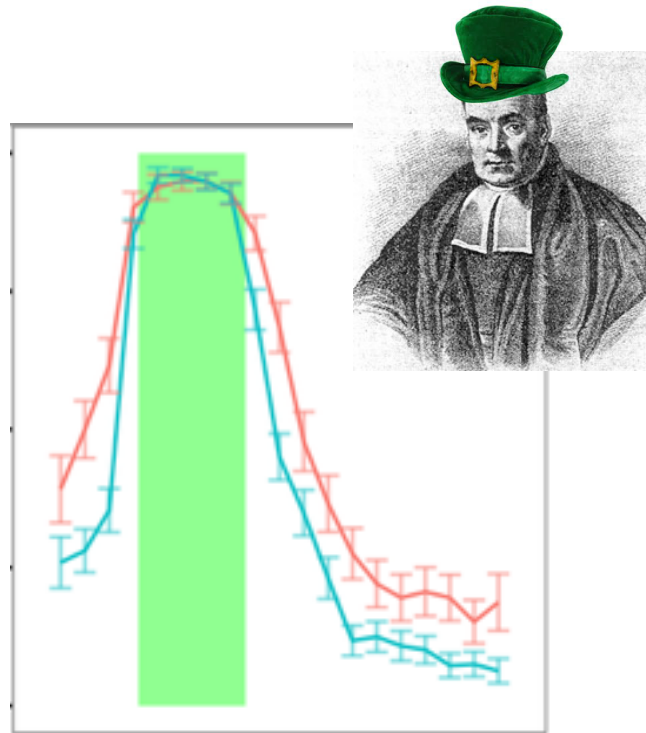
Sensitivity to sample size in simple generalisation



Insensitivity to sample size in simple generalisation

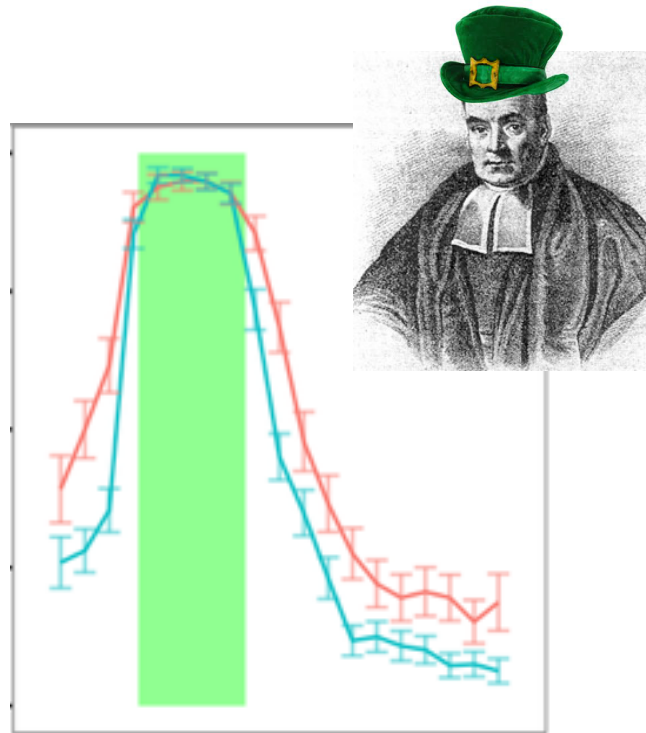


# And there are task differences:

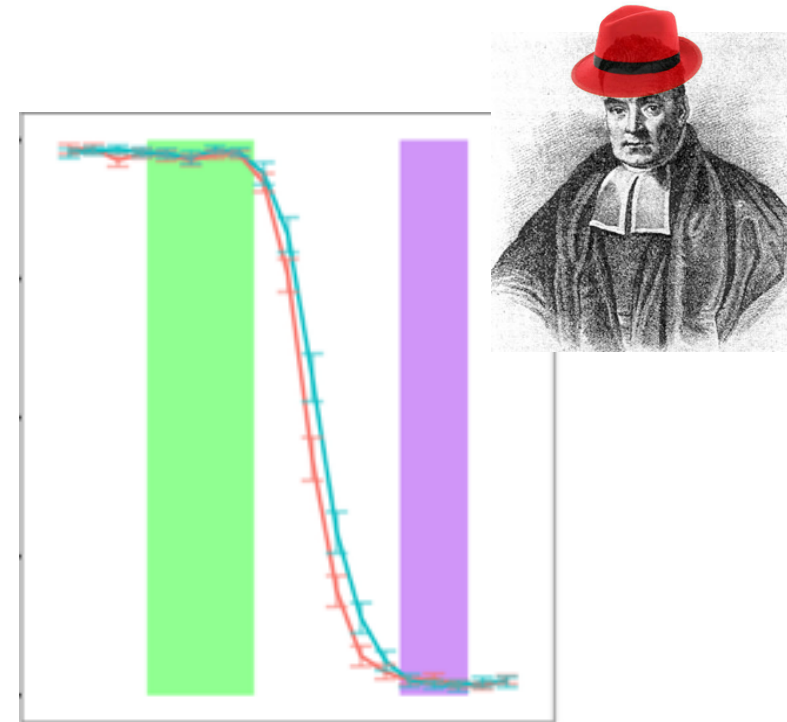


“Concept learning” designs  
where people see positive  
examples from one category  
produce the strong sampling  
“tightening” effect

# And there are task differences:



“Concept learning” designs where people see positive examples from one category produce the strong sampling “tightening” effect



“Classification” designs where people see labelled examples from two categories show no tightening, only a weak base rate effect (in the opposite direction)



- The tightening effect predicted by strong sampling does happen
- But there are differences across individuals and across tasks
- The task differences make sense if you assume people are forming theories about how the experiment(er) designed the task
- This starts to feel like social cognition...

# Relevance, social cognition and inductive reasoning



Navarro, Dry & Lee (2012). Sampling assumptions in inductive generalization. *Cognitive Science*



Hendrickson, Perfors & Navarro (in preparation). One cat, two cats: Sampling models in different category learning tasks produce qualitatively different inductive generalisations



Ransom, Perfors & Navarro (in press). Leaping to conclusions: Why premise relevance affects argument strength. *Cognitive Science*



Voorspoels, Navarro, Perfors, Ransom & Storms (under revision). How do people learn from negative evidence? Non-monotonic generalizations and sampling assumptions in inductive reasoning. *Cognitive Psychology*



Perfors, Navarro & Shafto (in preparation). Stronger evidence isn't always better: The role of social inference in evidence selection and interpretation. Previously rejected from *JEP:G*

GRIZZLY BEARS produce the hormone TH-L2.

---

Do LIONS produce the hormone TH-L2?

False

True (60% certain)

Done

GRIZZLY BEARS produce the hormone TH-L2.

---

Do LIONS produce the hormone TH-L2?

False

True (60% certain)

Done

GRIZZLY BEARS produce the hormone TH-L2.

---

+ BLACK BEARS produce the hormone TH-L2.

---

Do LIONS produce the hormone TH-L2?

False (65% certain)

True

Done

Grizzly Bears  $\rightarrow$  Lions

Grizzly Bears + Black Bears  $\rightarrow$  Lions



Adding the “Black Bears” premise  
weakens the argument?

Grizzly Bears  $\rightarrow$  Lions

Grizzly Bears + Black Bears  $\rightarrow$  Lions

Tigers  $\rightarrow$  Ferrets

Tigers + Lions  $\rightarrow$  Ferrets



Same thing with the “Lions” premise



Grizzly Bears  $\rightarrow$  Lions

Grizzly Bears + Black Bears  $\rightarrow$  Lions

Tigers  $\rightarrow$  Ferrets

Tigers + Lions  $\rightarrow$  Ferrets

Orangutans  $\rightarrow$  Gorillas

Orangutans + Chimpanzees  $\rightarrow$  Gorillas



Conversely, the “Chimpanzee” premise  
strengthens the argument here

Grizzly Bears + Black Bears

Tigers + Lions

Orangutans + Chimpanzees

In all cases the additional premise concentrates beliefs around a target category, e.g. bears, cats, primates

Is this “tightening” effect related to the tightening in the “tufa” generalisation problem?

Is this “tightening” effect related to the tightening in the “tufa” generalisation problem?

**Does it depend on the learner’s theory about how the argument was constructed?**

Is this “tightening” effect related to the tightening in the “tufa” generalisation problem?

Does it depend on the learner’s theory about how the argument was constructed?

**Can we produce qualitative shifts in people’s reasoning by manipulating their theory about how the argument was made?**

## Previous experience? (filler trials)

Cover  
story?

Relevant cover story, Relevant fillers	
Neutral cover story, Relevant fillers	Neutral cover story, Random fillers
	Random cover story, Random fillers

# Cover story manipulation



- **Relevant**: people were told that the “additional” premise was chosen by a helpful teacher
- **Neutral**: people were told nothing about how the second premise was generated



- **Random**: people were told that the second premise was selected at random from the set of true facts.

Eagles → Doves

Elephants → Deer

Kangaroos → Wombats

Three “filler” arguments



Eagles  $\rightarrow$  Doves

Elephants  $\rightarrow$  Deer

Kangaroos  $\rightarrow$  Wombats

Eagles + Hawks  $\rightarrow$  Doves

Elephants + Cows  $\rightarrow$  Deer

Kangaroos + Koalas  $\rightarrow$  Wombats

... with a **relevant**  
second premise

(positive premises from  
the same category suggest  
strong sampling)

Eagles → Doves

Elephants → Deer

Kangaroos → Wombats

Eagles + Hawks → Doves

Elephants + Cows → Deer

Kangaroos + Koalas → Wombats

Eagles - Tortoises → Doves

Elephants + Anteaters → Deer

Kangaroos - Flamingos → Wombats

... or a **random** one

(negated premises  
unrelated to the topic  
suggest weak sampling)


Stimulus ordering was fixed and designed to ensure that fillers (mostly) preceded targets:

First generalisation	Additional example	
	HELPFUL	RANDOM
EAGLES → DOVES	+HAWKS	−TORTOISES
ELEPHANTS → DEERS	+COWS	+ANTEATERS
<b>TIGERS → FERRETS</b>	+LIONS	+LIONS
KANGAROOS → WOMBATS	+KOALAS	−FLAMINGOS
<b>GRIZZLY BEARS → LIONS</b>	+BLACK BEARS	+BLACK BEARS
ORANGUTANS → GORILLAS	+CHIMPANZEES	+CHIMPANZEES

Participants were 296 people recruited through MTurk



**Condition**

 Both Relevant	 Relevant Fillers
 Random Fillers	 Both Random

orangutans  
chimpanzees  

---

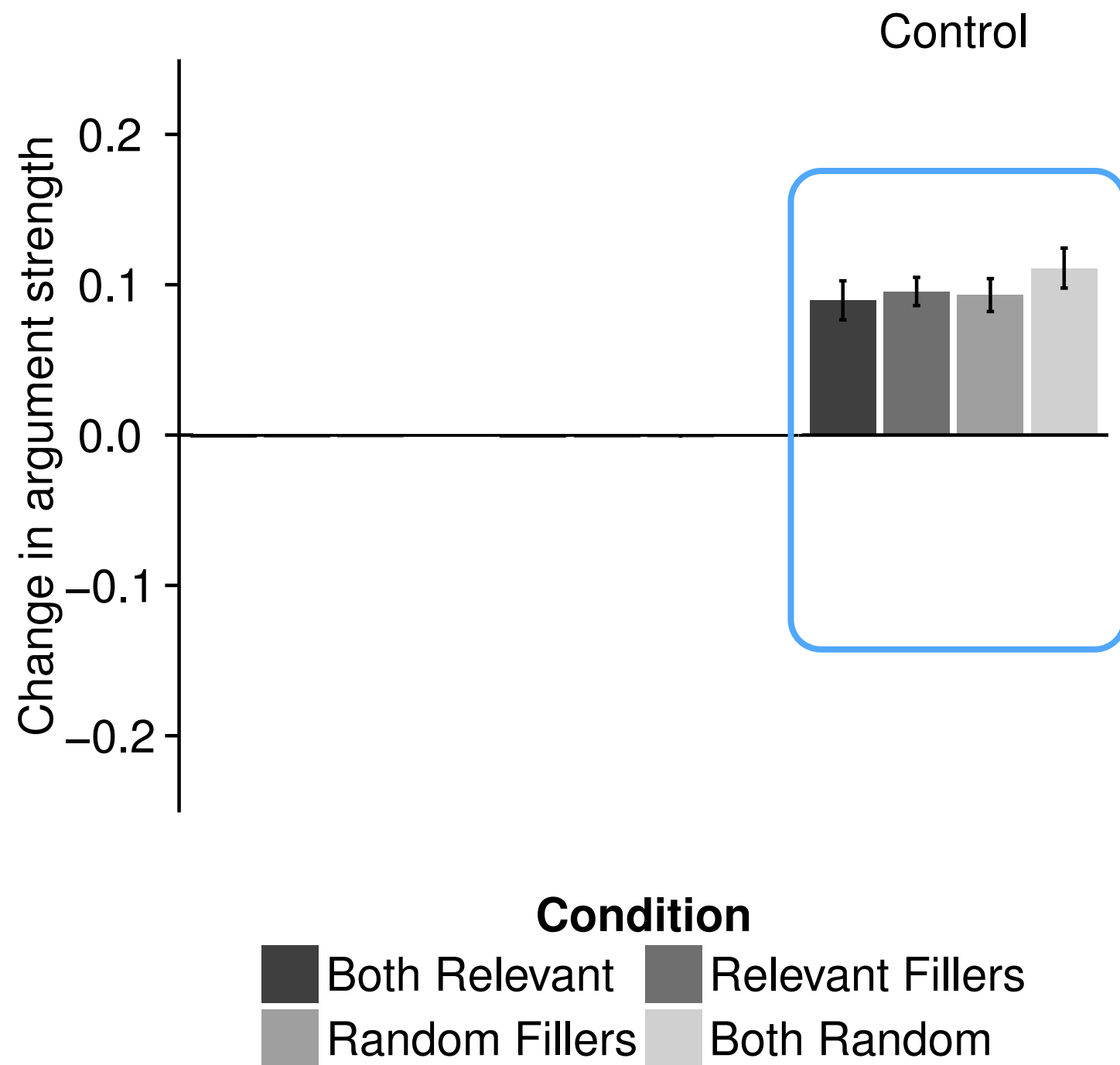
gorillas



orangutans  

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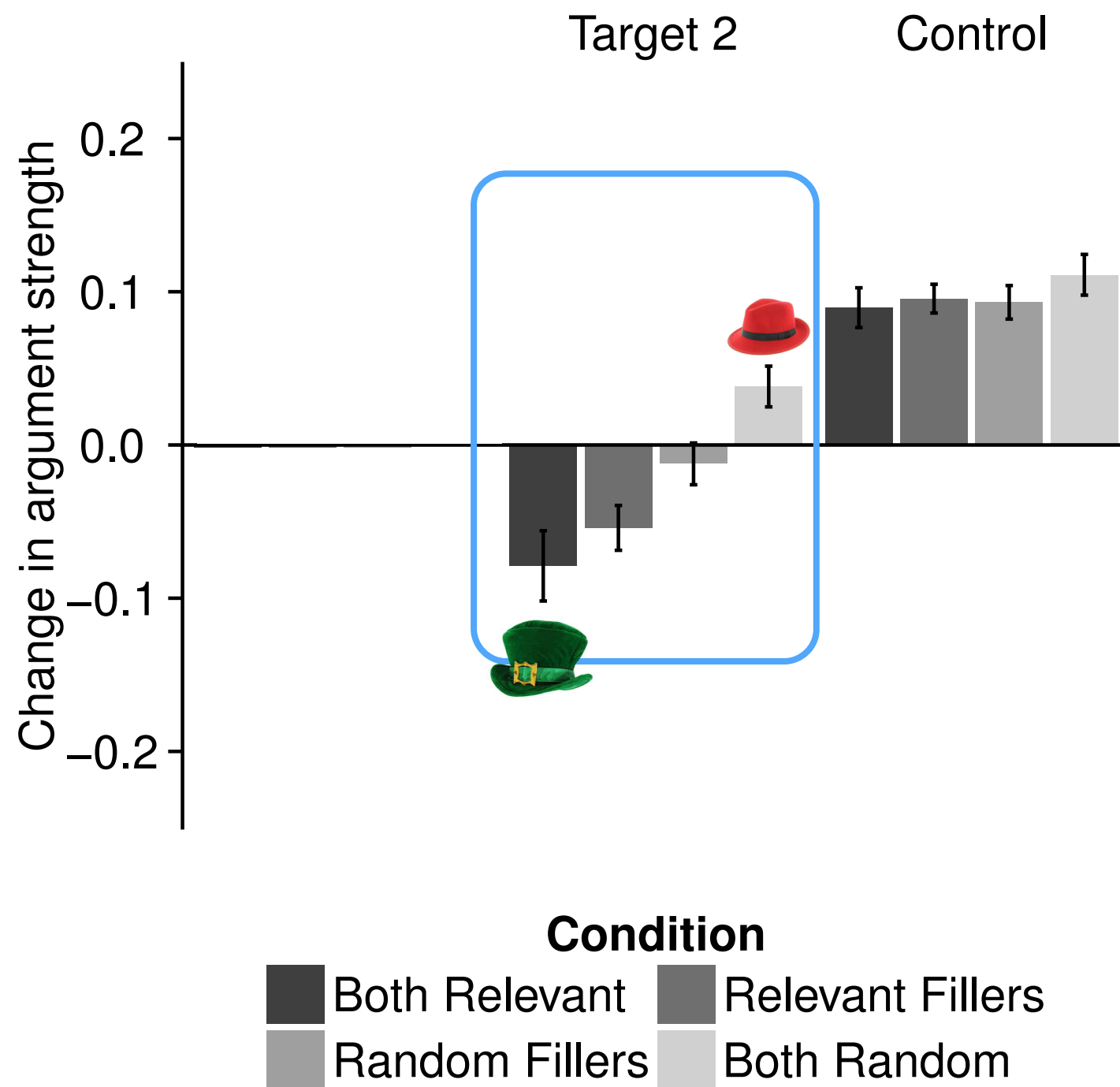
gorillas



orangutans  
chimpanzees  
gorillas

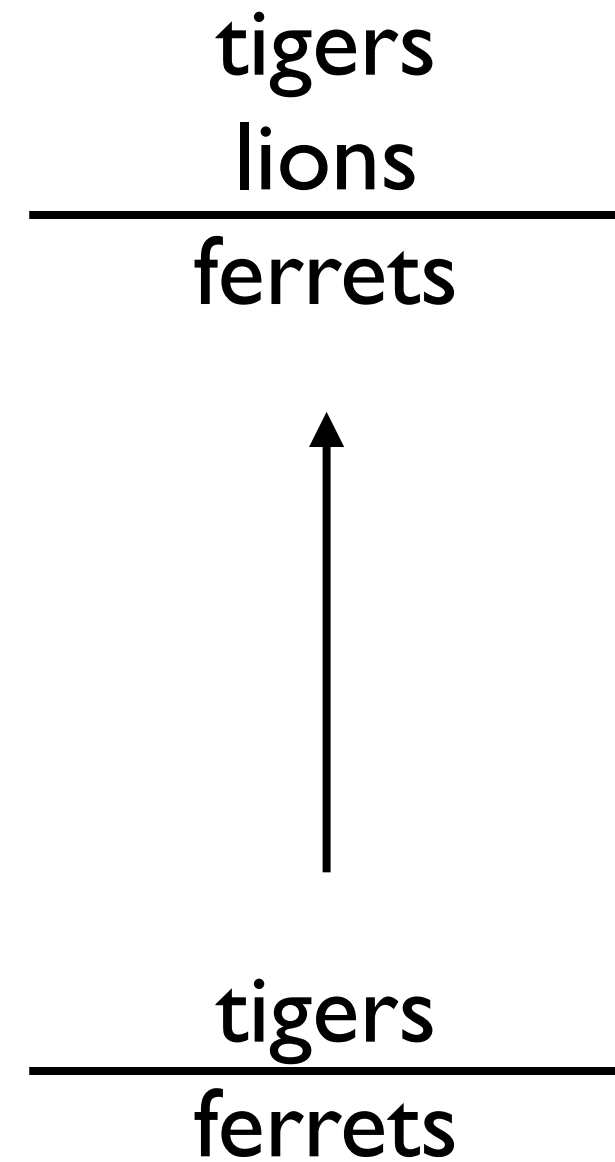
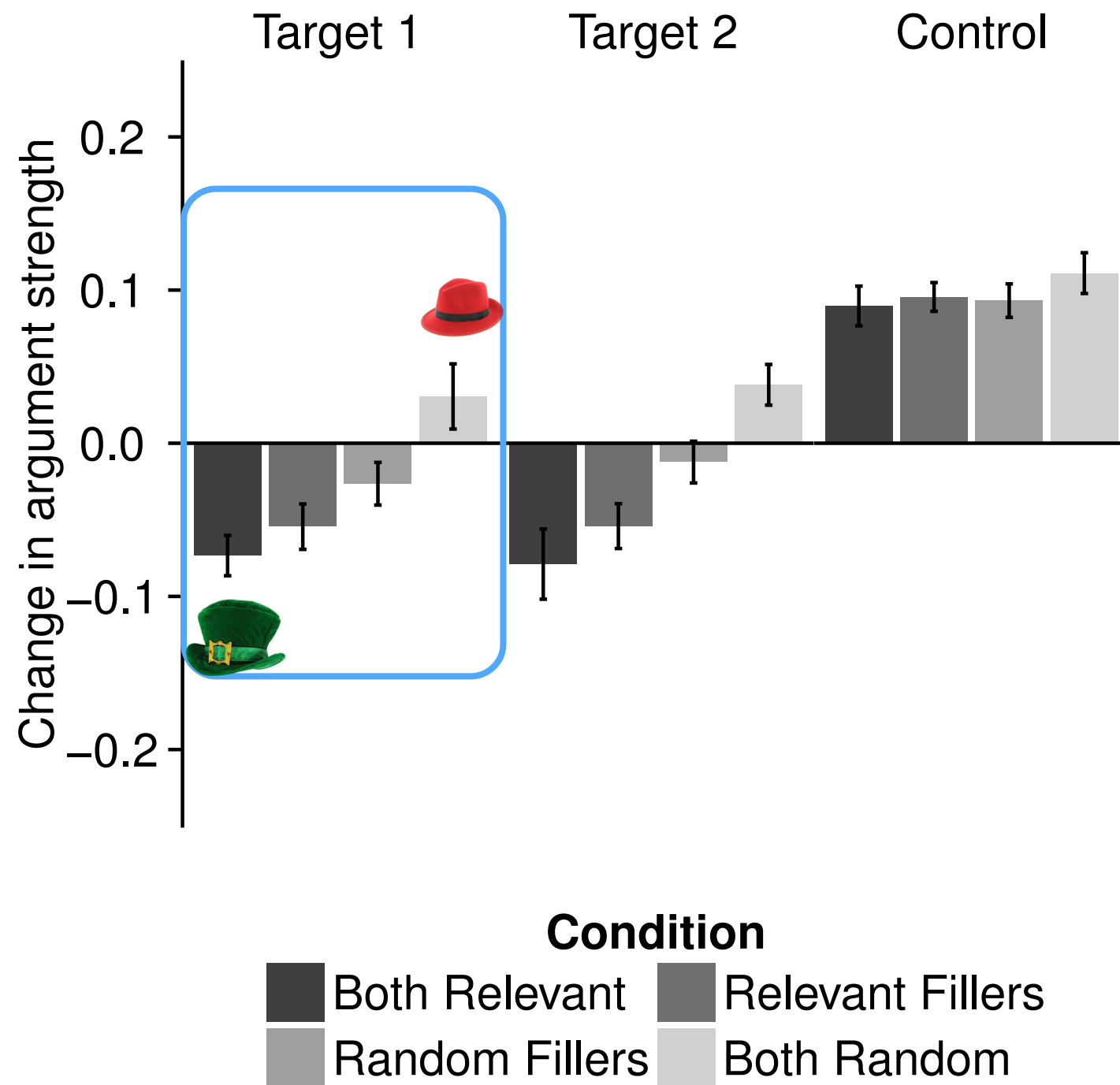


orangutans  
gorillas



grizzly bears  
black bears  
lions

grizzly bears  
lions



# (Bayesian) data analysis: hypothesis tests for order restricted models

Model	Order restrictions
NO EFFECT	$\mu_1 = \mu_2 = \mu_3 = \mu_4$
FILLERS ONLY	$\mu_1 = \mu_2 < \mu_3 = \mu_4$
STORY ONLY	$\mu_1 < \mu_2 = \mu_3 < \mu_4$
BOTH	$\mu_1 < \mu_2 < \mu_3 < \mu_4$
RANDOM EFFECT	$\mu_1 \neq \mu_2 \neq \mu_3 \neq \mu_4$



# Clear effect of cover story on targets, possibly also an effect of filler type

Model	Order restrictions	Bayes Factor ( : NO EFFECT)	
		Target 1	Target 2
NO EFFECT	$\mu_1 = \mu_2 = \mu_3 = \mu_4$	-	-
FILLERS ONLY	$\mu_1 = \mu_2 < \mu_3 = \mu_4$	740:1	12,000:1
STORY ONLY	$\mu_1 < \mu_2 = \mu_3 < \mu_4$	4,100:1	17,000:1
BOTH	$\mu_1 < \mu_2 < \mu_3 < \mu_4$	2,900:1	30,000:1
RANDOM EFFECT	$\mu_1 \neq \mu_2 \neq \mu_3 \neq \mu_4$	520:1	4,600:1

# Null effect for the control item

Model	Order restrictions	Bayes Factor ( : NO EFFECT)
		Control
NO EFFECT	$\mu_1 = \mu_2 = \mu_3 = \mu_4$	-
FILLERS ONLY	$\mu_1 = \mu_2 < \mu_3 = \mu_4$	$< 1 : 1$
STORY ONLY	$\mu_1 < \mu_2 = \mu_3 < \mu_4$	$< 1 : 1$
BOTH	$\mu_1 < \mu_2 < \mu_3 < \mu_4$	$< 1 : 1$
RANDOM EFFECT	$\mu_1 \neq \mu_2 \neq \mu_3 \neq \mu_4$	$< 1 : 1$

Should we model this as a difference  
between two Bayesian learners?



A weakly sampling  
falsificationist



A strongly sampling  
Ockhamist

Or posit a continuum of Bayesians?



$\theta=0$

$\theta=.33$

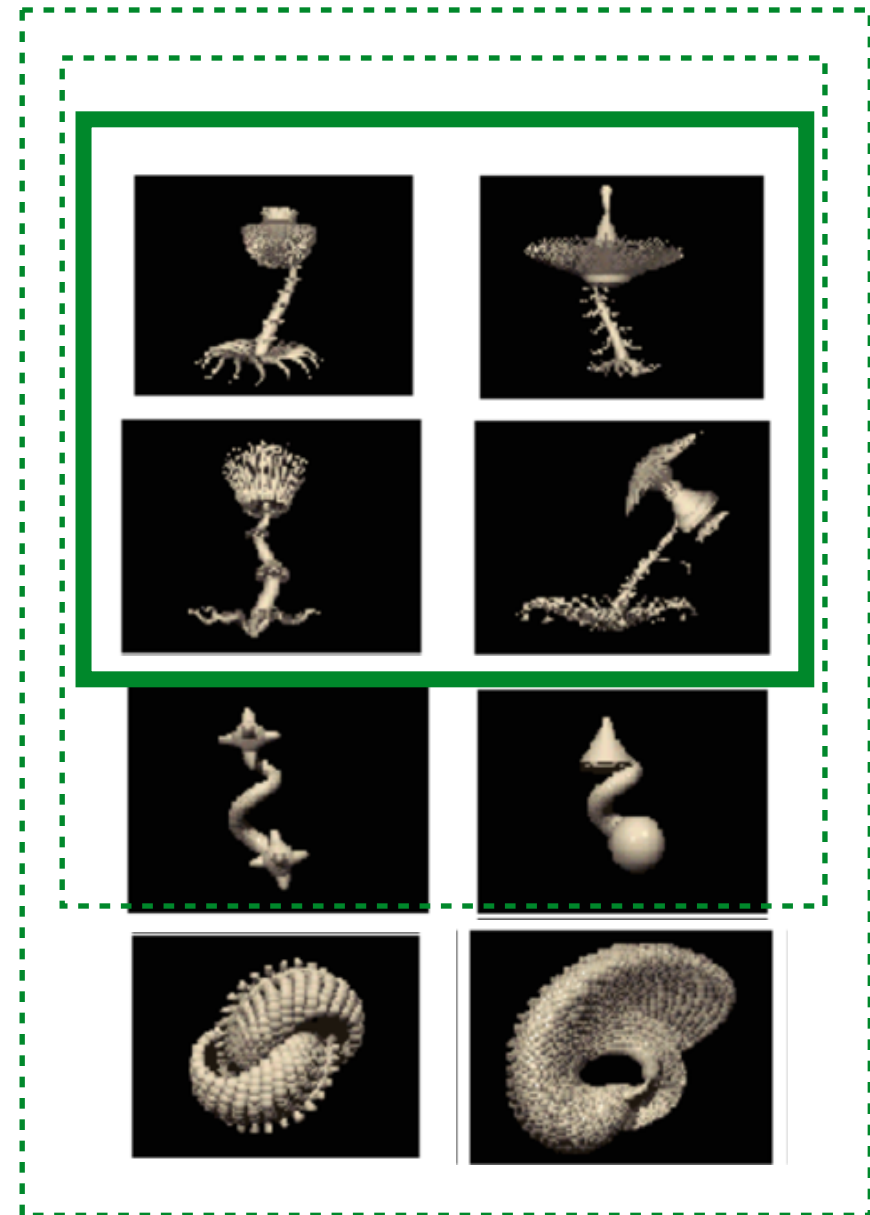
$\theta=.67$

$\theta=1$

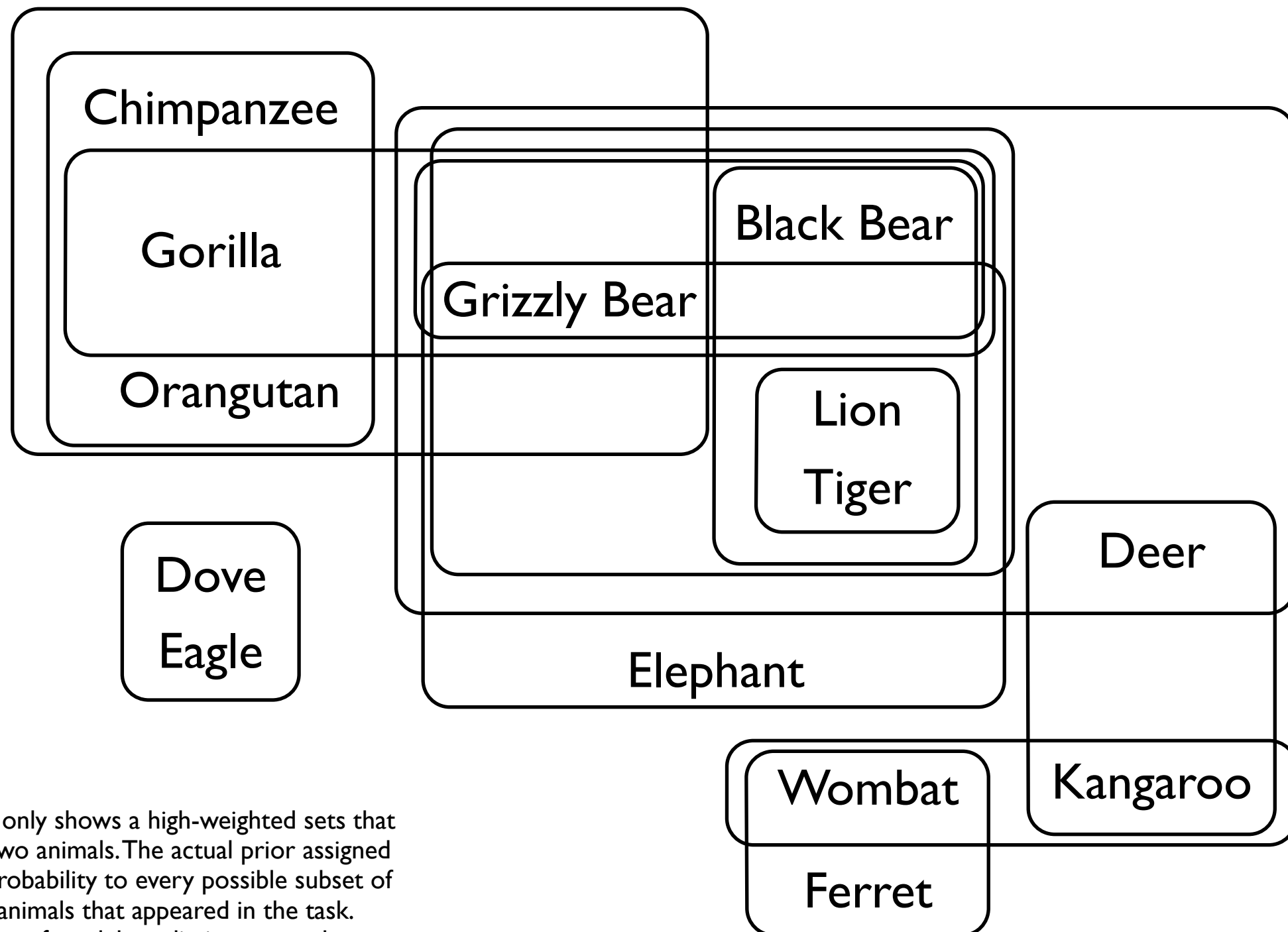
“weak”

“strong”

And what shall our Bayesians use for their hypothesis space and priors?

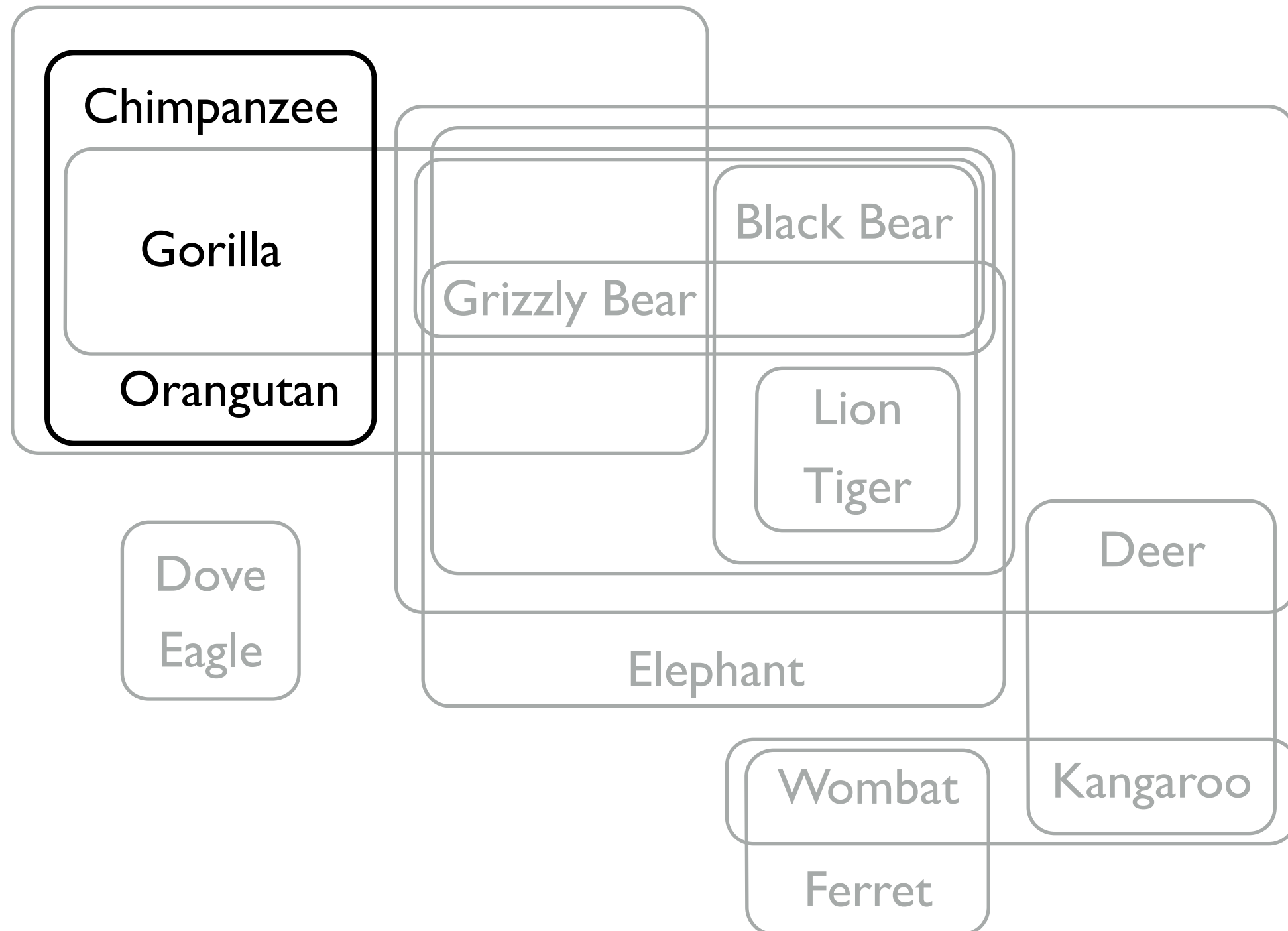


Assume any subset of items is a legitimate hypothesis,  
with weights inferred from similarity judgments

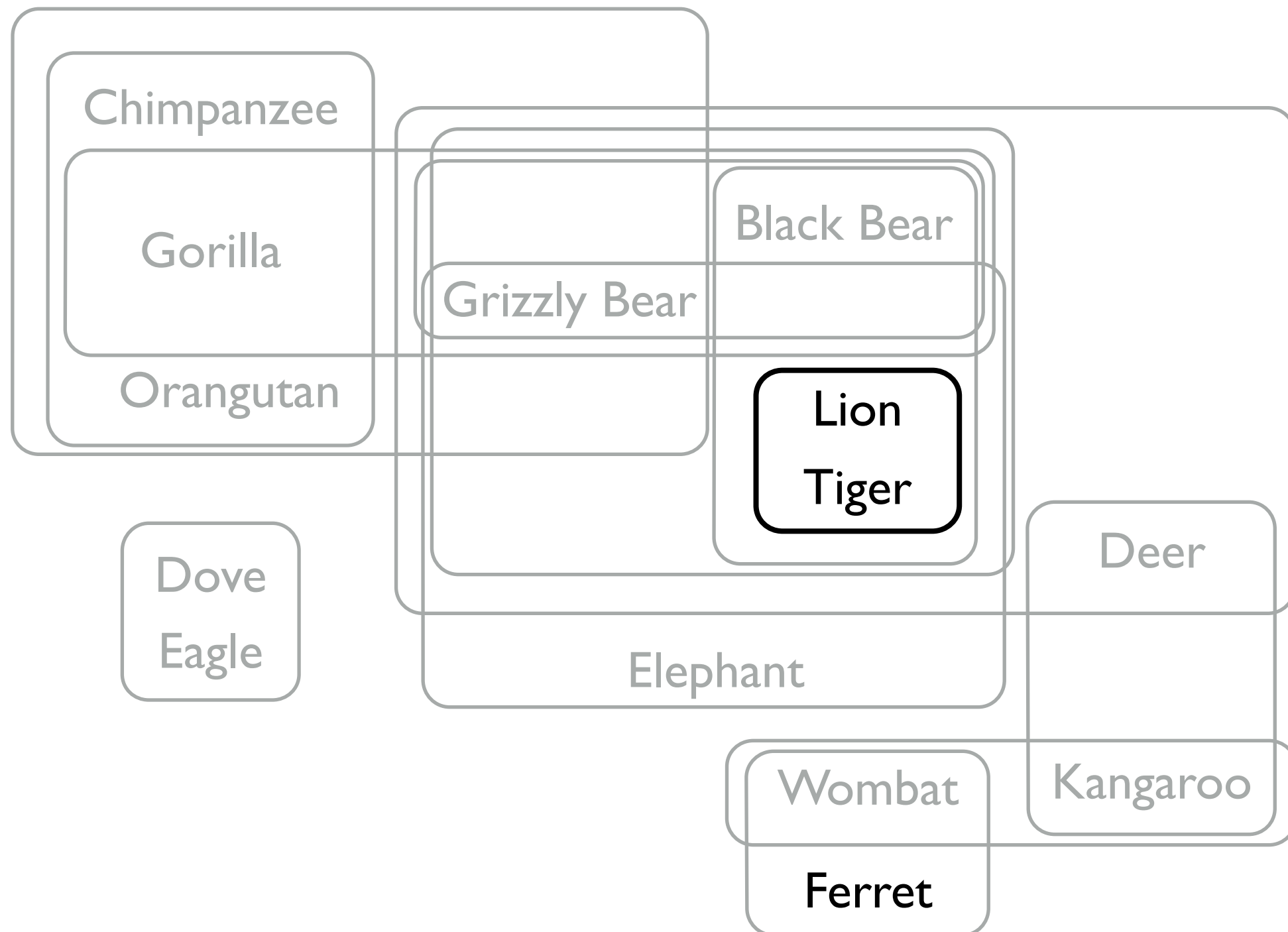


\* This illustration only shows a high-weighted sets that contain at least two animals. The actual prior assigned non-zero prior probability to every possible subset of the set of all animals that appeared in the task. Qualitative features of model predictions are robust to the specific choice of prior: anything even semi-reasonable seems to work

# (Chimpanzee, Gorilla, Orangutan)

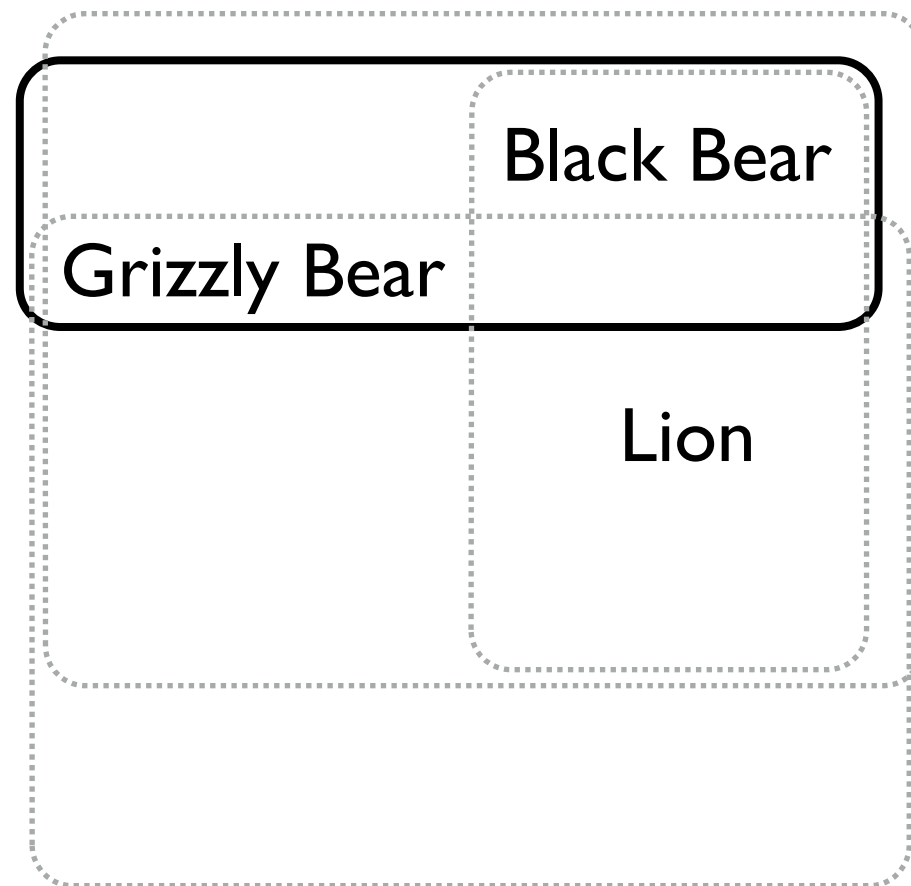


(Lions, Tigers) but not Ferrets



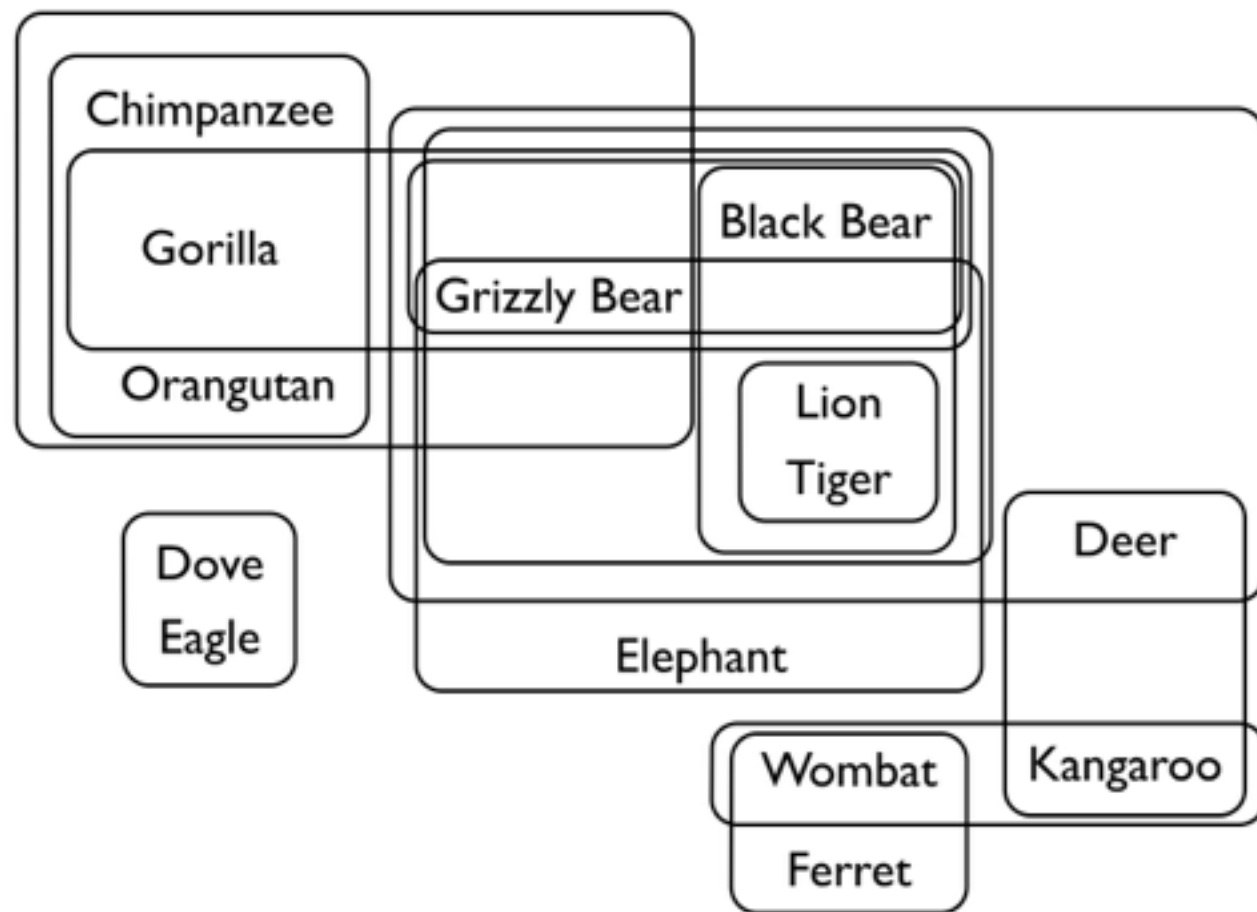


# (Grizzly Bears, Black Bears) but not Lions?



There are many high weighted features involving these three, but overall the prior puts the bears together more often

The prior explains why there are structural differences between the targets and the control

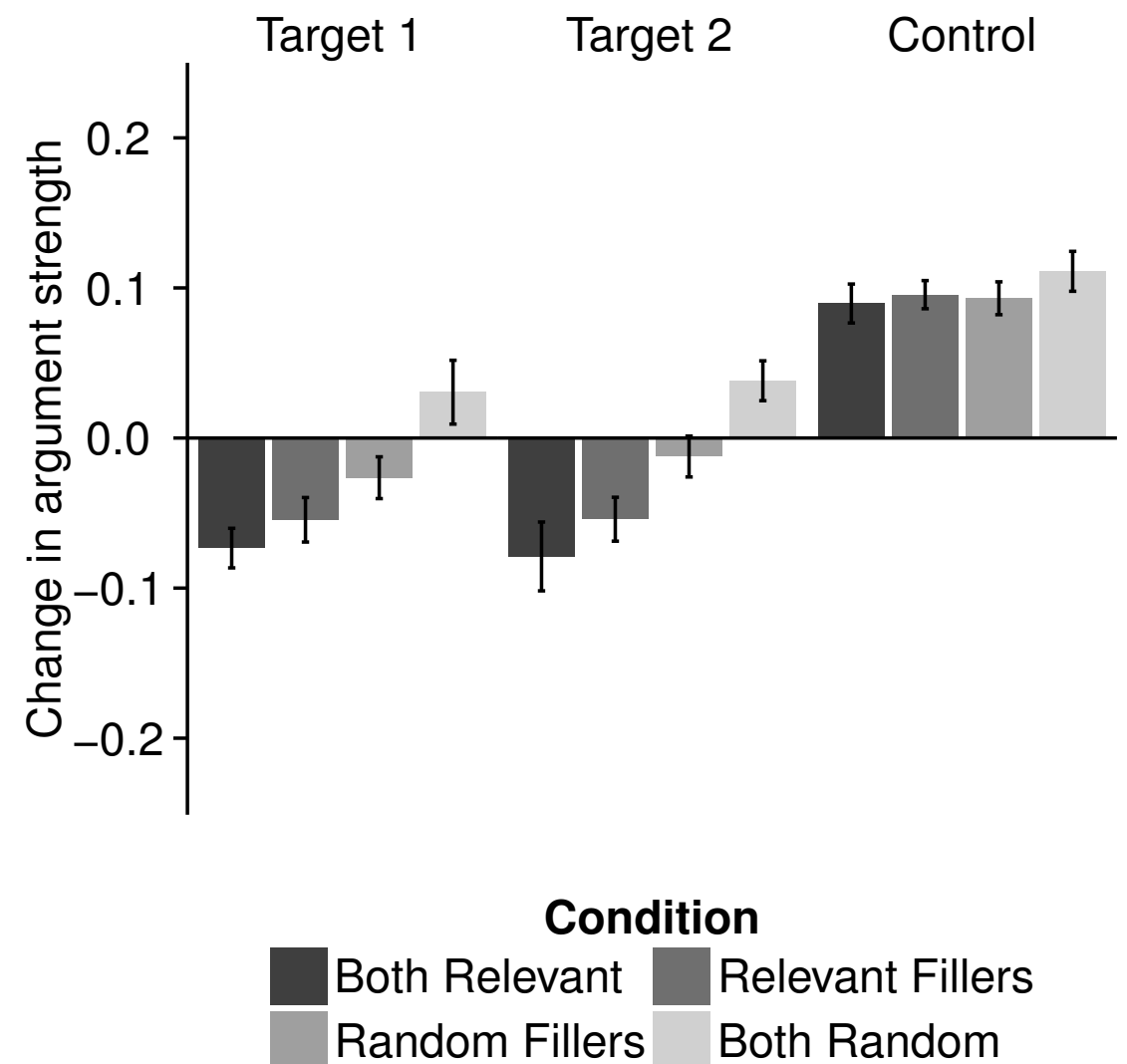


The likelihood describes how “adding more premises” can have different effects across conditions

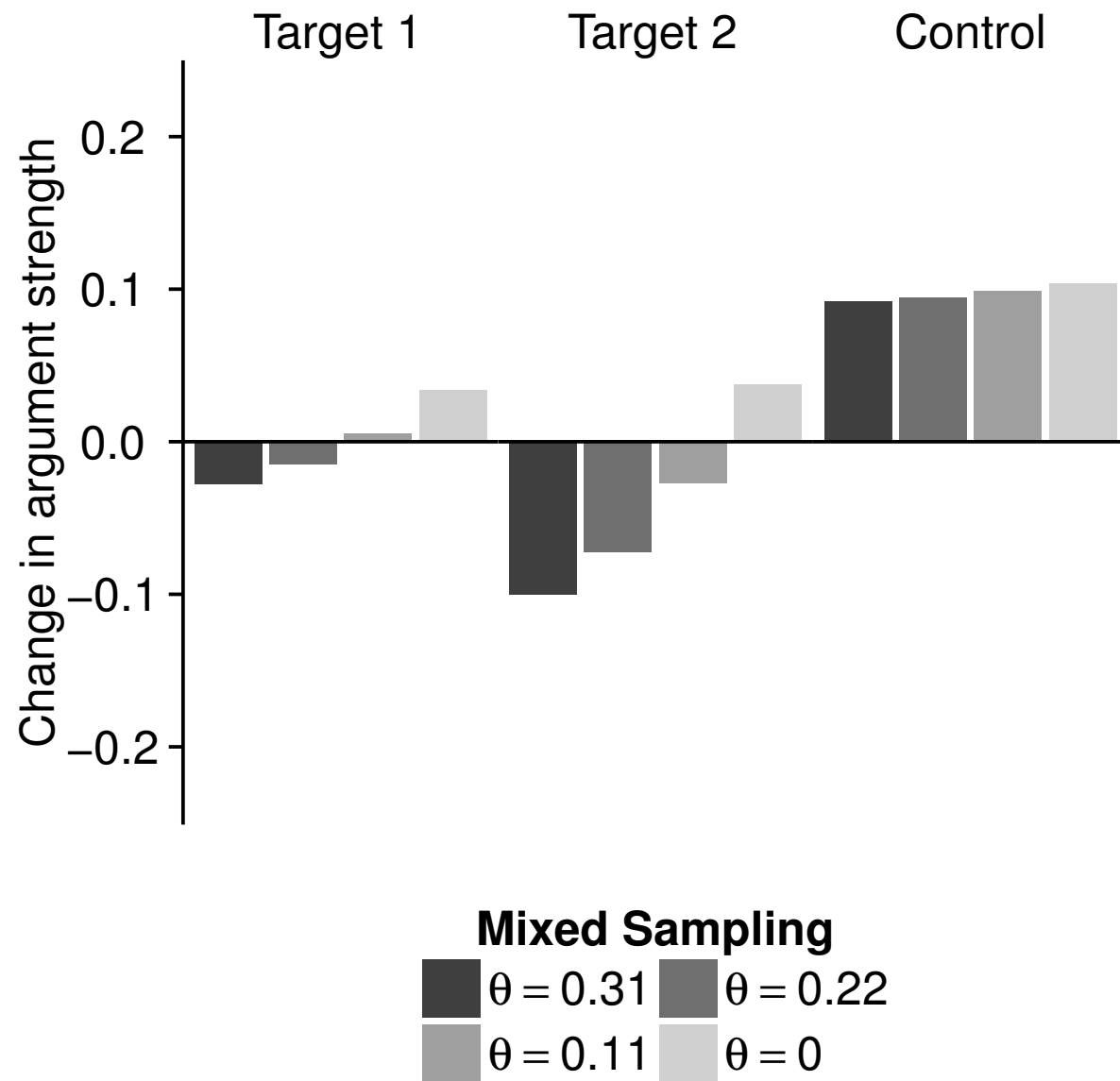


Does the model  
work???

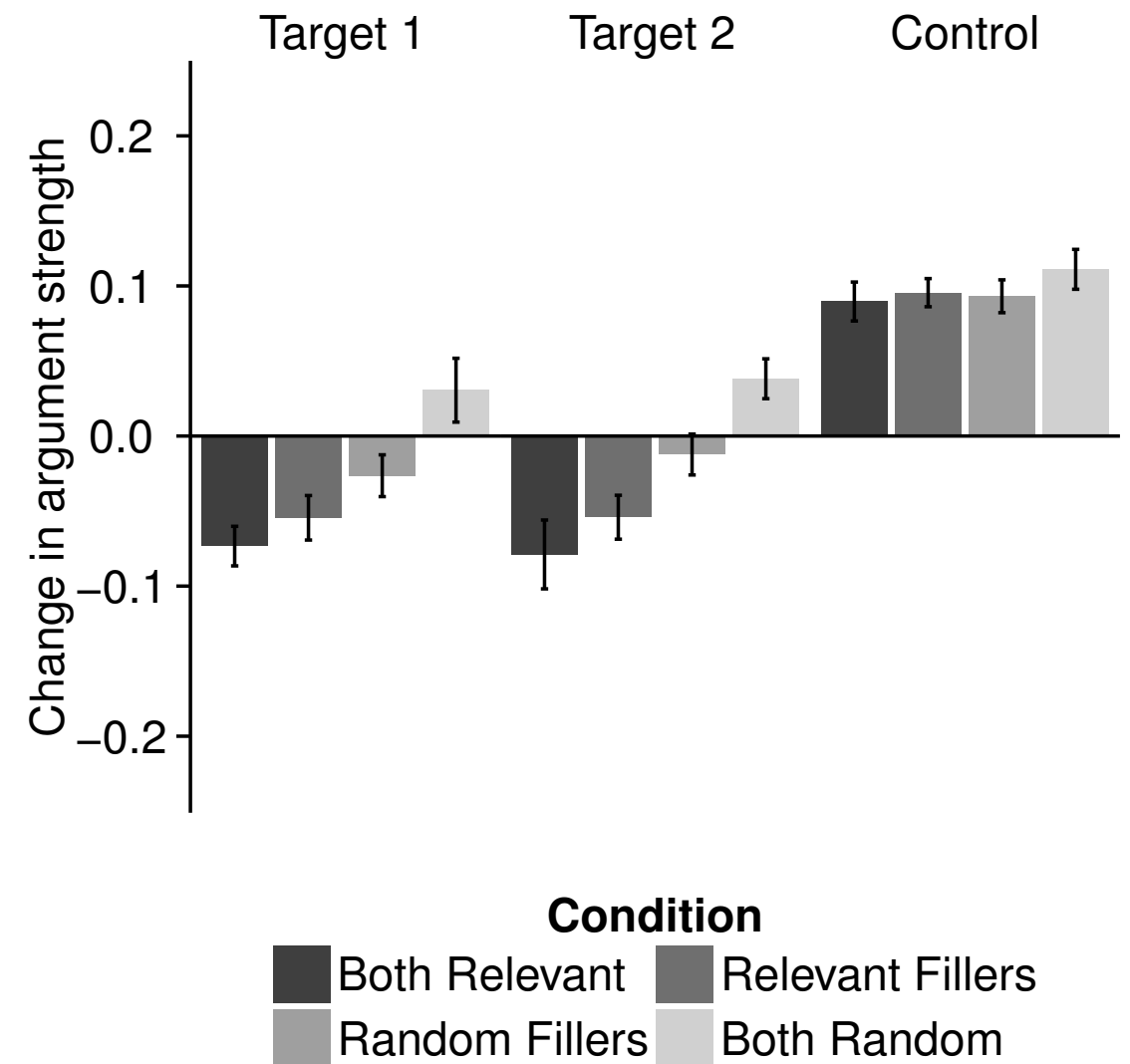
## Empirical data



# Model fits



# Empirical data



- It's not just about the evidence facts provide for a conclusion, it's also about how you think those facts were put together
- Bayesian models explain the reversal as a shift in the sampling assumption
- This is encouraging, so...

How to take a helpful hint...  
(the curious power of negative evidence)



Navarro, Dry & Lee (2012). Sampling assumptions in inductive generalization. *Cognitive Science*



Hendrickson, Perfors & Navarro (in preparation). One cat, two cats: Sampling models in different category learning tasks produce qualitatively different inductive generalisations



Ransom, Perfors & Navarro (in press). Leaping to conclusions: Why premise relevance affects argument strength. *Cognitive Science*



Voorspoels, Navarro, Perfors, Ransom & Storms (under revision). How do people learn from negative evidence? Non-monotonic generalizations and sampling assumptions in inductive reasoning. *Cognitive Psychology*



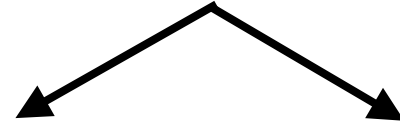
Perfors, Navarro & Shafto (in preparation). Stronger evidence isn't always better: The role of social inference in evidence selection and interpretation. Previously rejected from *JEP:G*

You want to infer whether all ravens are black.  
Which of these observations is more helpful?





Law of contraposition makes these  
two statements logically equivalent



Raven  $\rightarrow$  Black

$\neg$ Black  $\rightarrow$   $\neg$ Raven



Okaaaay.... apparently these are the same?

Raven  $\rightarrow$  Black

$\neg$ Black  $\rightarrow$   $\neg$ Raven



(raven, black)



( $\neg$ black,  $\neg$ raven)

Raven

¬Raven

Black



¬Black

???



Raven

¬Raven

Black



¬Black

???



# Category size/frequency matters, theoretically & empirically

- Positive (labelled) categories are small
  - Oaksford & Chater (1998), Navarro & Perfors (2011), etc.
- Sampling from a small category is more powerful
  - Good (1960), Klayman & Ha (1987), Oaksford & Chater (1998), Navarro & Perfors (2011), Austerweil & Griffiths (2011), etc
- People treat positive evidence as more informative than negative evidence
  - Wason (1960, 1968), many many others...
  - So it all makes sense! And...

# Paradox resolved!

A black raven is very  
informative



A non-black non-raven has  
non-zero but negligible  
evidentiary value



So we'll just some empirical work, with some obviously predictable results...

Mozart produces  
alpha waves



The sound of a falling  
rock does not





music

$\neg$ music

alpha



$\neg$ alpha

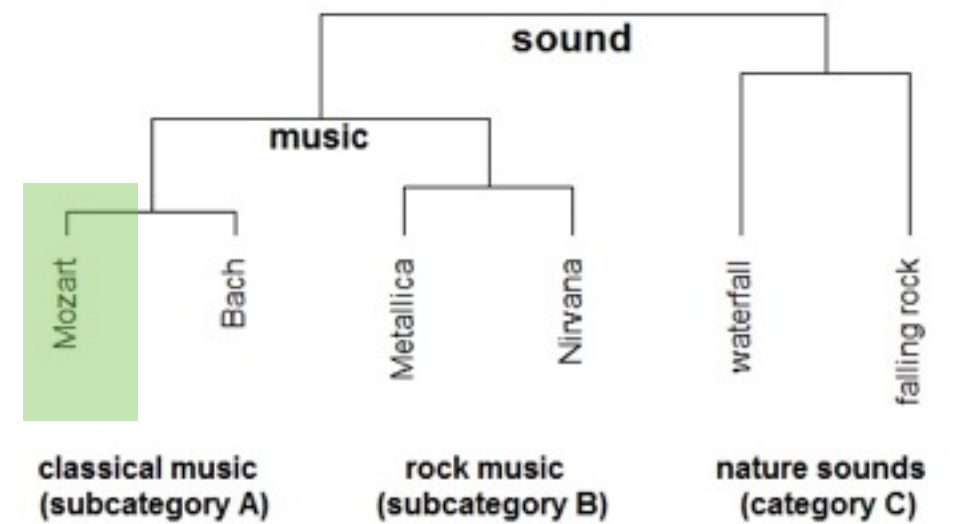
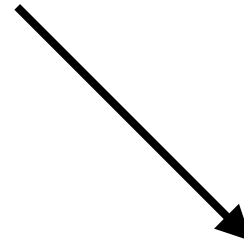
???



This ought to be about as  
utterly useless as the green  
shoes thing

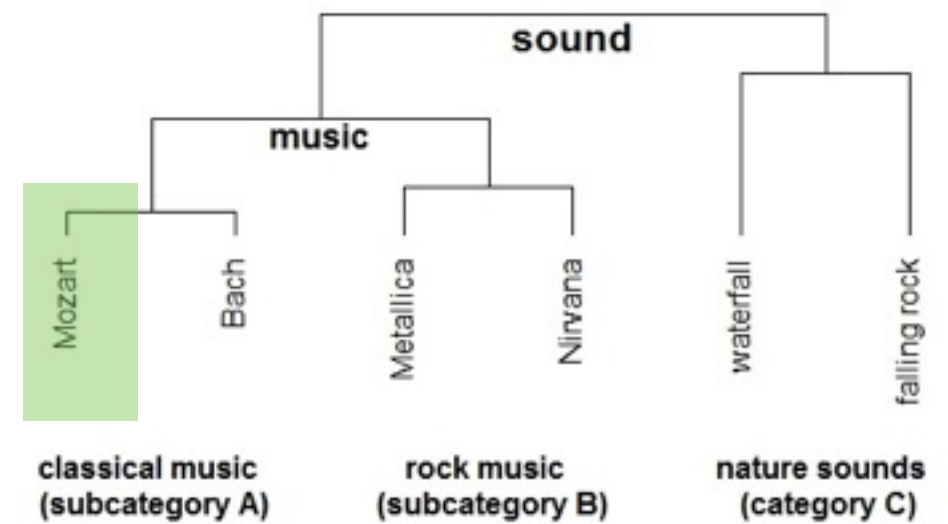
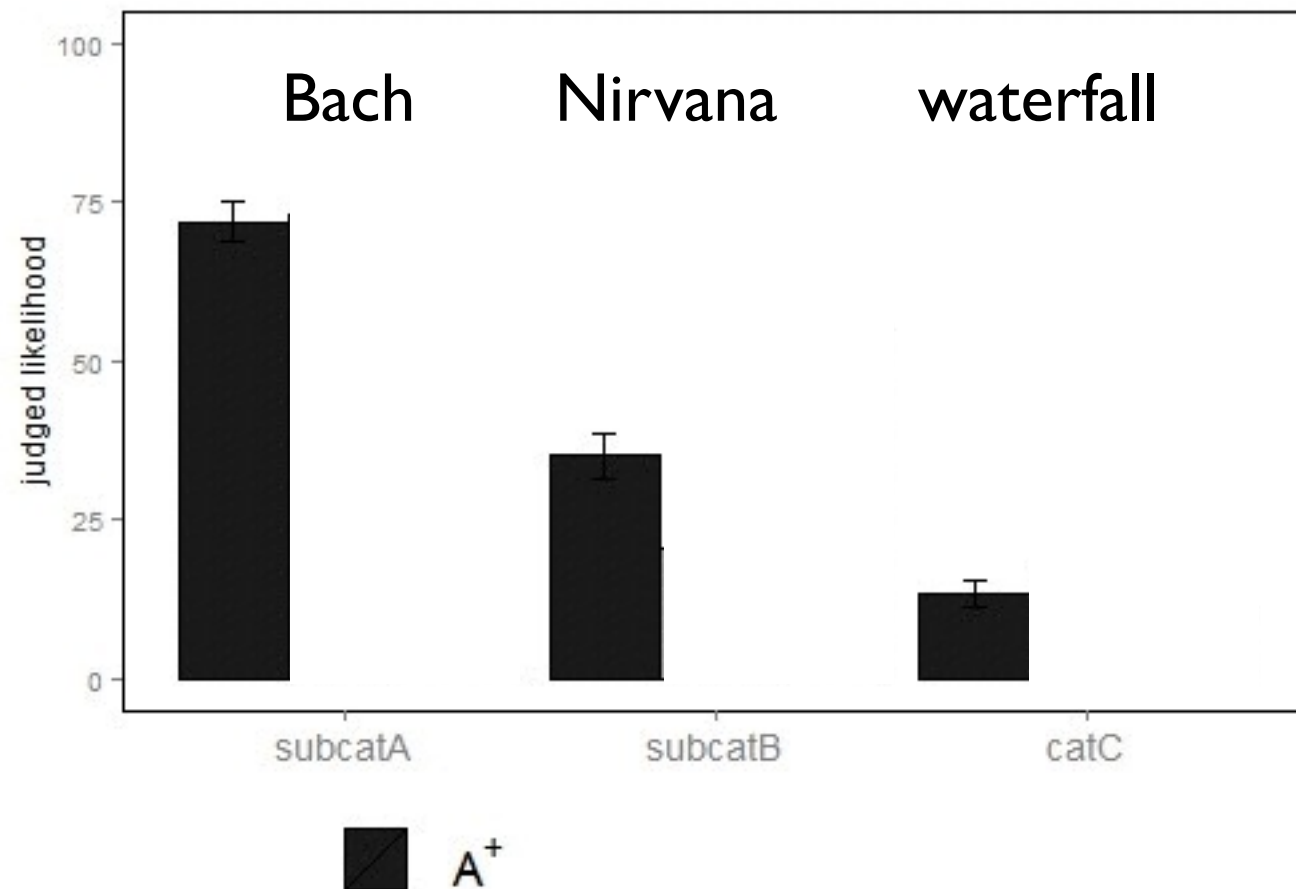
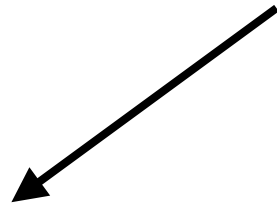


Okay, we start by telling people that Mozart does produce alpha waves...



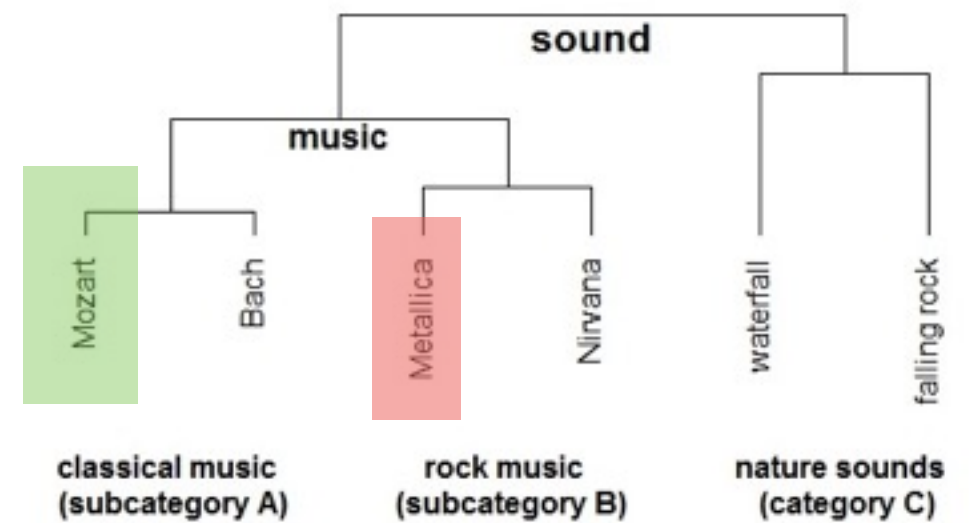
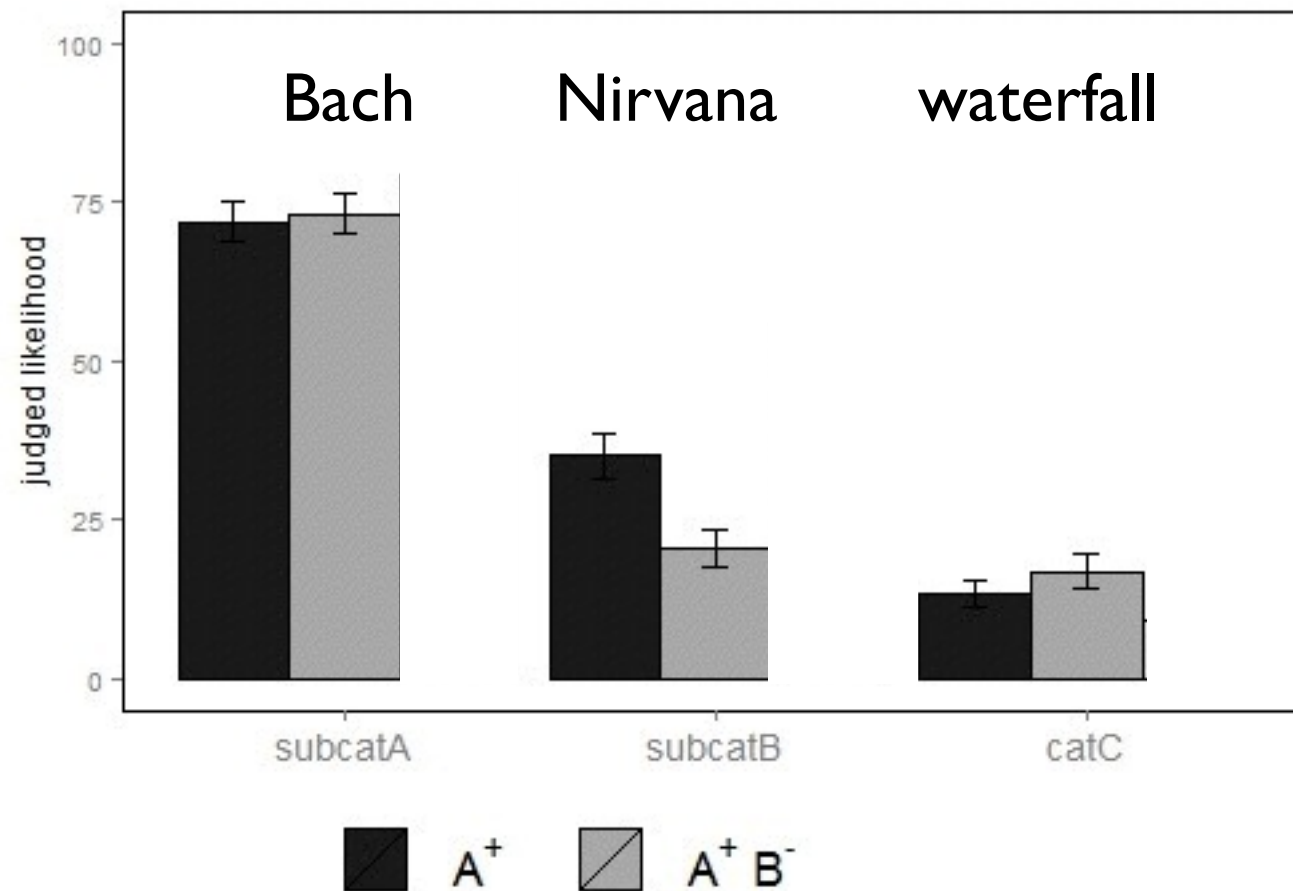
Mozart+

... and they generalise in a way that seems terribly sensible



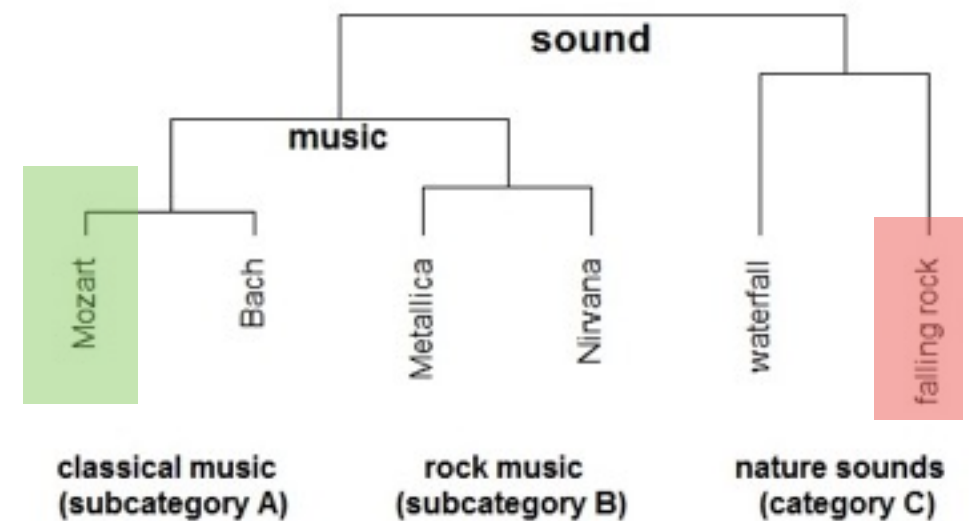
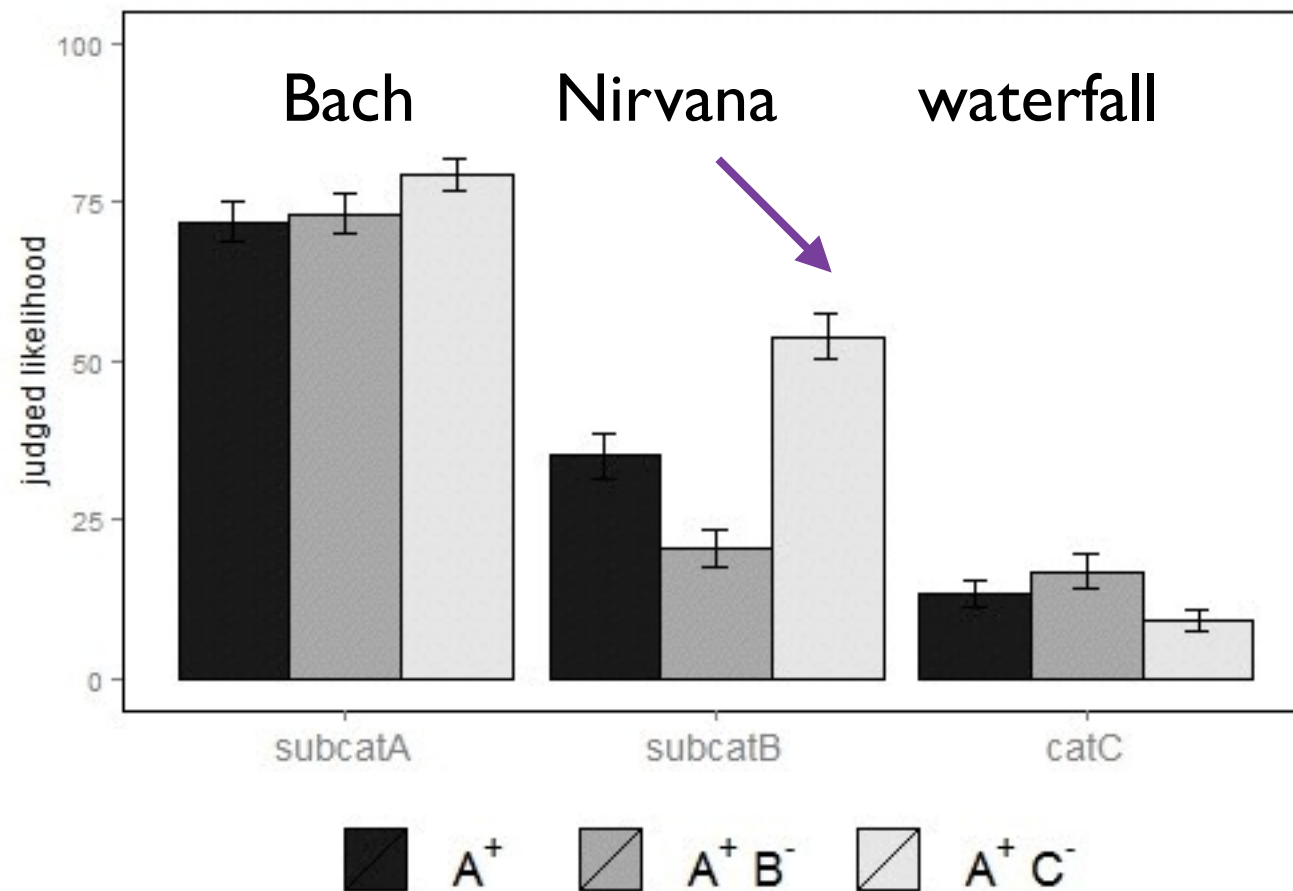
Mozart+

# Adding Metallica as a negative example has a small effect (yay!)



Mozart+ Metallica-

# OKAY WTF HUMANS I HATE YOU ALL.



Mozart+ Falling Rock-



classical music

all music

all sound

three relevant hypotheses for the  
extension of the alpha waves property



positive example of classical  
music means people strongly  
endorse the narrow category

classical music

+

all music

all sound

-



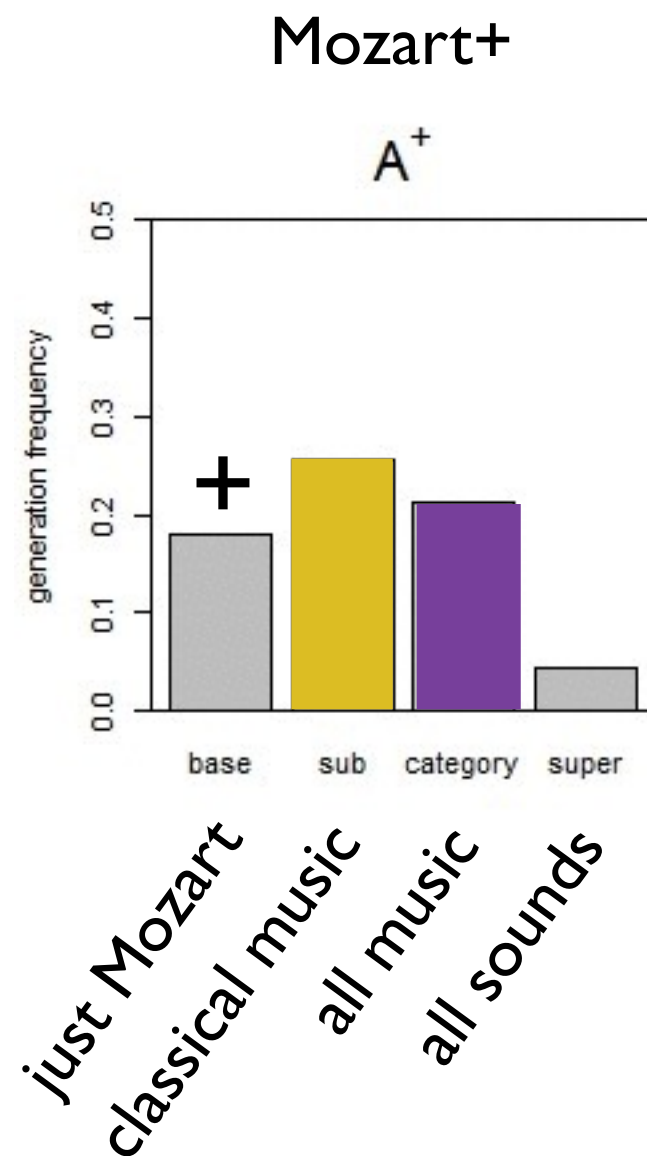
but add a negative observation  
from a distant category and you  
get a huge belief revision?



Apparently people make a  
(pragmatic?) inference that the  
negative observation is used to  
demarcate the category boundary



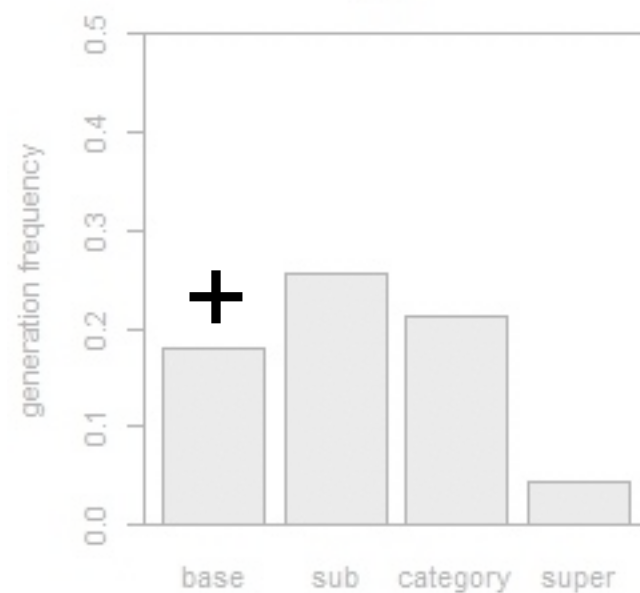
Well, let's ask them what they think the true extension of the property is...



Well, let's ask them what they think the true extension of the property is...

Mozart+

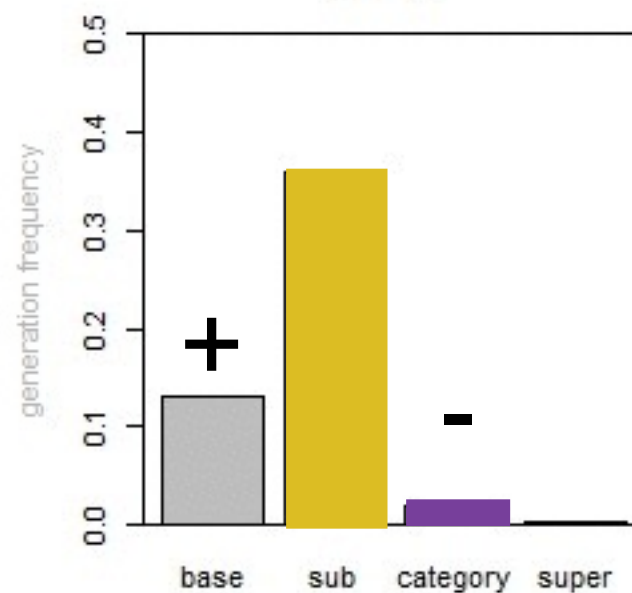
$A^+$



just Mozart  
classical music  
all music  
all sounds

Mozart+ Metallica-

$A^+ B^-$



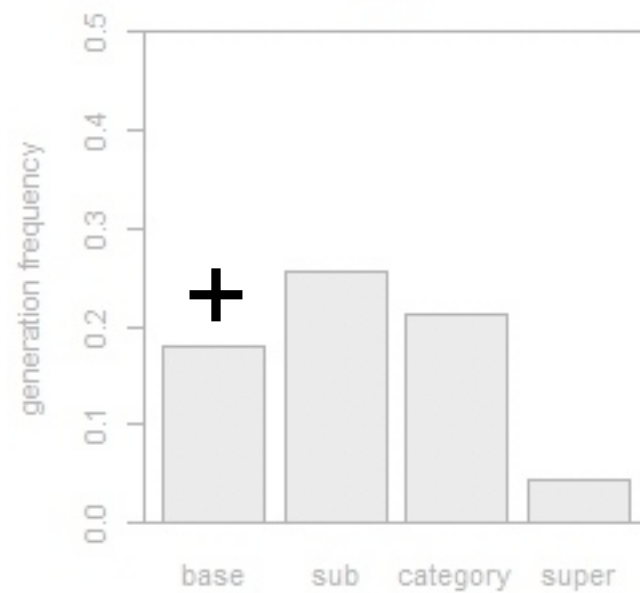
just Mozart  
classical music  
all music  
all sounds

And there it is.



Mozart+

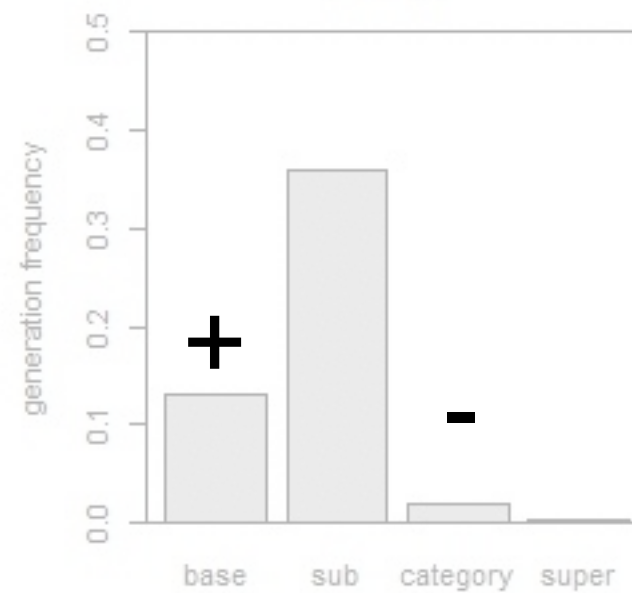
$A^+$



just Mozart  
classical music  
all music  
all sounds

Mozart+ Metallica-

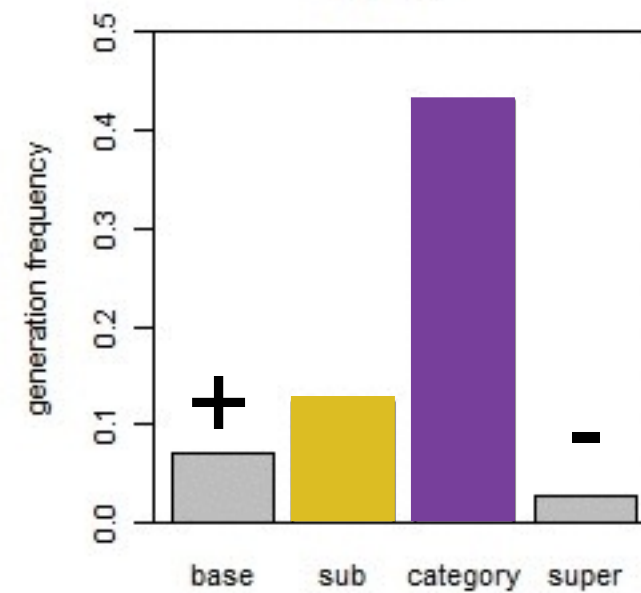
$A^+ B^-$



just Mozart  
classical music  
all music  
all sounds

Mozart+ Falling Rock-

$A^+ C^-$



just Mozart  
classical music  
all music  
all sounds

(aside: the actual experiment  
used many different arguments)

topic	premises			conclusions		
	subcat A	subcat B	cat C	A-member	B-member	C-member
MUSIC	Mozart	Metallica	falling rock	Bach	Nirvana	waterfall
PAINTERS	Rubens	Dahli	woodcarver	Van Eyck	Warhol	sculpturer
PUBLIC FIGURES	actors	librarians	moles	politicians	programmers	pheasants
SHIPS	freight ships	hovercrafts	cars	cruise ships	sail boats	rocks
GLASS	window glass	bottle glass	art glass	car glass	drinking glass	jewelry glass
DISPLAYS	LCD	television	paintings	plasma	traffic signs	book page
WATER BODIES	Atlantic	Balaton	mustard gass	Mediterranean	Silverlake	olive oil
WIND	flute	guitar	crying child	clarinet	violin	door
FRUIT	strawberries	banana's	grass blades	cranberries	apples	oak leafs
WATER BIRDS	ducks	sparrows	elephants	seagulls	blackbirds	camels
INSECTS	moths	spiders	lizzards	flies	centipede	goldfish
POLAR ANIMALS	polar bears	deer	sow bug	pinguins	parakeet	ant

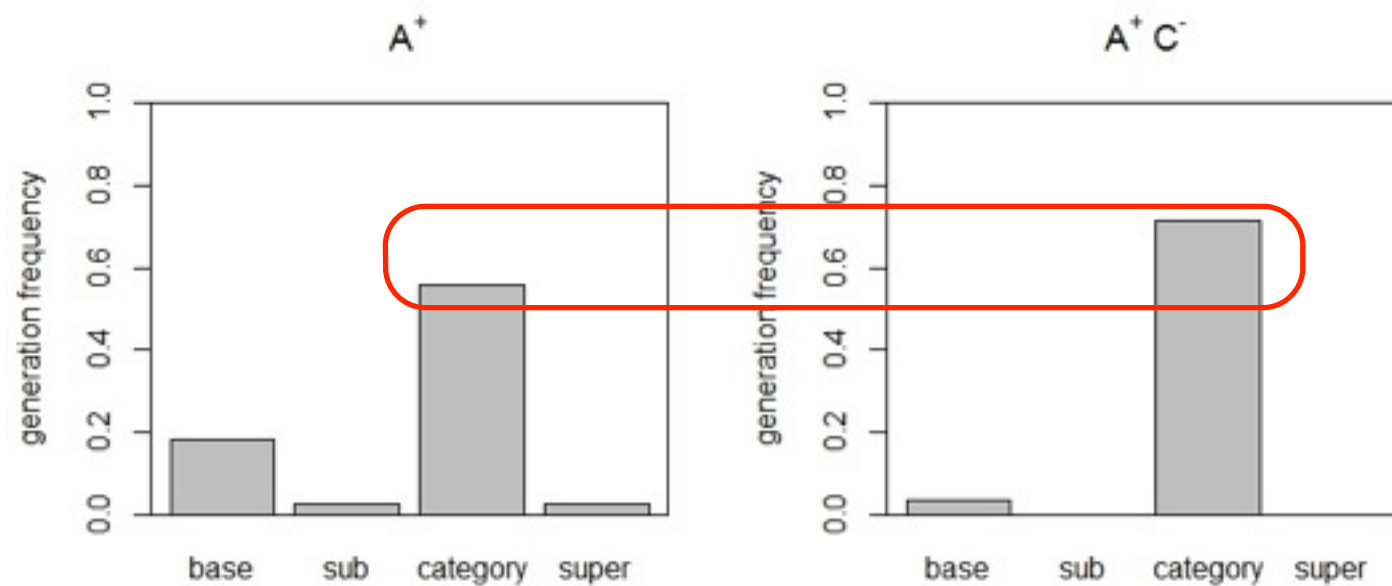
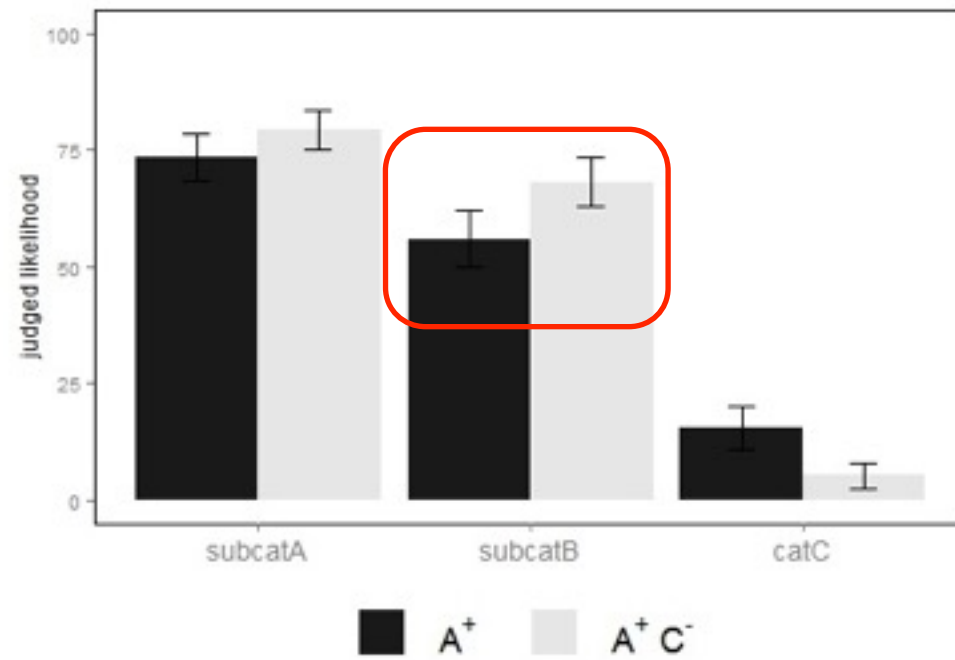
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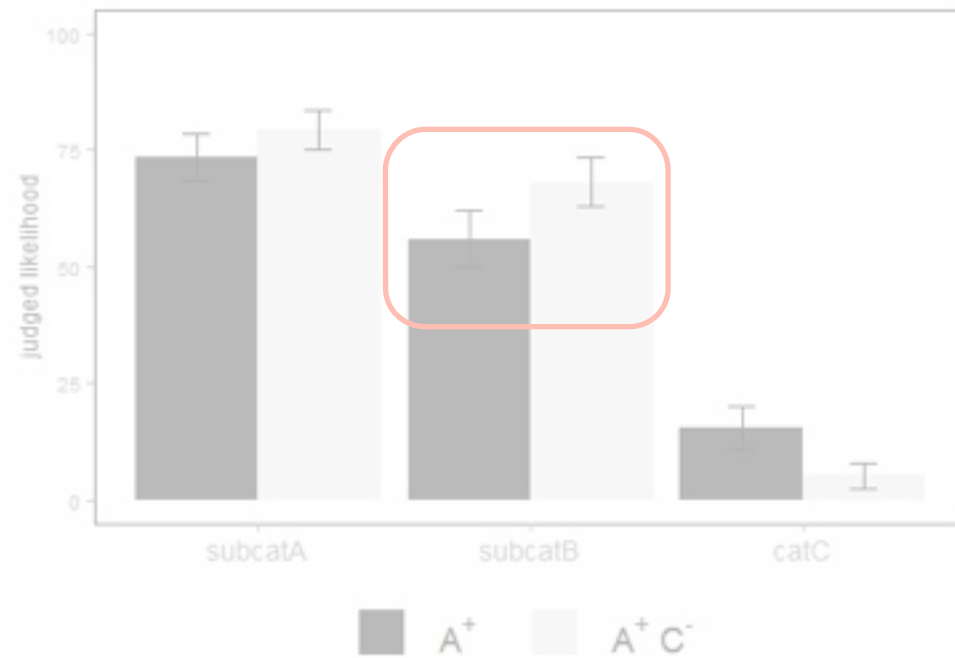
plus we ran an entire pseudo-  
replication with different items

topic	premises		conclusions		
	subcat A	cat C	A-member	B-member	C-member
MAMMALS	dog (+)	magpie (-)	wolf	donkey	blackbird
BIRDS	crow (+)	tuna fish (-)	raven	swan	halibot
FISH	salmon (+)	lizzard (-)	codfish	goldfish	snake
INSECTS	bee (+)	sparrow (-)	ant	cricket	pigeon

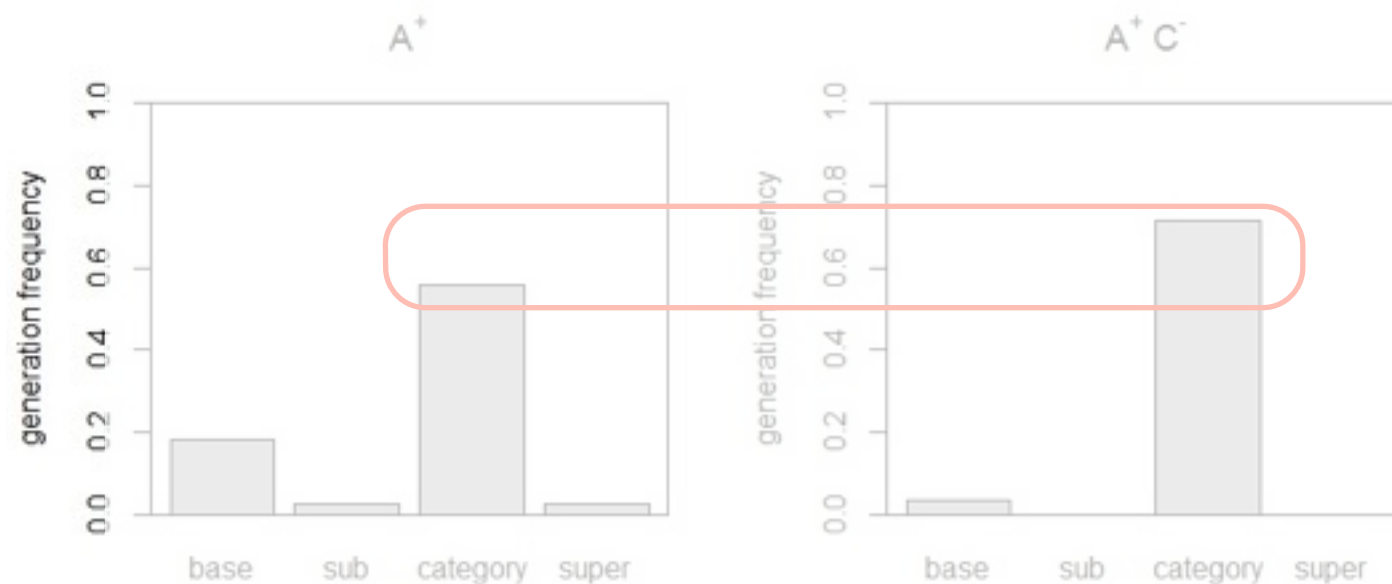
(and yes, the replication worked)



(and yes, the replication worked)

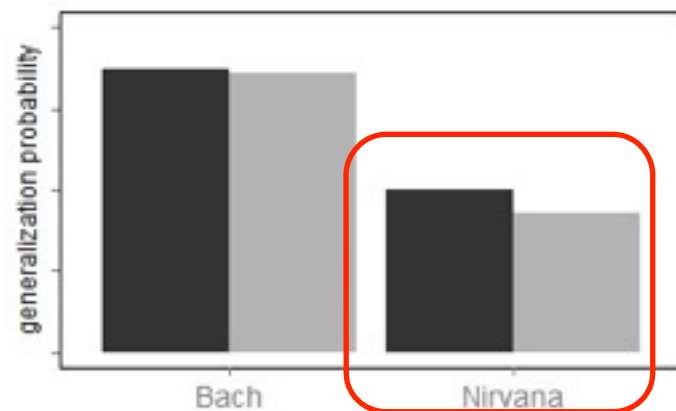


The big question is how to account for the results...

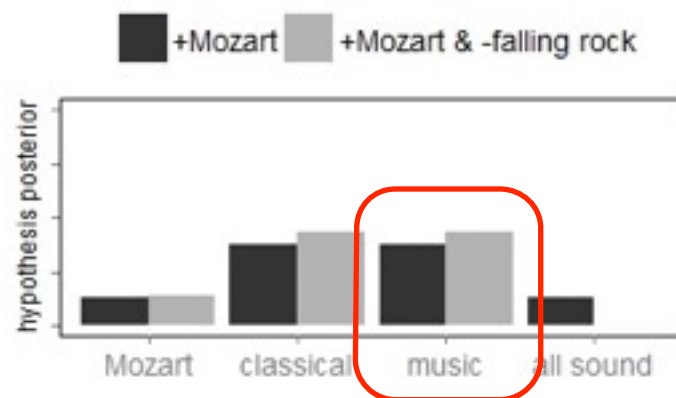


# Does the **weak sampling** model capture the effect?

## Weak sampling



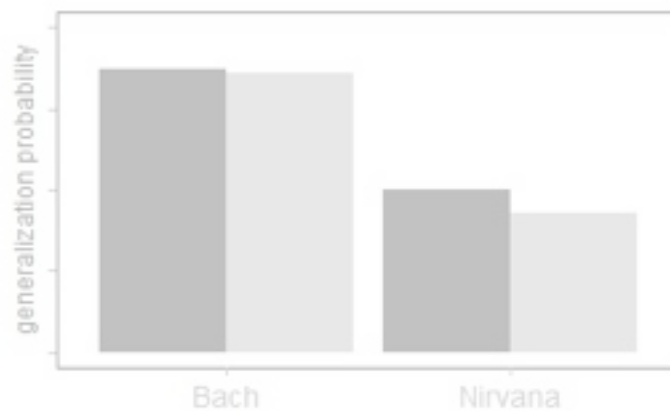
No, it predicts a null effect



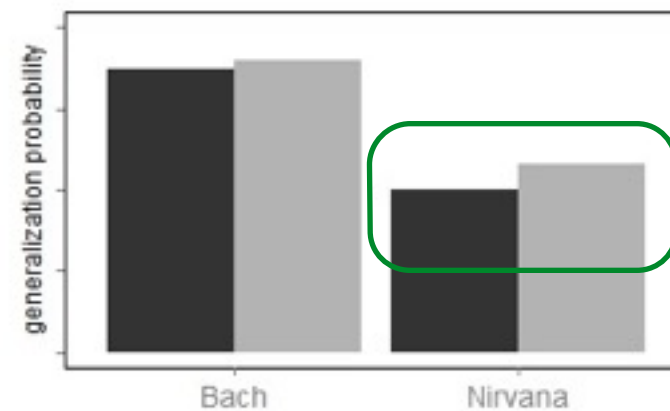


Okay, does the “strong sampling” model capture the effect?

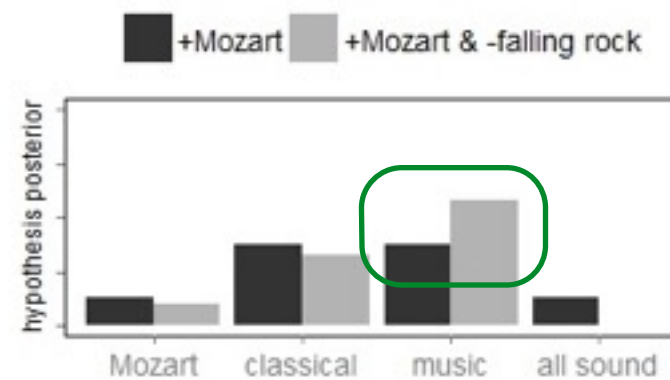
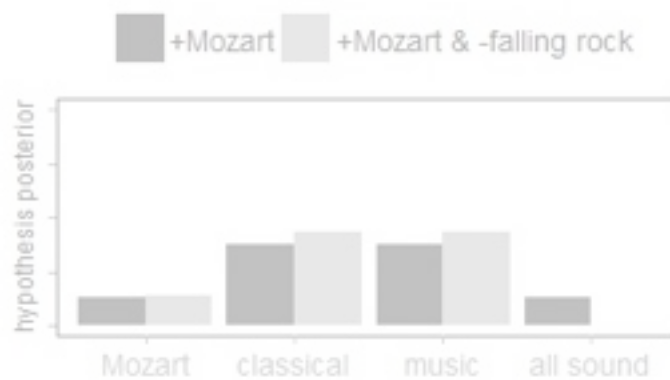
Weak sampling



Strong sampling

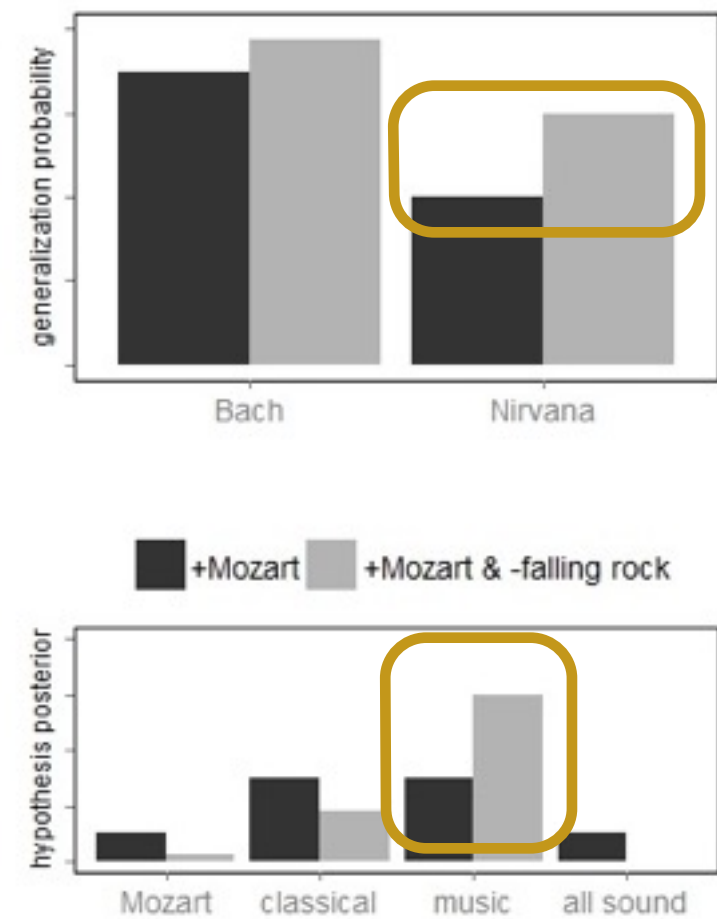


Yes, but the effect is much smaller than the empirical one



(people are out-Bayesing Bayes??)

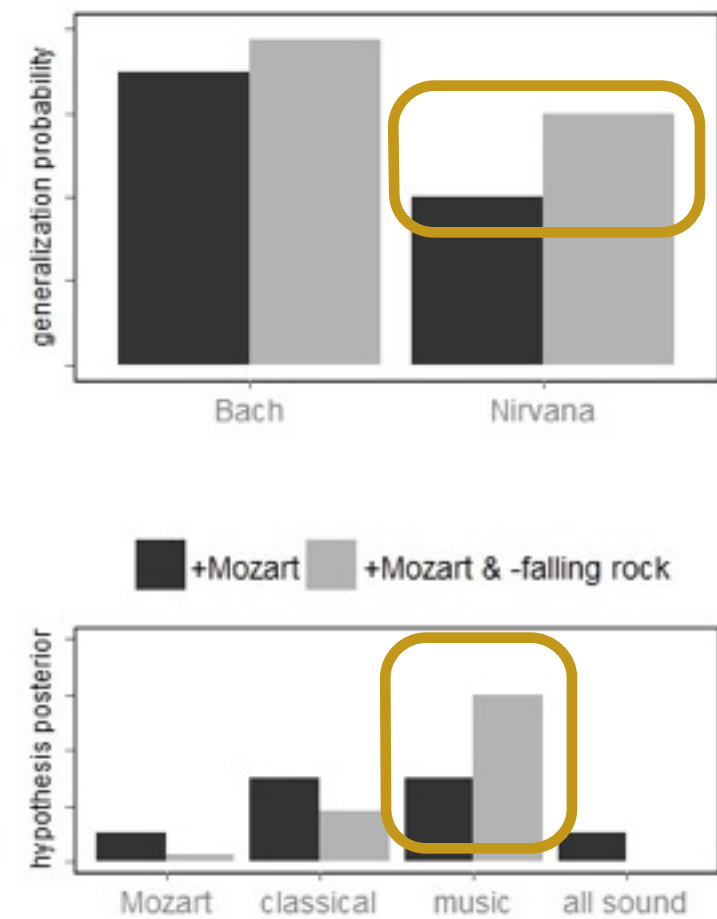
Well, here's a model that gets the  
effect size right...



But Bayes is going to  
need a fancier hat...



## Pedagogical sampling



Weak sampling



An argument consists of random true statements about the world

Weak sampling



An argument consists of random true statements about the world

Strong sampling



An argument consists of randomly selected facts particular to a target category



Weak sampling



An argument consists of random true statements about the world

Strong sampling



An argument consists of randomly selected facts particular to a target category

Pedagogical /  
persuasive  
sampling



An argument consists of purposefully chosen facts designed to convince an intelligent reasoner of the truth of some proposition

$$P(x|h) \propto P(h|x)^\alpha$$

The data  $x$   
selected by the  
communicator...

... is designed to  
maximise the  
learner's posterior  
degree of belief in  
hypothesis  $h$

If that's right, then the same manipulation we used in the previous study should work...

If the negative example is perceived as a “helpful hint” we should continue to get the effect



If it is construed as an arbitrary fact, the effect should vanish

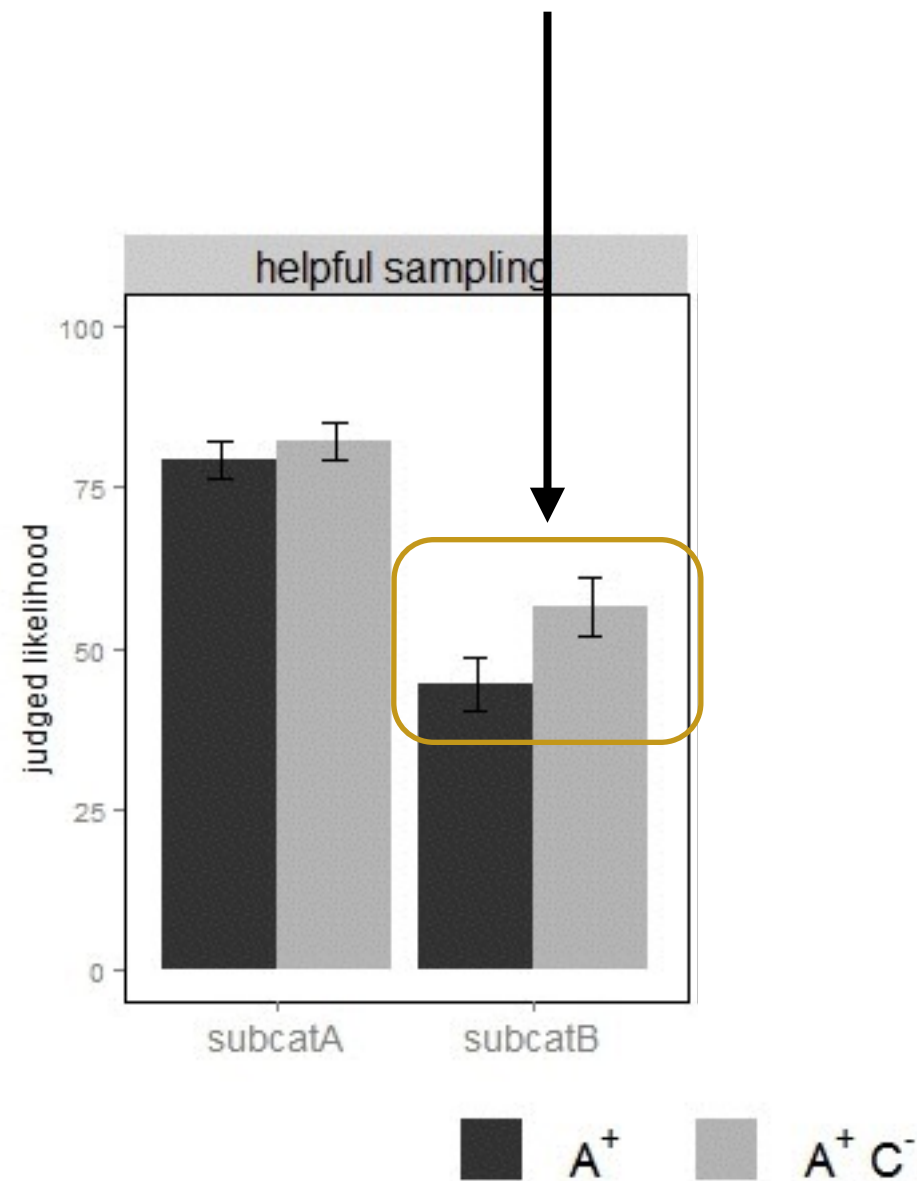




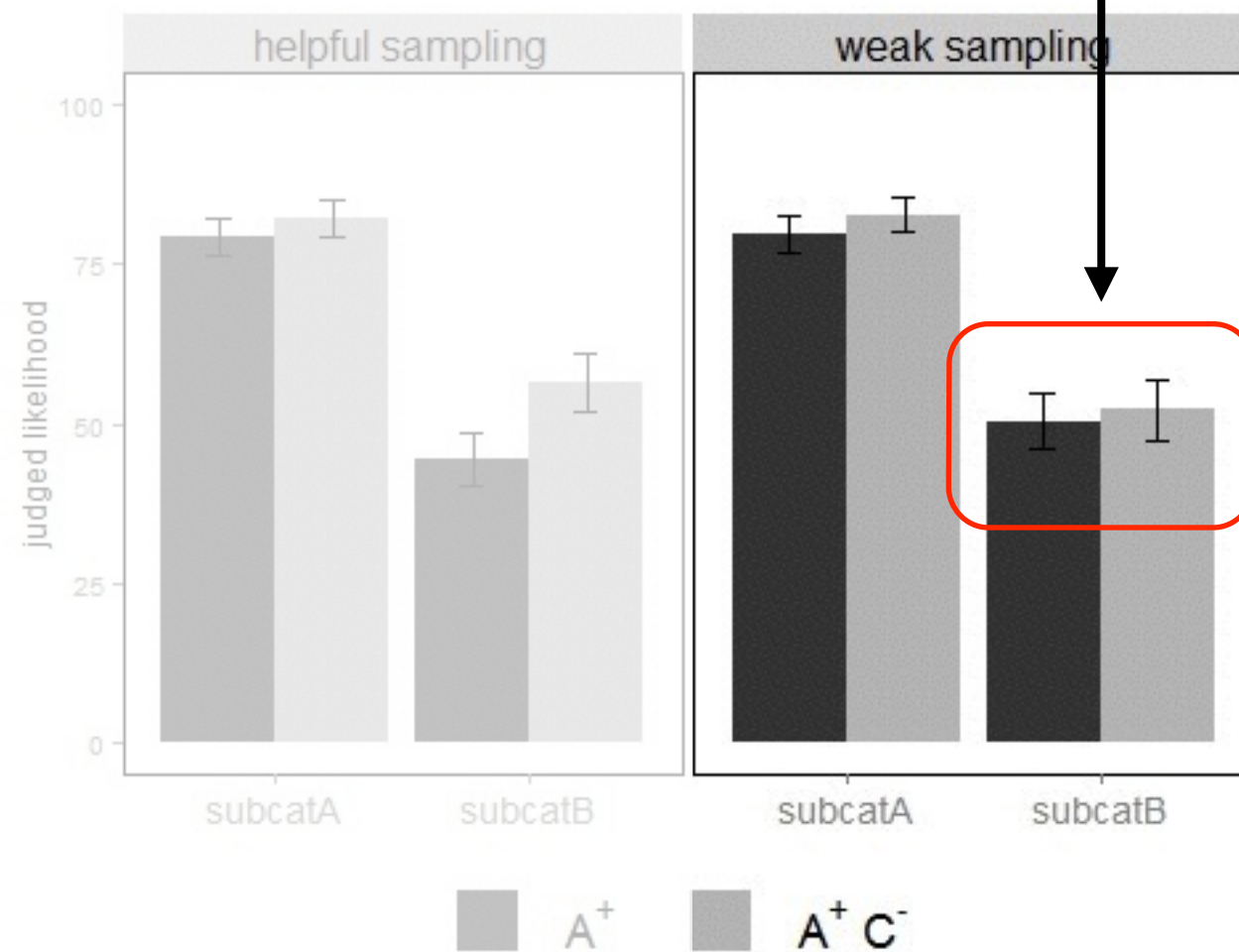
	<b>topics</b>		A-member	B-member
	premise 1 (+)	premise 2 (-)		
MUSIC	Mozart	waterfall	Bach	Nirvana
FRUIT	strawberries	grass blades	blackberry	apple
BIRDS	ducks	elephants	swan	blackbird
TYPES OF WATER	Atlantic ocean	tap water	Mediterranean	Lake Balaton
<b>fillers weak sampling</b>				
	premise 1	premise 2	conclusion 1	conclusion 2
EXAMPLE	sheep (+)	dogs (-)	horses	chickens
TRIAL 1	aluminium (+)	lead (+)	copper	tin
TRIAL 2	Earth (+)	weather satelite (-)	Uranus	Sun
FILLER	physicists (+)	engineers (+)	mathematicians	carpenters
FILLER	cobras (+)	iguanas (-)	pythons	sea turtles
<b>fillers helpful sampling</b>				
	premise 1	premise 2	conclusion 1	conclusion 2
EXAMPLE	sheep (+)	cows (+)	horses	pigs
TRIAL 1	aluminium (+)	brass (-)	copper	lead
TRIAL 2	Earth (+)	Mars (+)	Uranus	Sun
FILLER	cobras (+)	pythons (-)	vipers	anacondas
FILLER	physicists (+)	mathematicians (+)	chemists	carpenters

200 participants on MTurk

Adding negative evidence as a “hint”  
produces the effect, as before



Presenting it as an arbitrary fact makes  
the effect vanish...



- The social aspect to inductive reasoning is central
  - By default, people seem to “read” an inductive argument as if it were put together for a purpose
- Pedagogical sampling as normative standard
  - In real life, arguments aren't collections of facts
  - They're acts of persuasion
  - If so, shouldn't “normative” accounts reflect that?



Let's make the social aspect explicit:

The role of goals and social reasoning  
when aggregating expert opinions





Navarro, Dry & Lee (2012). Sampling assumptions in inductive generalization. *Cognitive Science*



Hendrickson, Perfors & Navarro (in preparation). One cat, two cats: Sampling models in different category learning tasks produce qualitatively different inductive generalisations



Ransom, Perfors & Navarro (in press). Leaping to conclusions: Why premise relevance affects argument strength. *Cognitive Science*



Voorspoels, Navarro, Perfors, Ransom & Storms (under revision). How do people learn from negative evidence? Non-monotonic generalizations and sampling assumptions in inductive reasoning. *Cognitive Psychology*



Perfors, Navarro & Shafto (in preparation). Stronger evidence isn't always better: The role of social inference in evidence selection and interpretation. Previously rejected from *JEP:G*

**You're a journalist writing an article about  
expert opinions about climate change...**

# You're a journalist writing an article about expert opinions about climate change...



93% likely



95% likely



97% likely



92% likely



99% likely



91% likely



89% likely



# You're a journalist writing an article about expert opinions about climate change...



93% likely



95% likely



97% likely



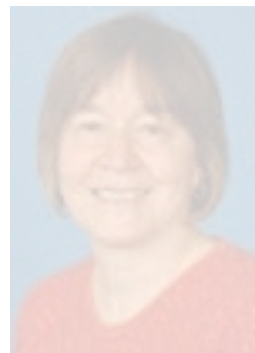
5% likely



92% likely



99% likely



91% likely



89% likely



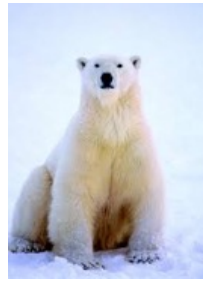
93



95



97



92



99



91



89



5

Here's your full  
distribution of  
expert opinion

Your editor says the article only has room for  
(at most) three quotes. Who to choose??



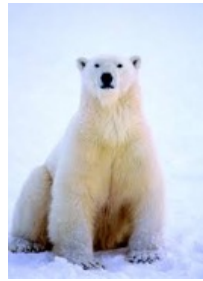
93



95



97



92



99



91



89



5



99



93



91

Do you quote only from the consensus?



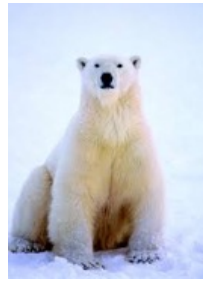
93



95



97



92



99



91



89



5



99

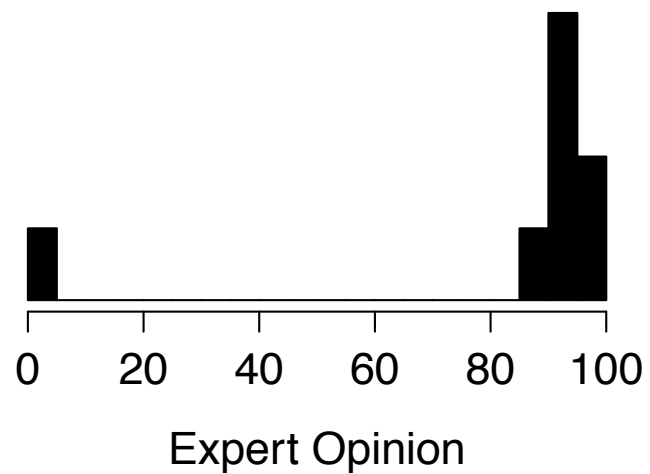


93

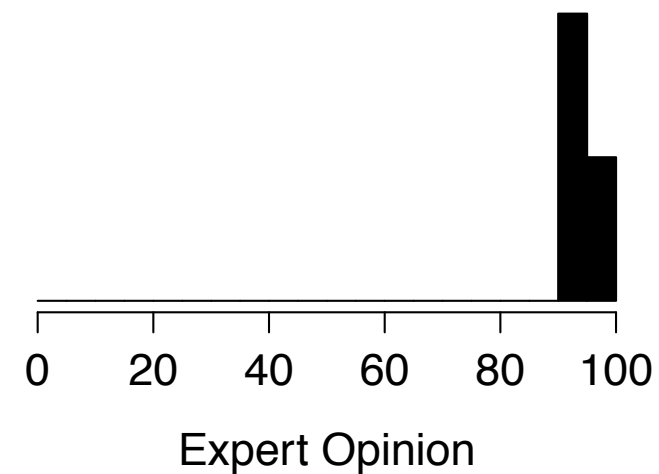


91

Full Distribution



Quoted Distribution



(maximises distributional similarity)



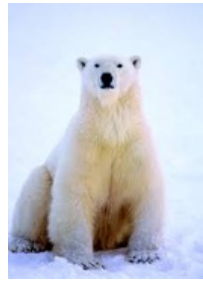
93



95



97



92



99



91



89



5



99



93



5

Or do you include the dissenter?





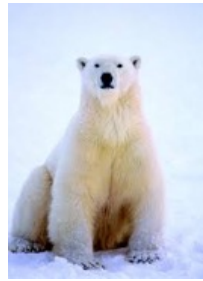
93



95



97



92



99



91



89



5



99

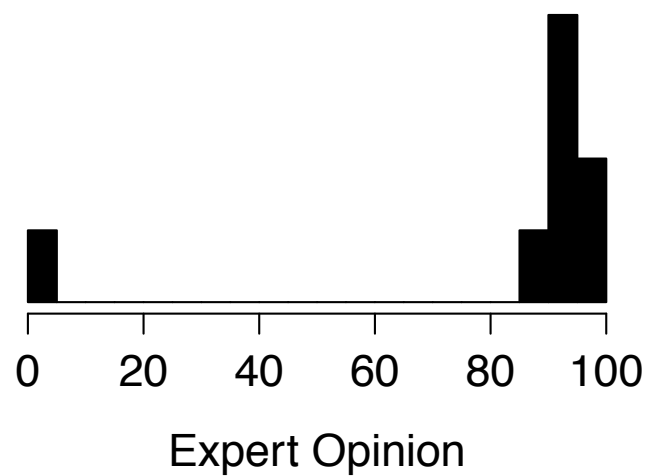


93

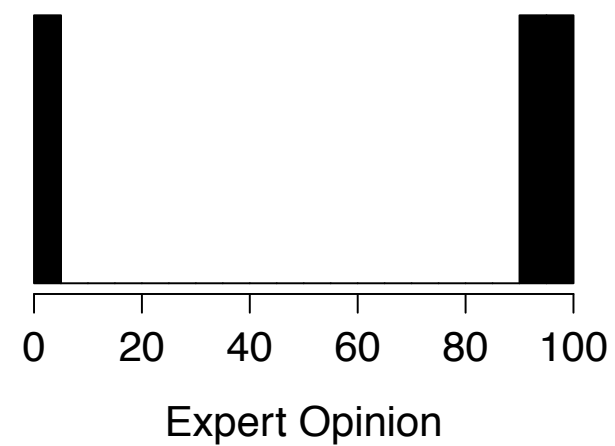


5

Full Distribution

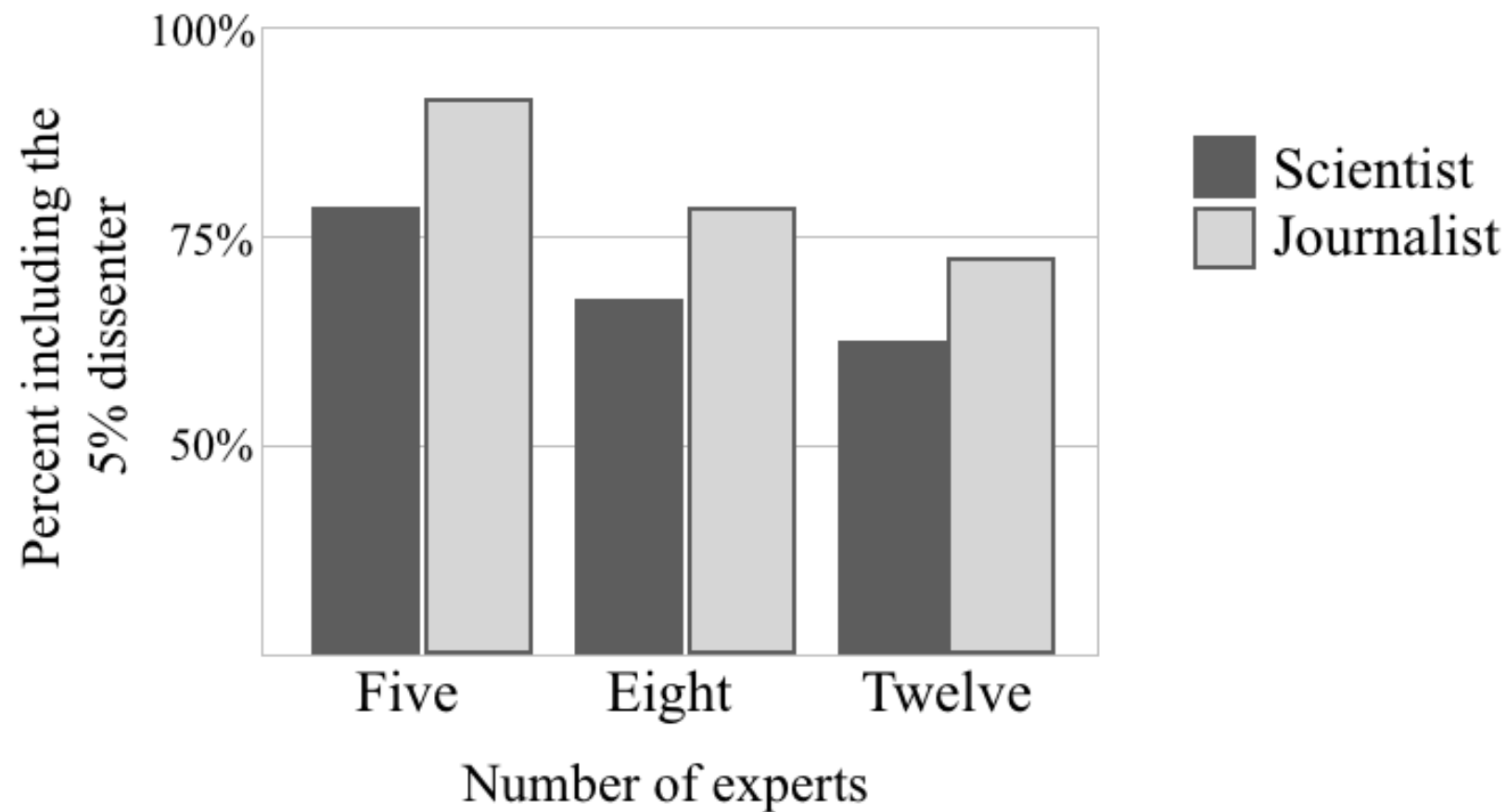


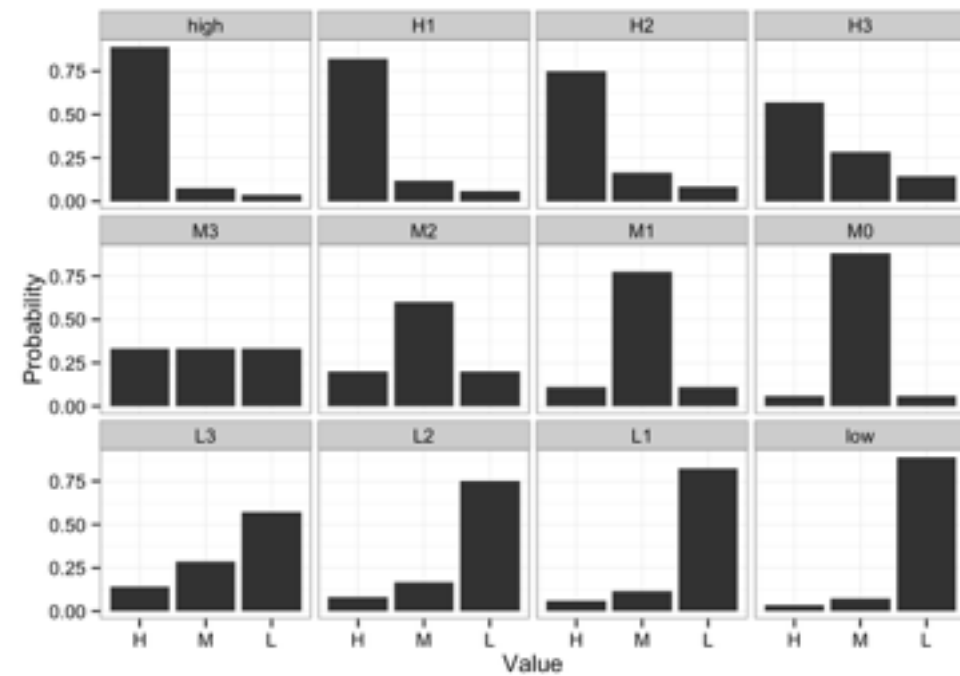
Quoted Distribution



(“full spectrum” but terrible approximation)

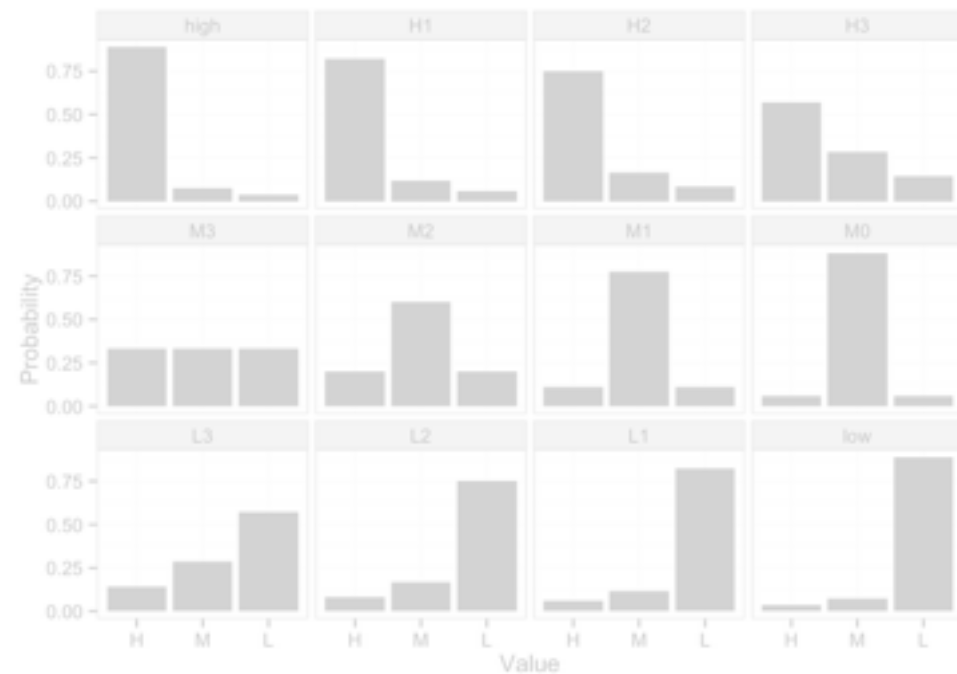
Some empirical data. Even when outnumbered 11 to 1, most people choose to quote the contrarian.





A hypothesis space  
of possible expert  
distributions





A hypothesis space  
of possible expert  
distributions

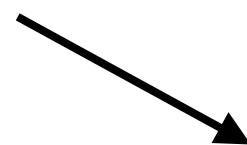
A hypothesis space  
of possible  
journalistic agendas

“Helpful”

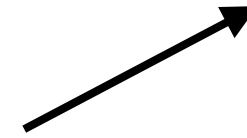


Communicate the  
true distribution

“Bias high”



“Bias low”



Communicate a  
distribution with  
highest/lowest mean

Select evidence to manipulate  
the reader's beliefs



Bayesian writer



Bayesian reader

Select evidence to manipulate  
the reader's beliefs



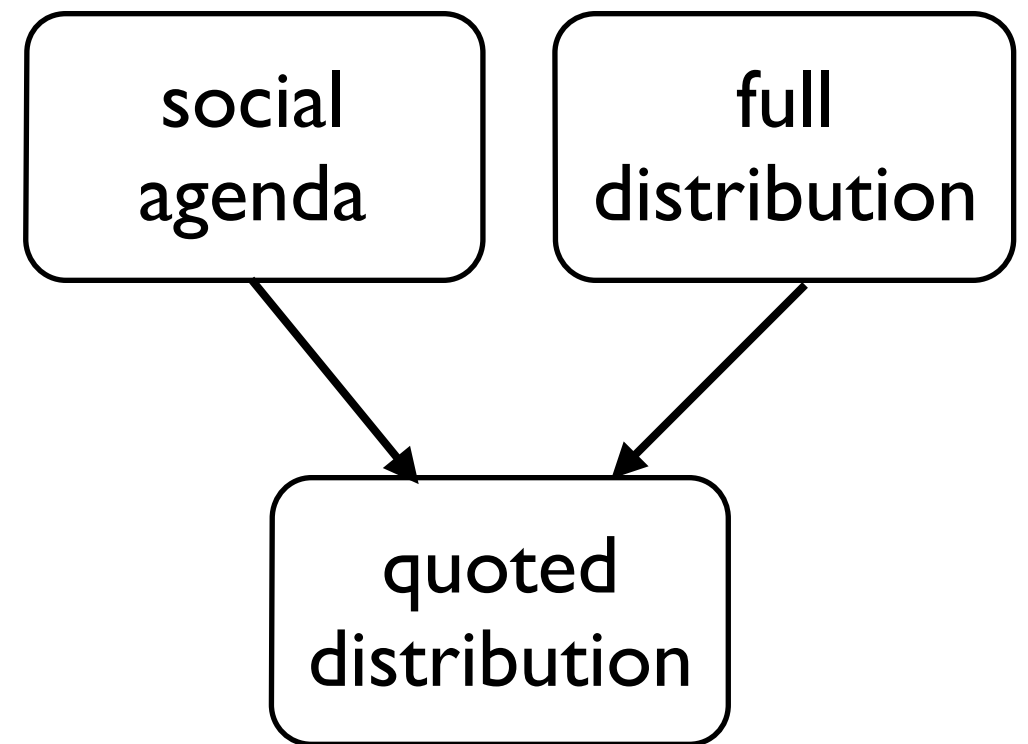
Bayesian writer



Bayesian reader

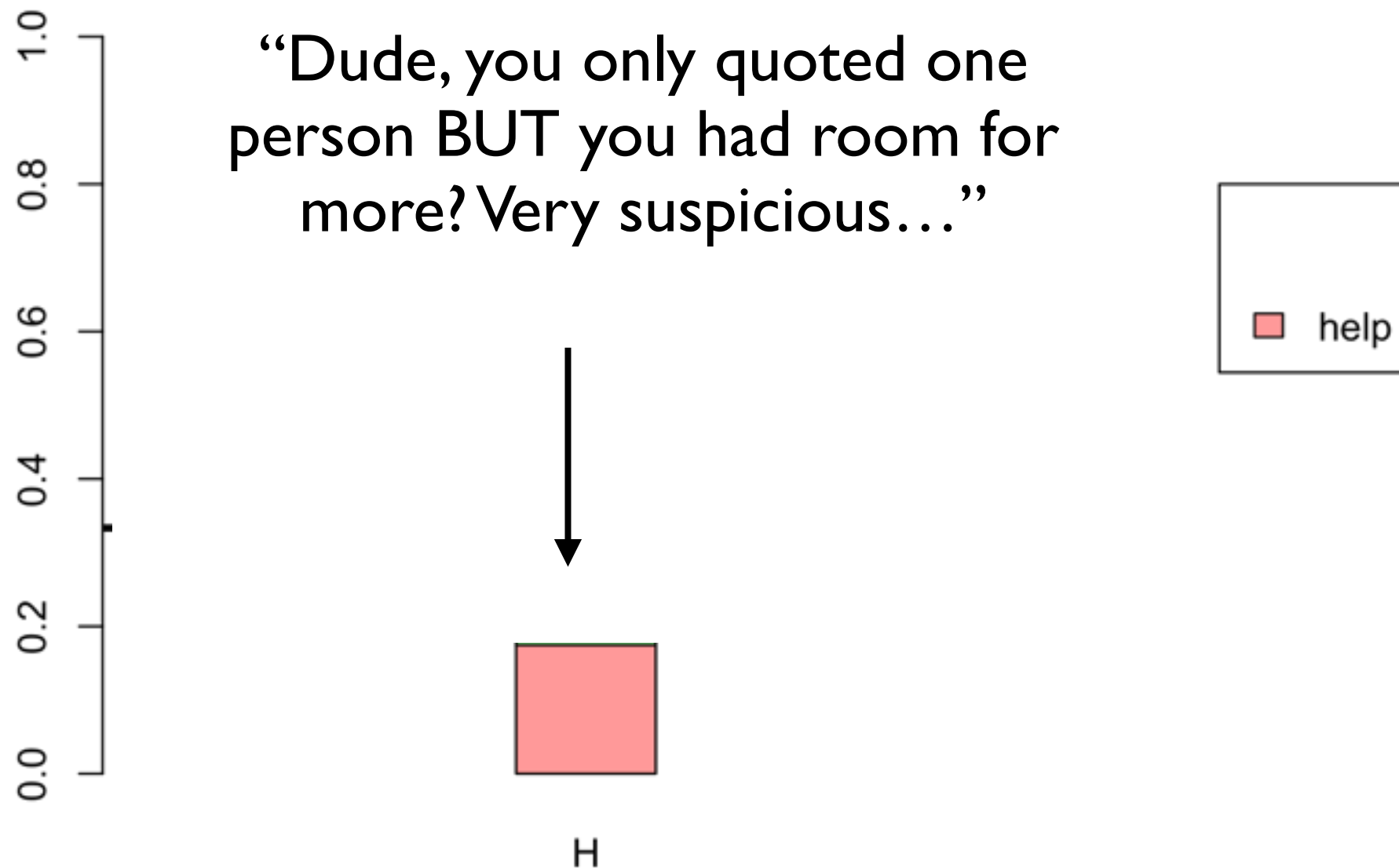
Guess the true distribution AND  
infer the journalistic agenda

# So what does a Bayesian reader infer about the Bayesian writer?

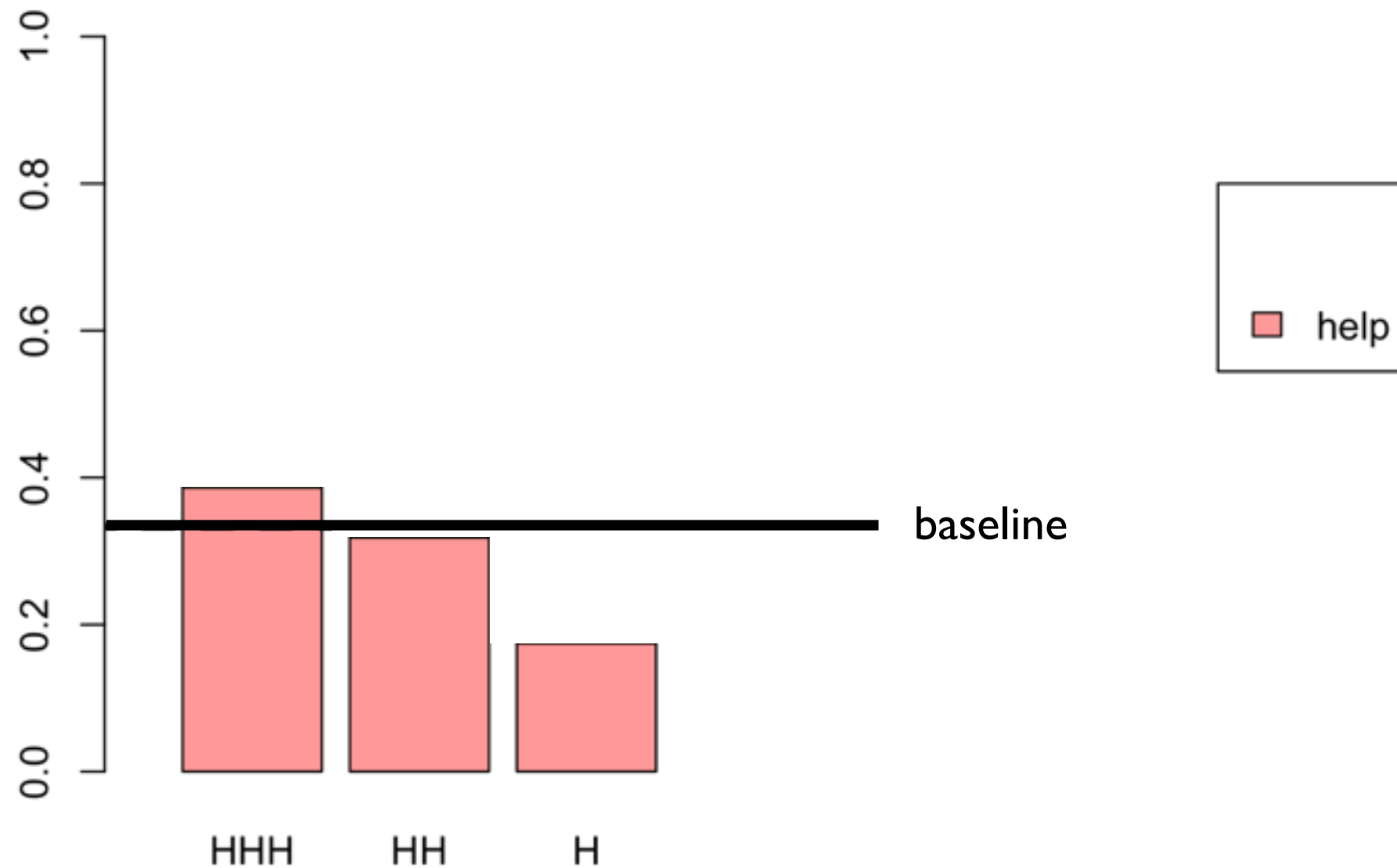


(I'll assume uniform priors over possible agendas and over possible distributional hypotheses)

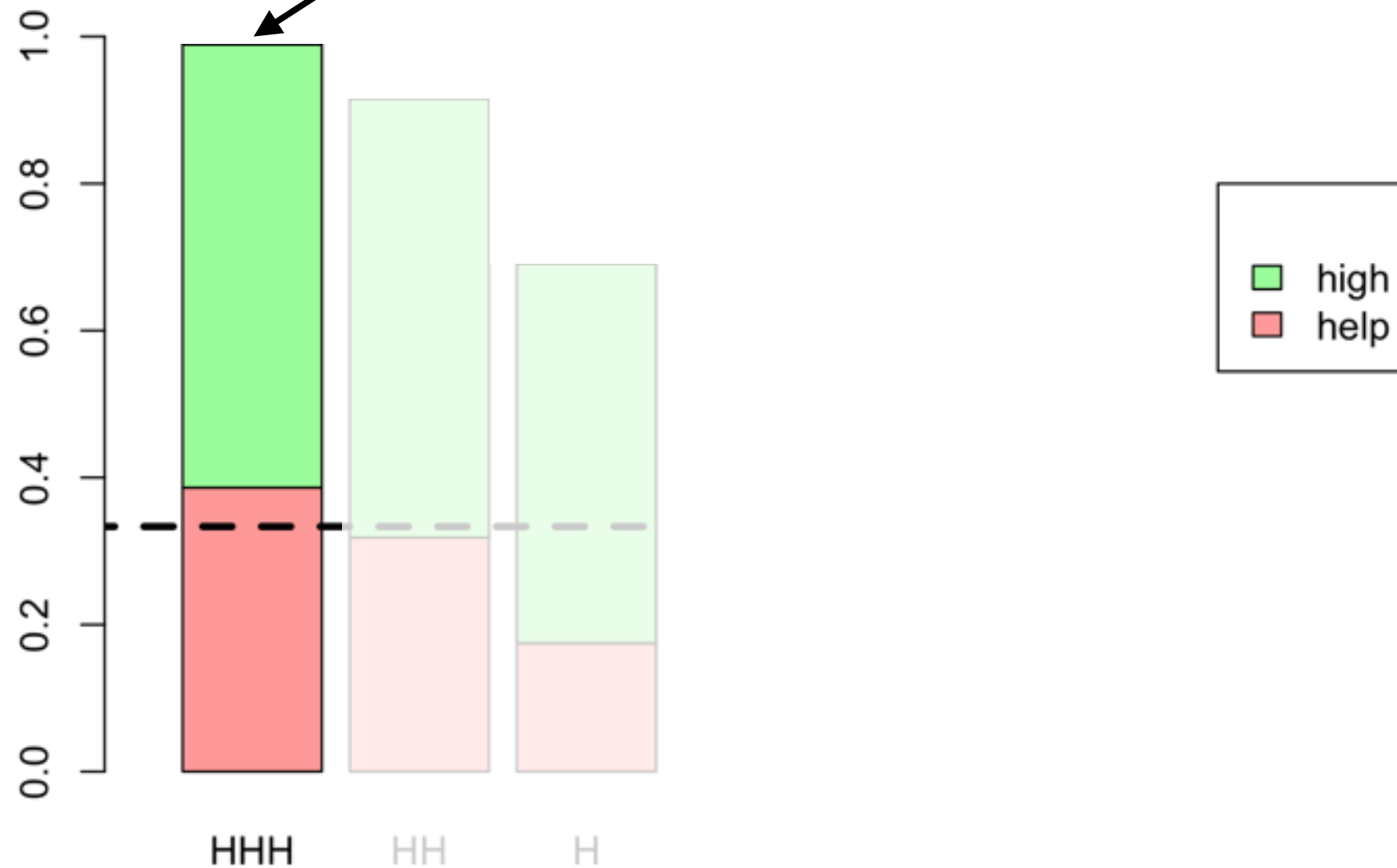
# Quoting one expert only looks suspicious



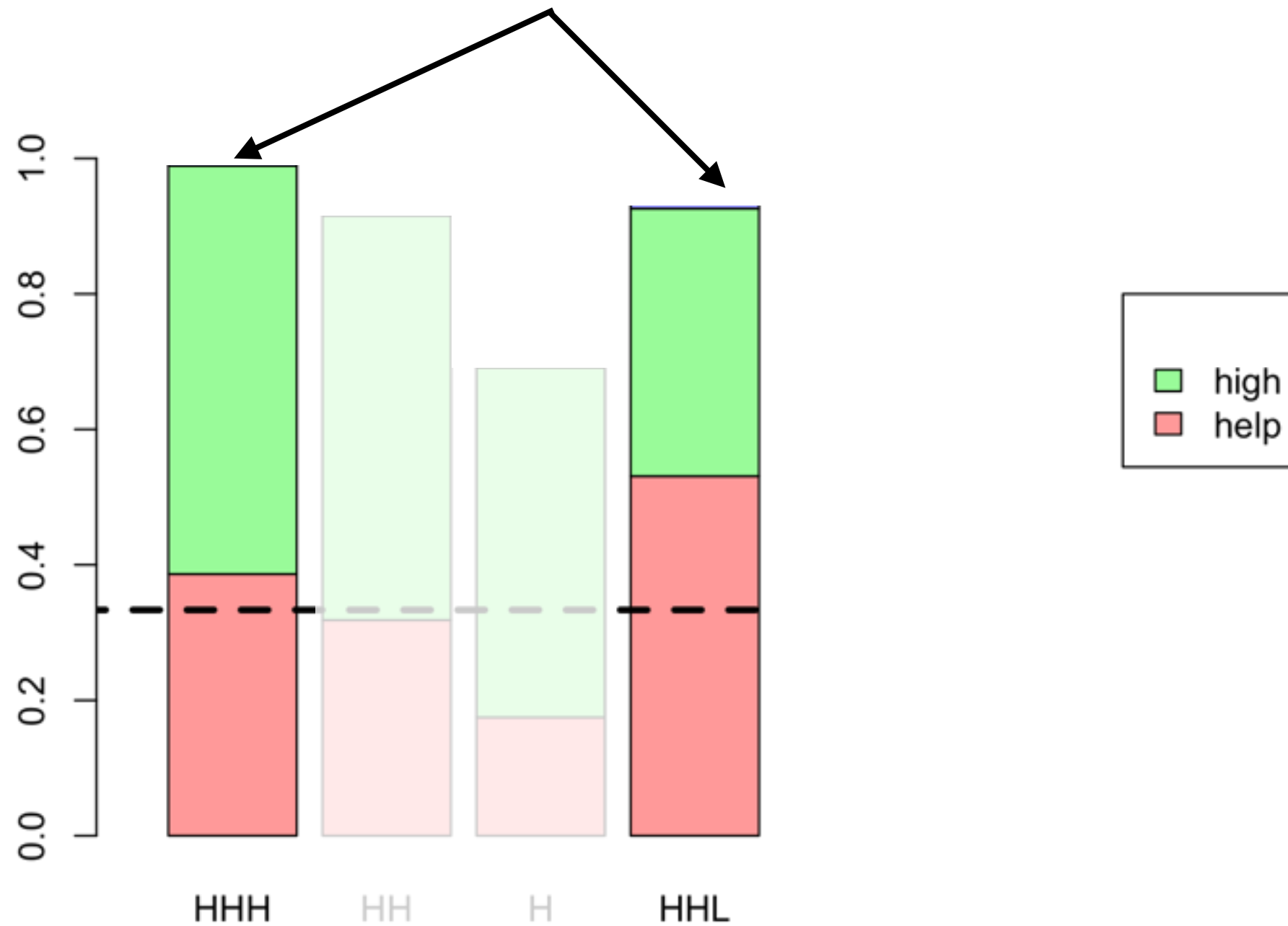
Anything less than maximum  
number of experts causes a  
deterioration of trust



But when all the quoted experts agree, the reader thinks you're probably biased



You can increase the reader's trust  
by including the contrarian



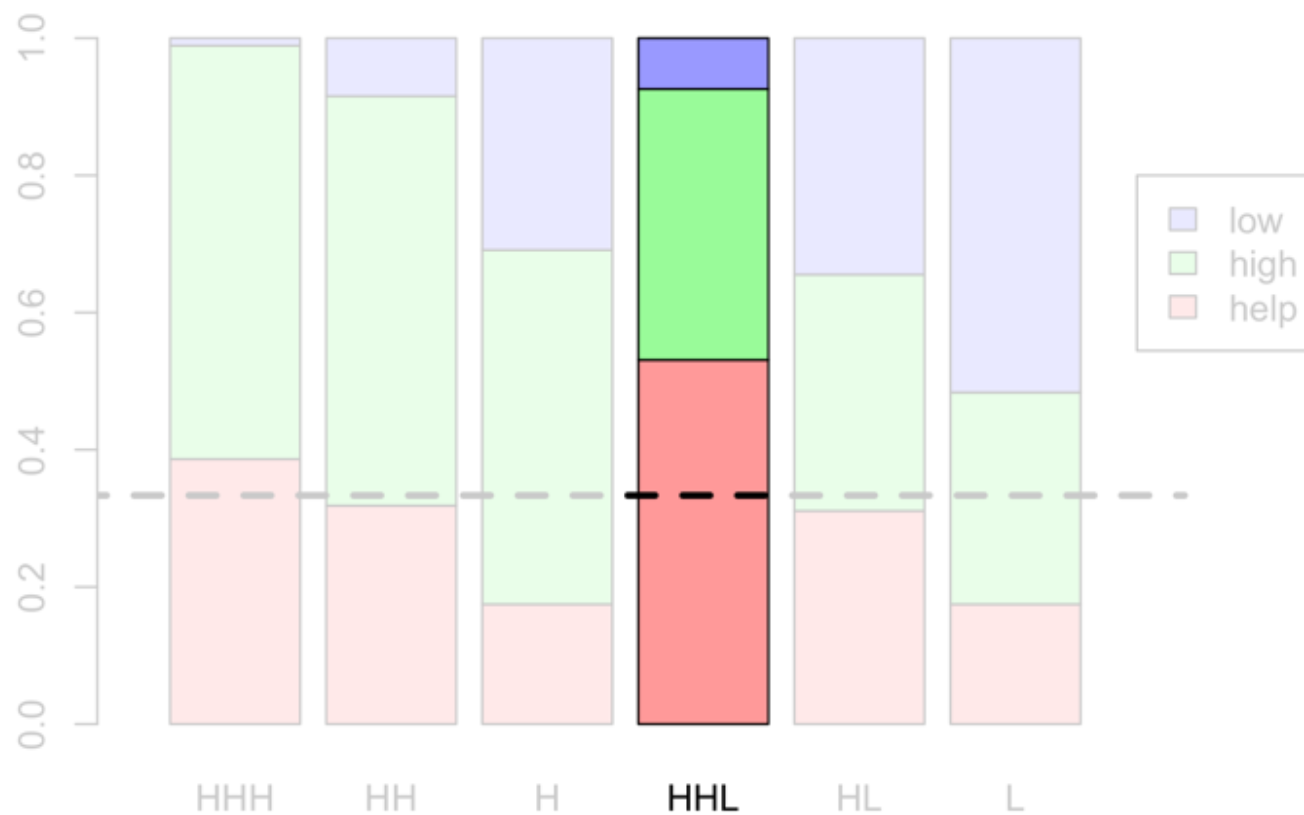




A Bayesian journalist who cares about their reputation has a strong motivation to pursue “he says she says” journalism



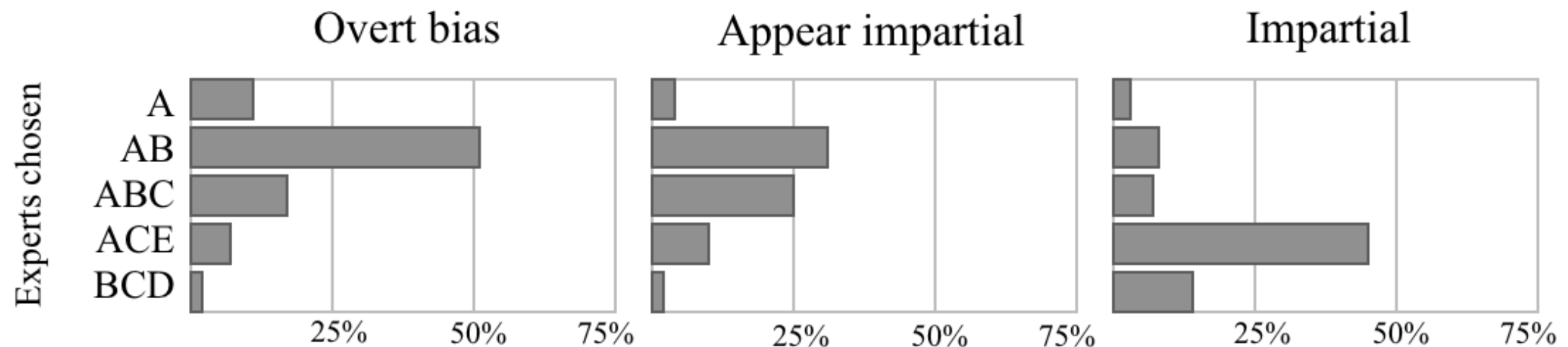
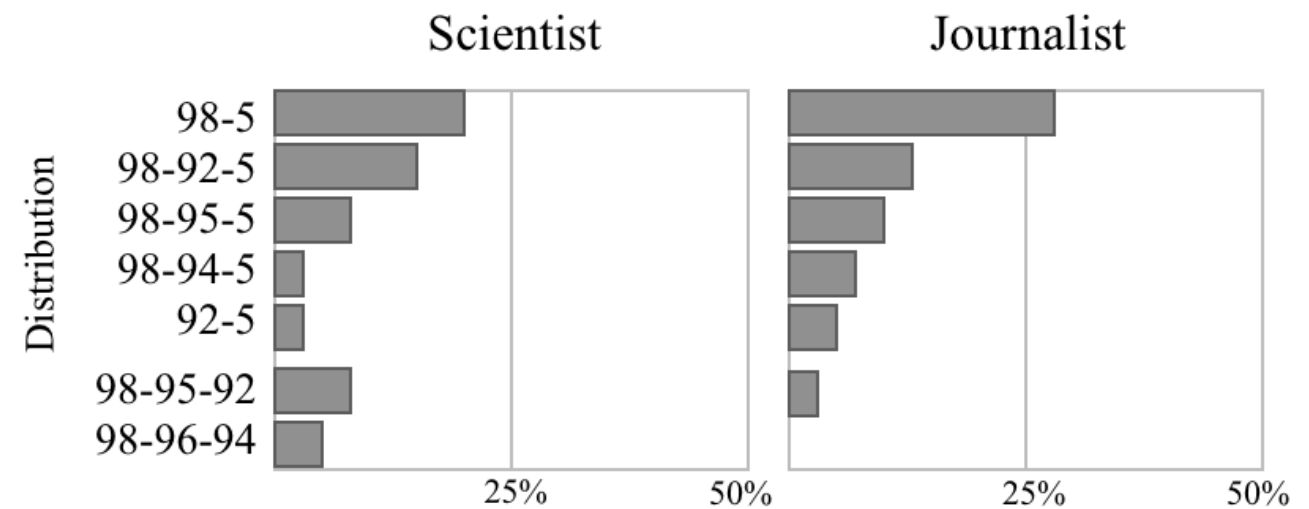
A Bayesian journalist who cares about their reputation has a strong motivation to pursue “he says she says” journalism



Because a Bayesian reader can't tell the difference between journalistic bias and expert consensus

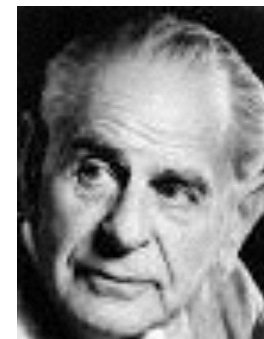
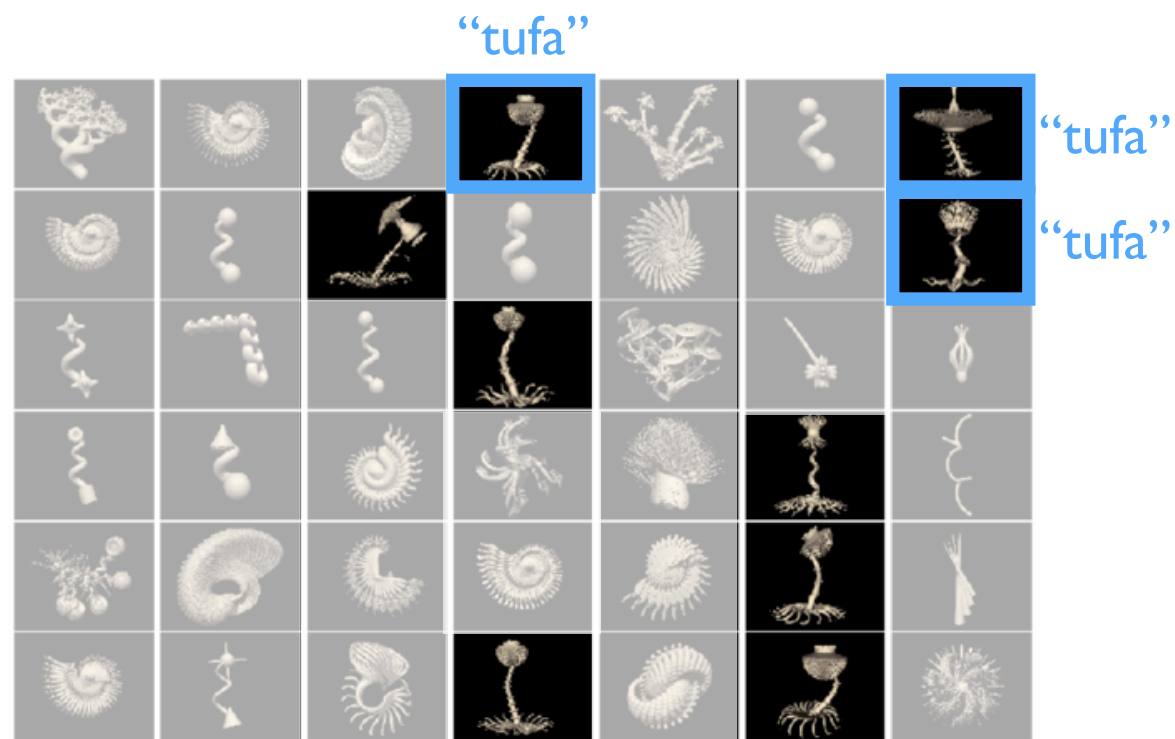
# Oh, and we have a heap of other data and modelling on this too, but I have no time...

Tr	Goal	Story	Distribution	
●	Overt bias	Restaurant reviewer	A B C D E	Uniform
●	Impartial	Documentary maker	86 80 51 10 6	
●	Appear impartial	Advisor to minister	90 85 55 13 8	
●	Overt bias	Lawyer	94 89 59 17 12	
			98 92 63 22 18	
●	Scientist (impartial no matter what)		98 96 94 92 5	Skewed
	Journalist (impartial + reputation)		98 96 95 95 95 94 92 5	
			98 97 96 96 95 95 95 94 94 93 92 5	
●	"Check" question for validation purposes		100 100 50 1 1	



A few final thoughts about human reasoning and Bayesian reasoning

Traditional accounts of learning and inference specify norms that implicitly rely on something like falsificationist reasoning

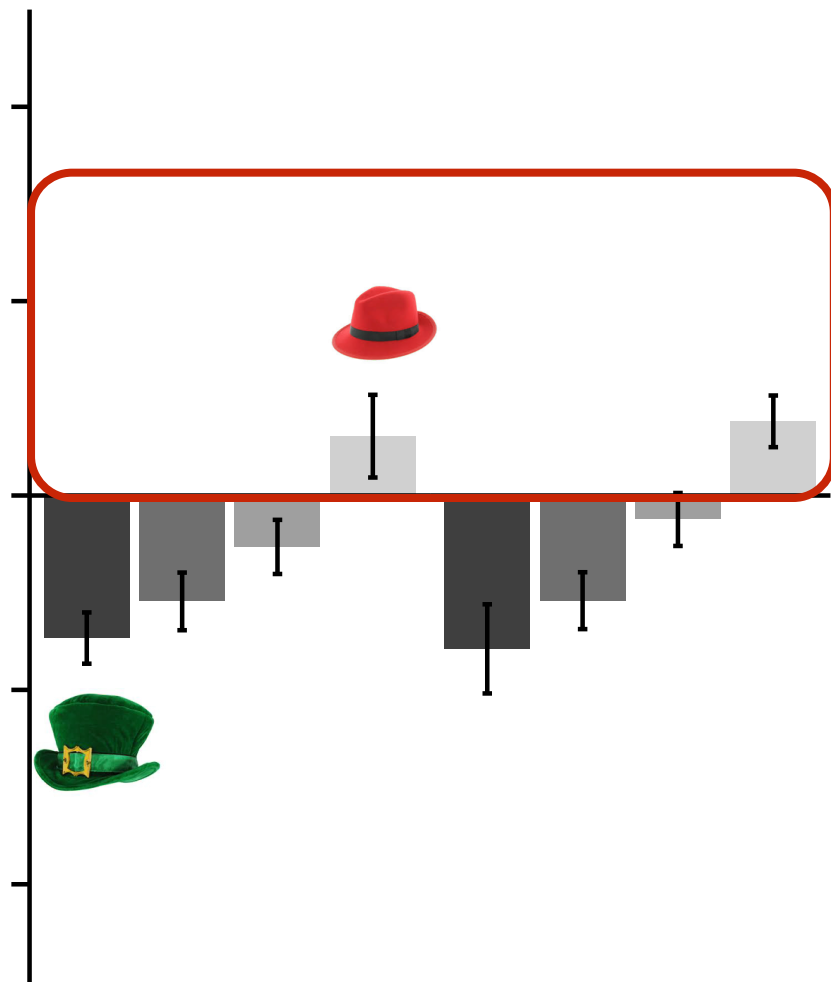


falsificationist  
learning



weak sampling

# But why?

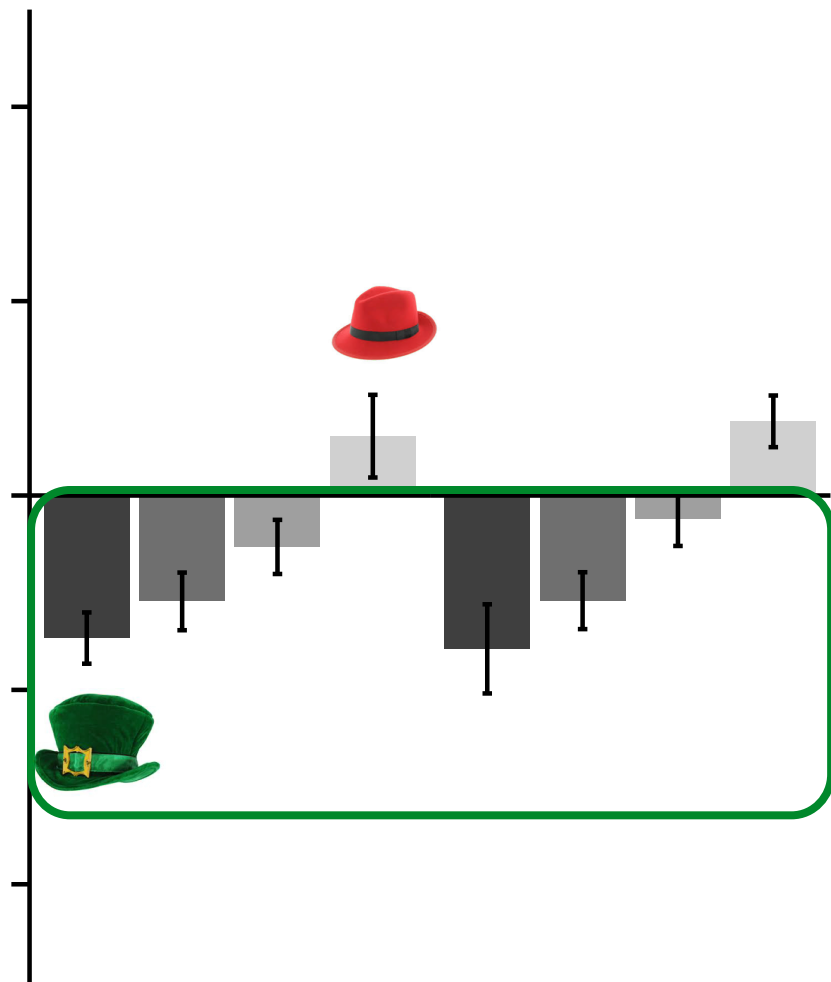


... it only makes sense when evidence is selected in an arbitrary and random fashion

Both Random ←



In real life, isn't  
**ANYTHING ELSE** a more  
reasonable theory for the  
origin of the data????



■ Both Relevant   ■ Relevant Fillers  
■ Random Fillers







“Common sense” inference requires people to learn from complex (and smart) data sources...





social  
agenda

full  
distribution

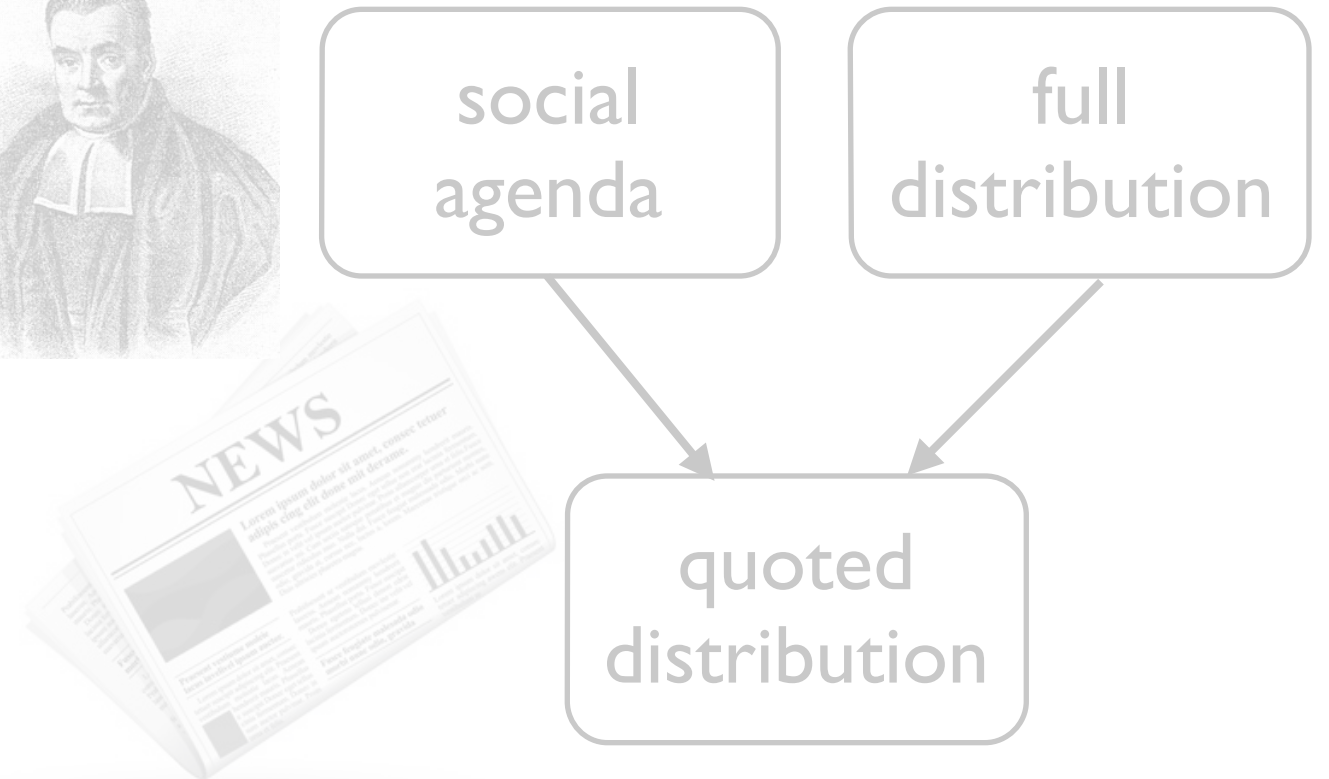


quoted  
distribution

We need to disentangle  
facts from agendas



We need to  
detect trickery





social  
agenda

full  
distribution



quoted  
distribution



We need to detect  
novelty and invariances in  
a dynamic world



social  
agenda

full  
distribution



quoted  
distribution

We need to read the  
intention of other agents





# Understanding human common sense reasoning requires something a lot richer



Thanks!